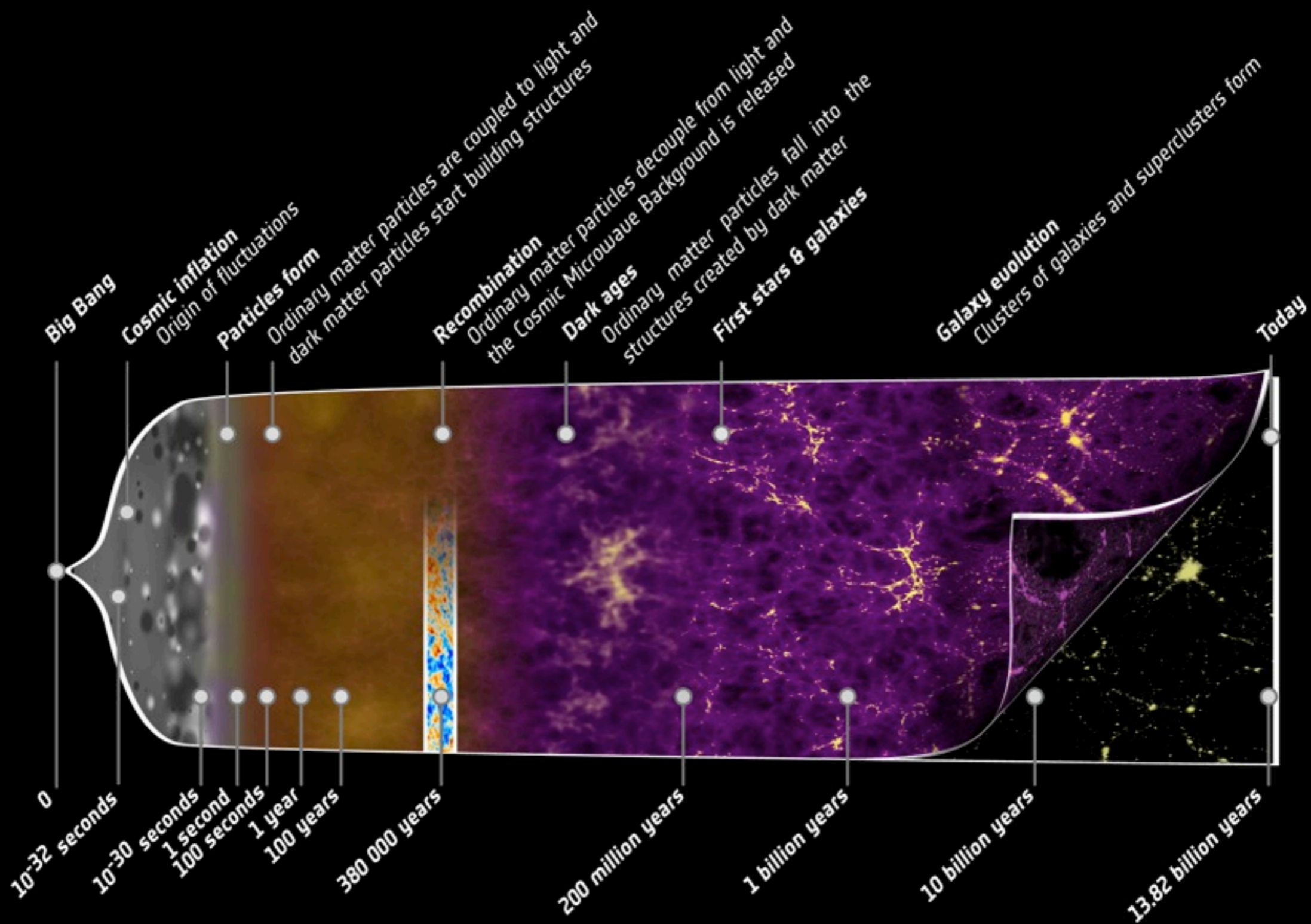


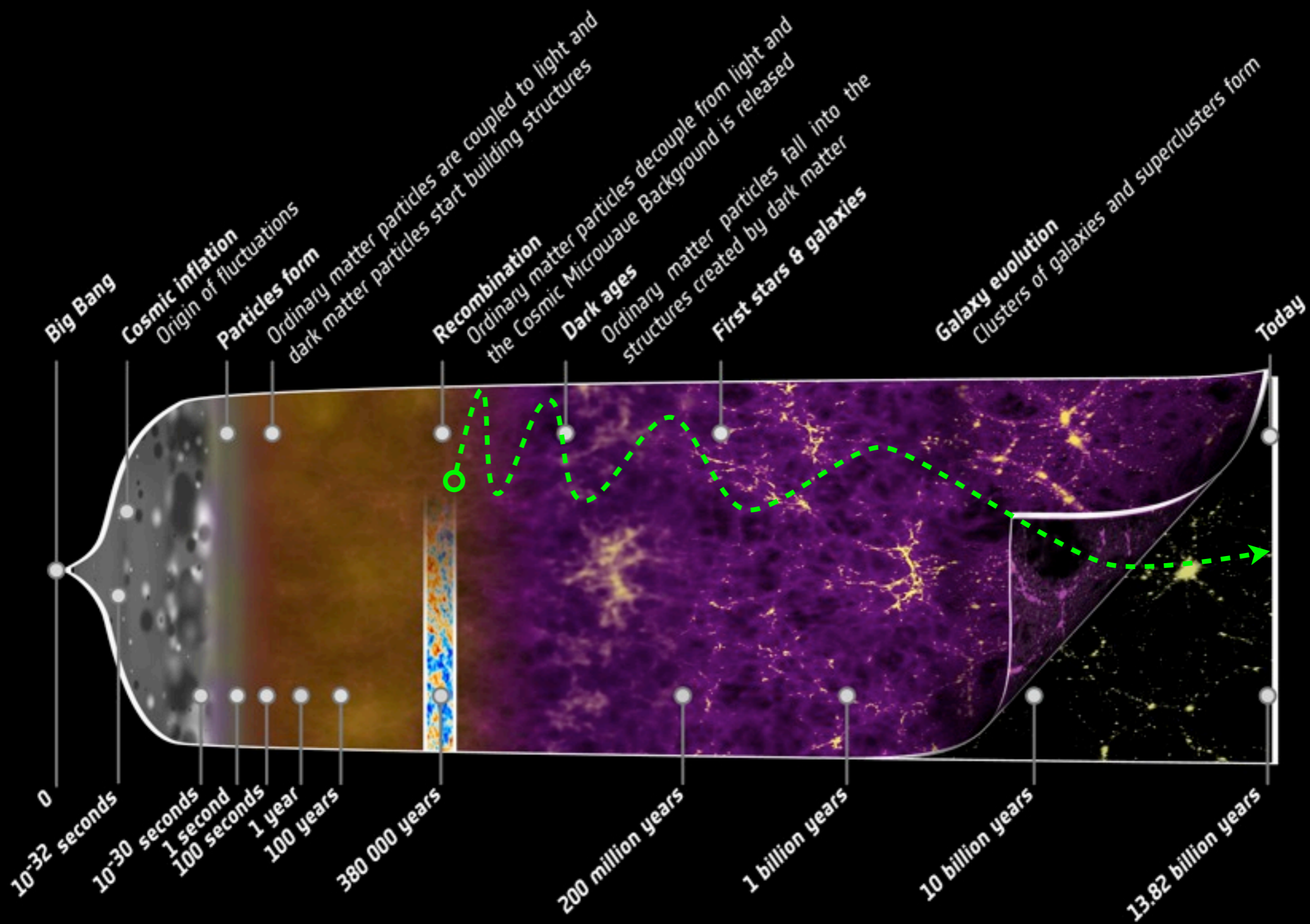
Spectator mechanism and the CMB modulation

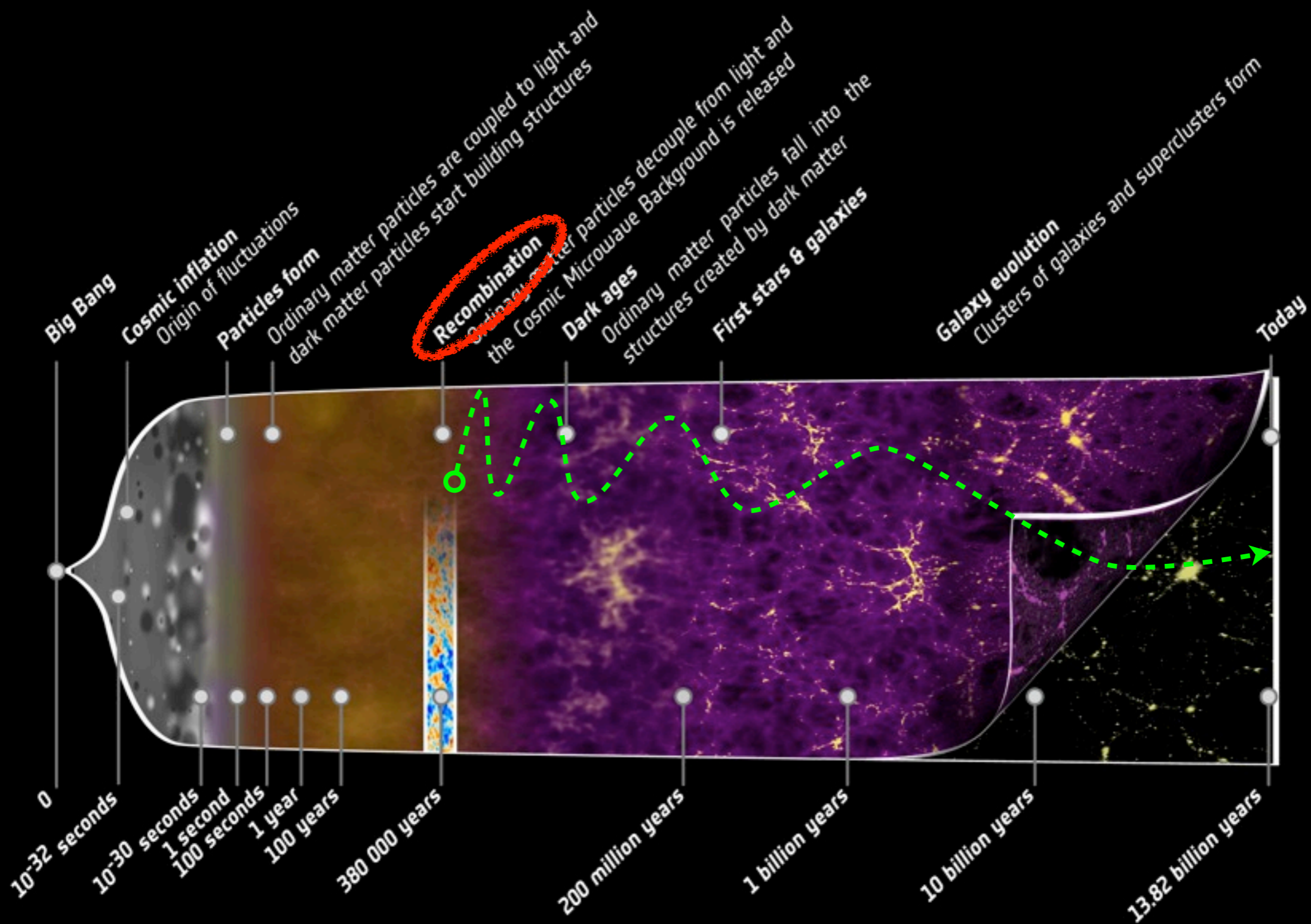
Lingfei Wang
Lancaster University

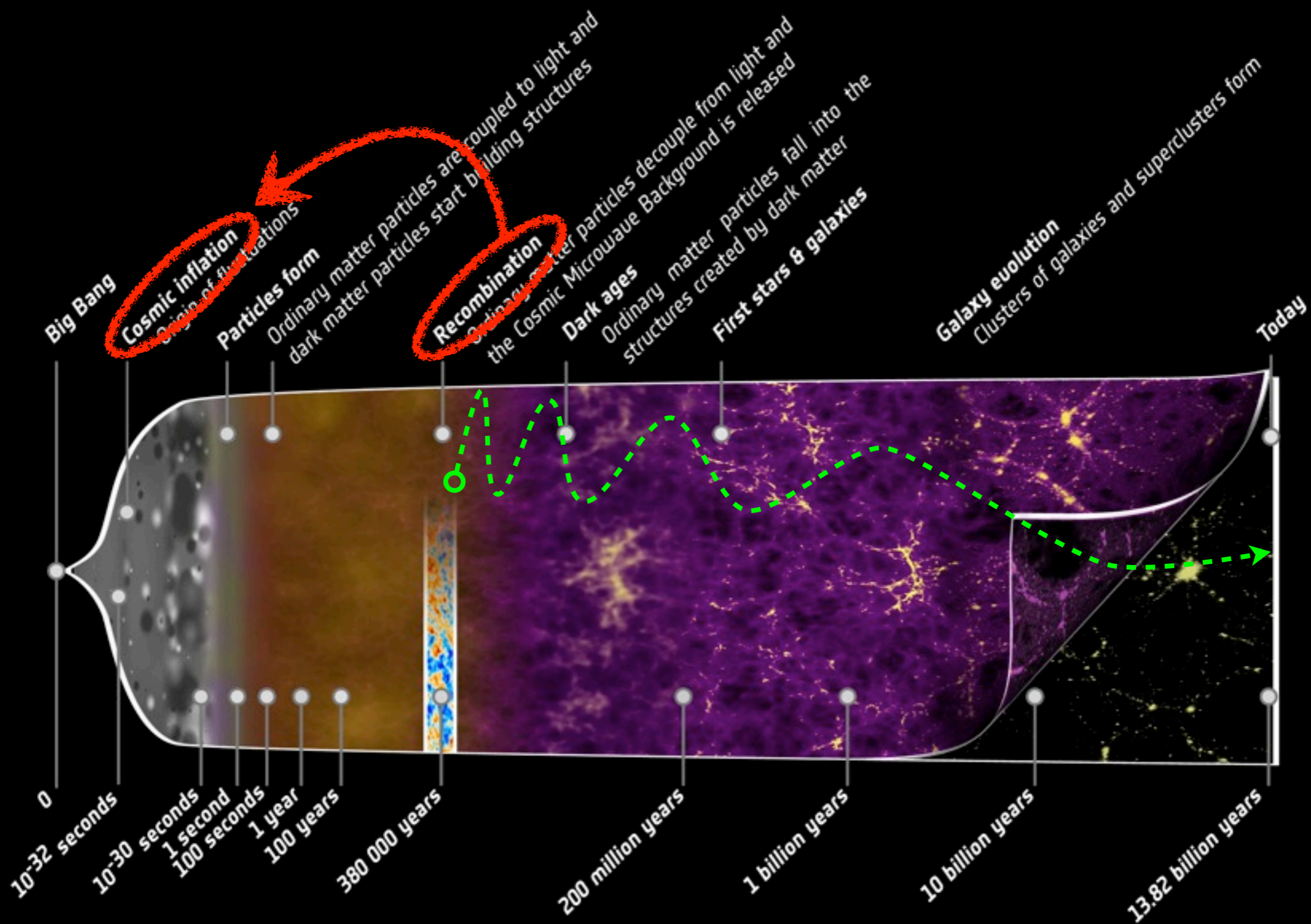
Based on [1306.5736], PRD 88 023512,
JCAP 1307 019, JCAP 1305 012, PRD 87 083501

21 October, 2013

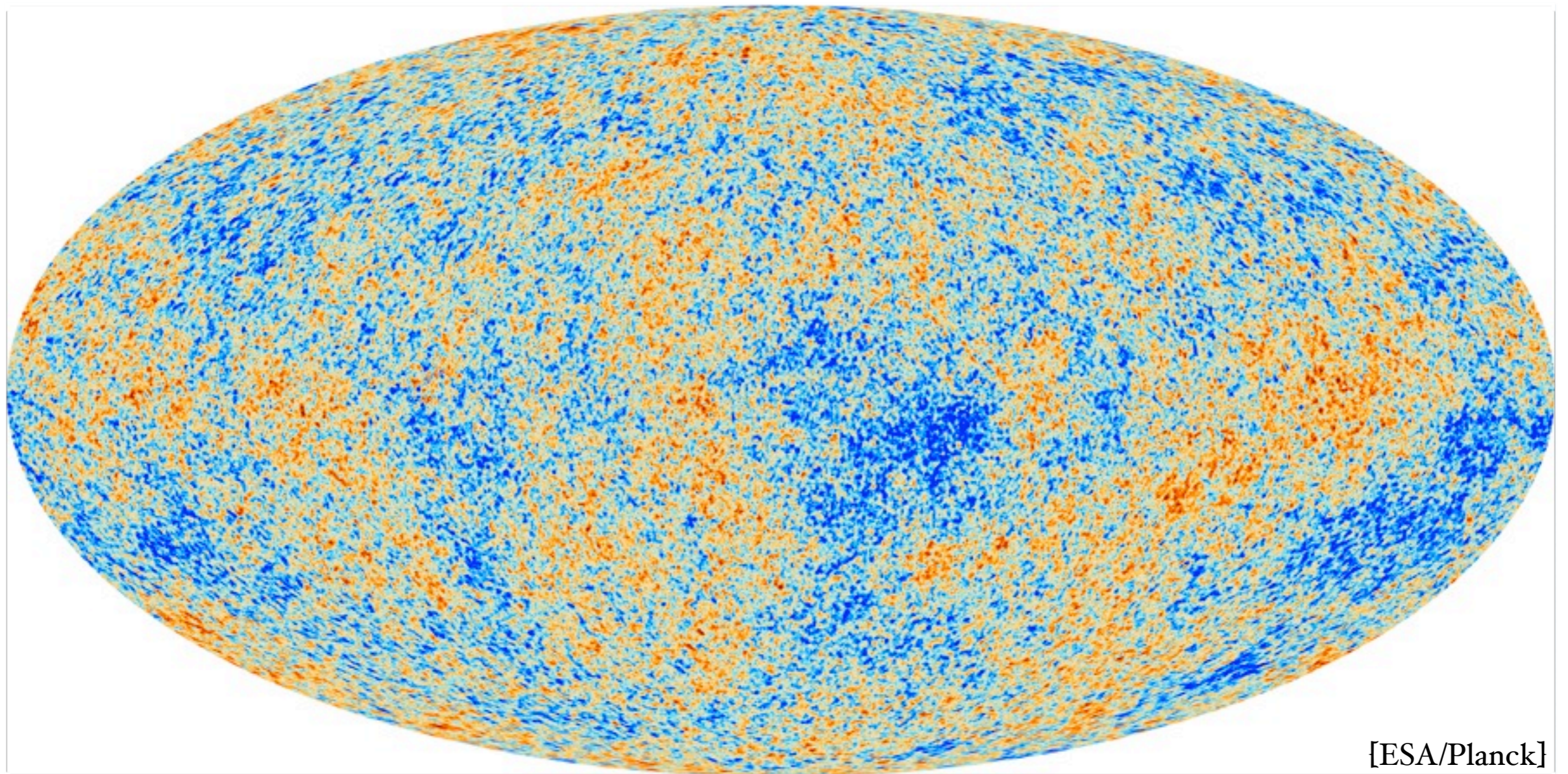




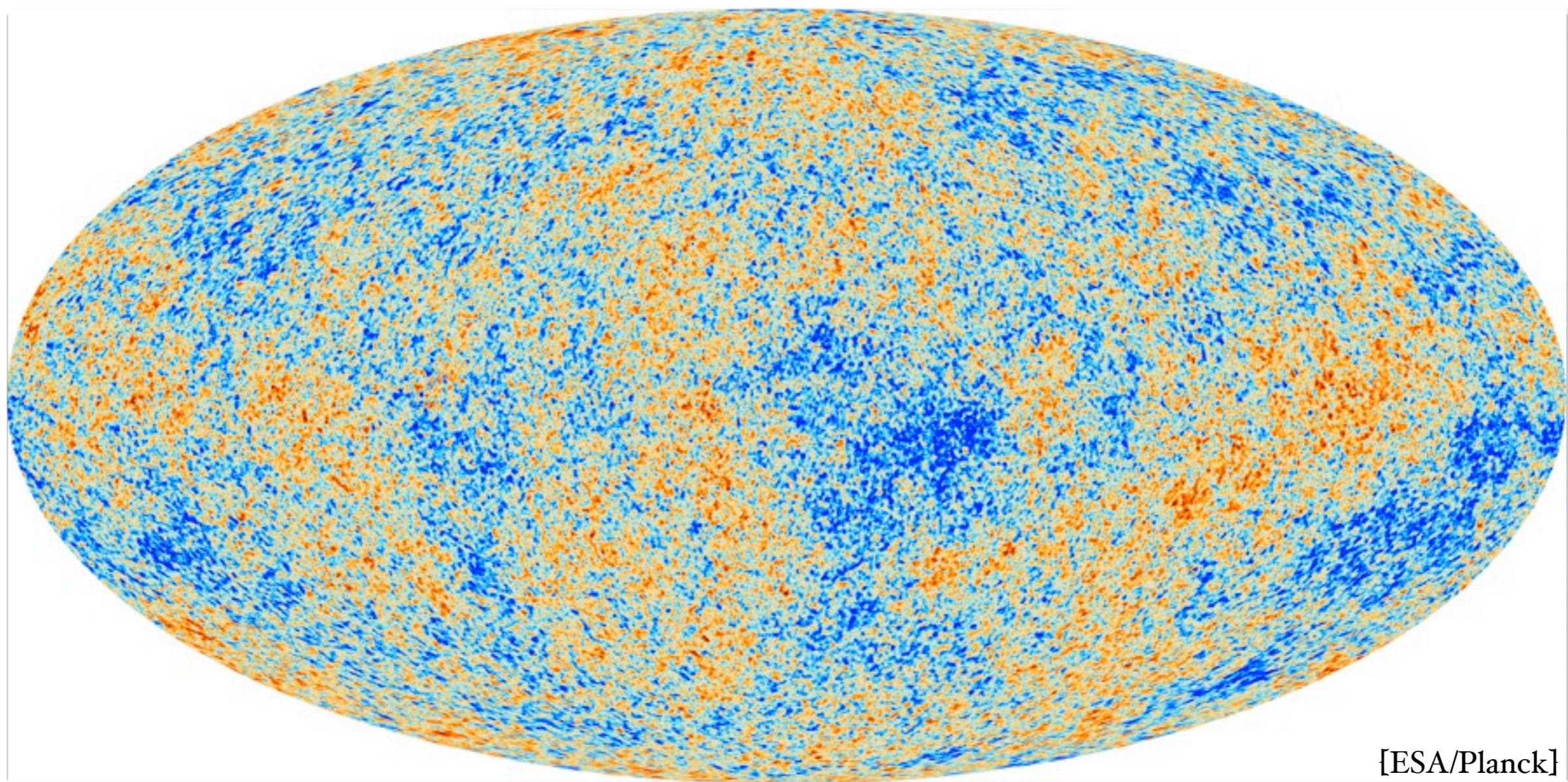




CMB anisotropy



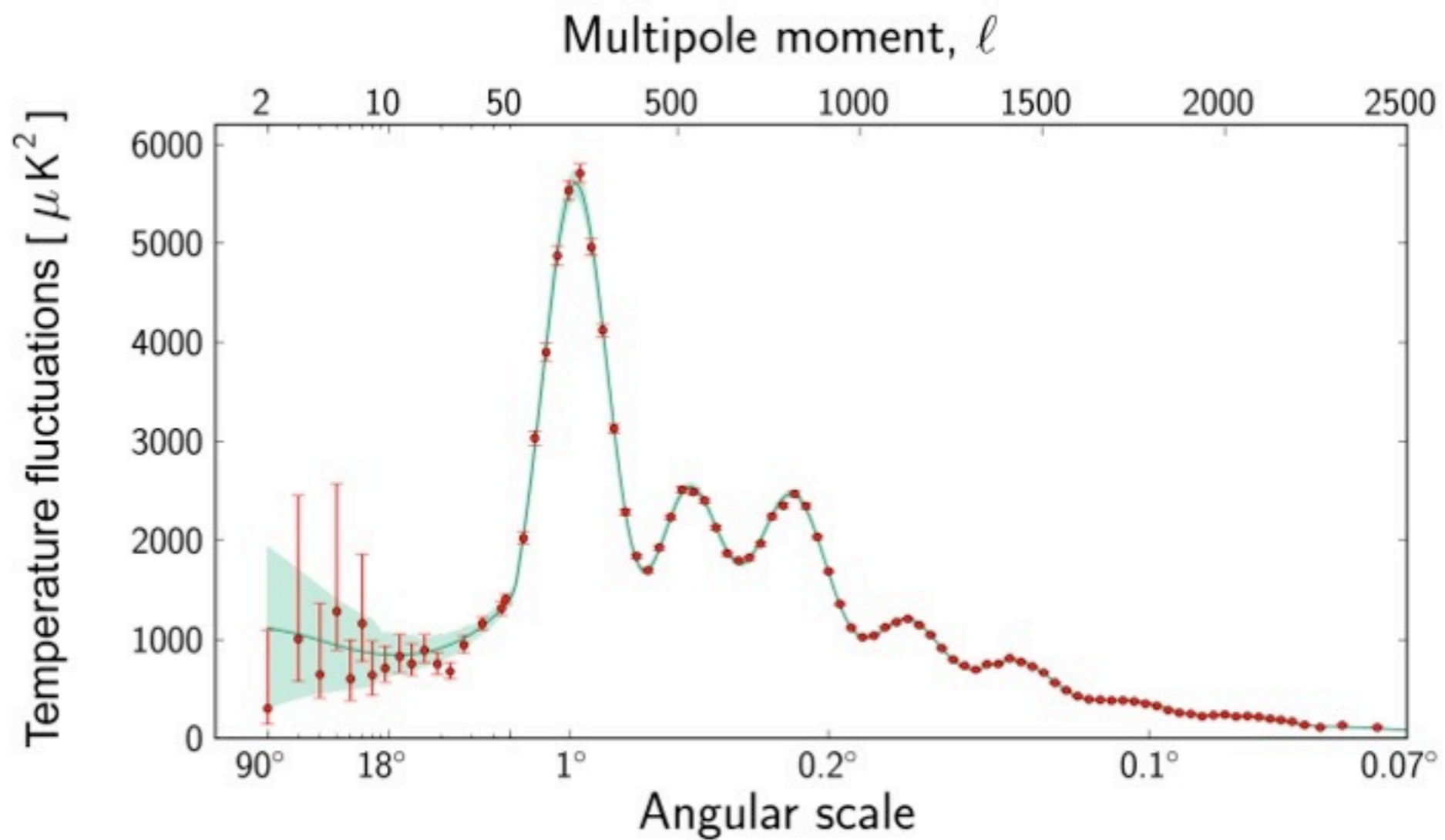
[ESA/Planck]



$$\Delta T(\hat{\mathbf{n}}) = \sum_{lm} a_{lm} Y_{lm}(\hat{\mathbf{n}})$$

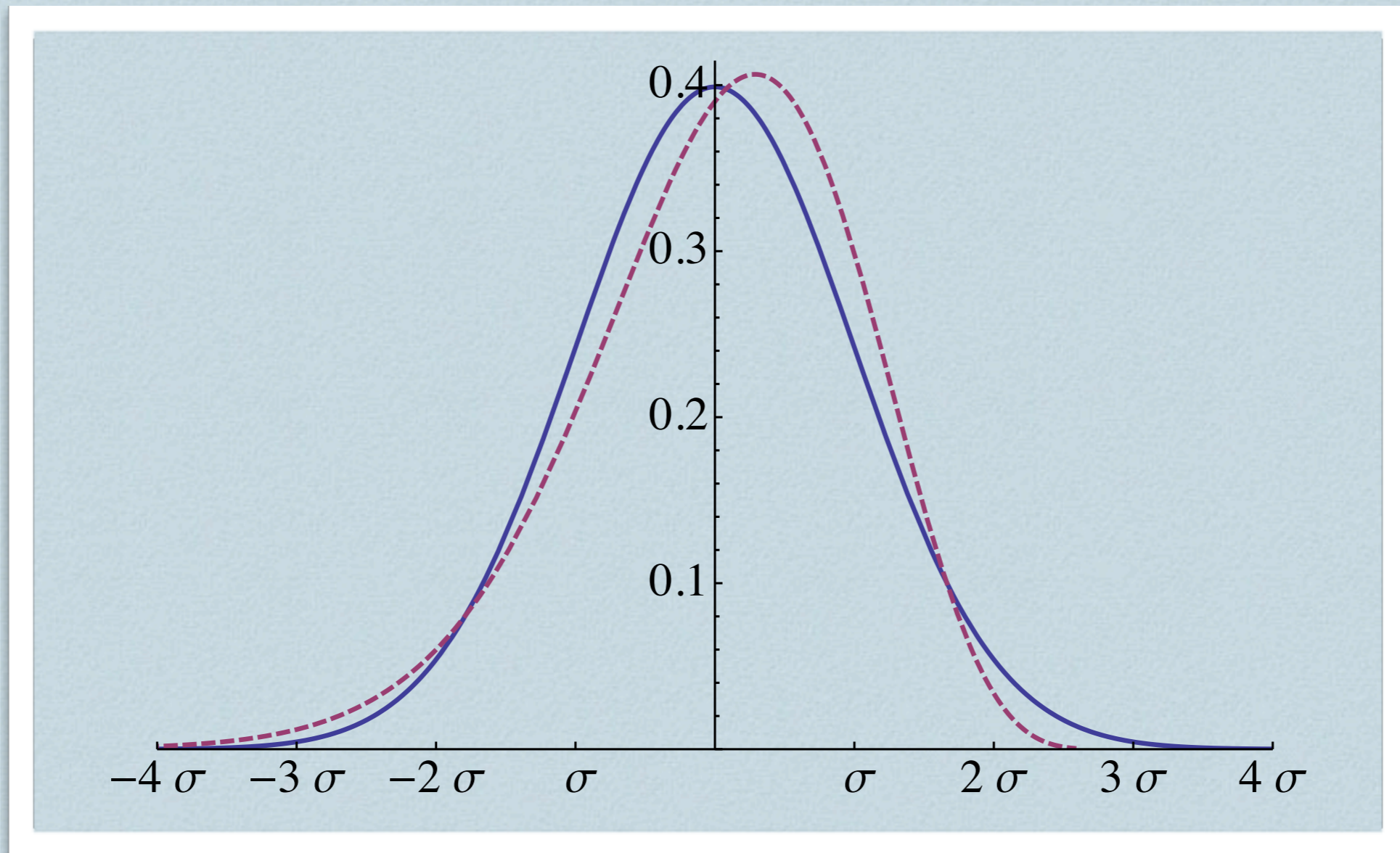
$$\langle a_{lm}^* a_{l'm'} \rangle = C_l \delta_{ll'} \delta_{mm'}$$

CMB anisotropy



[ESA/Planck]

CMB non-Gaussianity



CMB non-Gaussianity

- ❖ Temperature fluctuations

$$\Delta T(\hat{\mathbf{n}}) = \sum_{lm} a_{lm} Y_{lm}(\hat{\mathbf{n}})$$

- ❖ Angular bispectrum

$$\langle a_{l_1 m_1} a_{l_2 m_2} a_{l_3 m_3} \rangle = \begin{pmatrix} l_1 & l_2 & l_3 \\ m_1 & m_2 & m_3 \end{pmatrix} B_{l_1 l_2 l_3}$$

- ❖ Post-inflation: ISW effect, etc

- ❖ Inflation: primordial bispectrum (e.g. local f_{NL})

$$\langle \Phi(\mathbf{k}_1) \Phi(\mathbf{k}_2) \Phi(\mathbf{k}_3) \rangle = (2\pi)^3 \delta^3(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) B(k_1, k_2, k_3)$$

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- ❖ Trispectrum τ_{NL}

$$\langle a_{l_1 m_1} a_{l_2 m_2} a_{l_3 m_3} a_{l_4 m_4} \rangle, \dots$$

CMB non-Gaussianity

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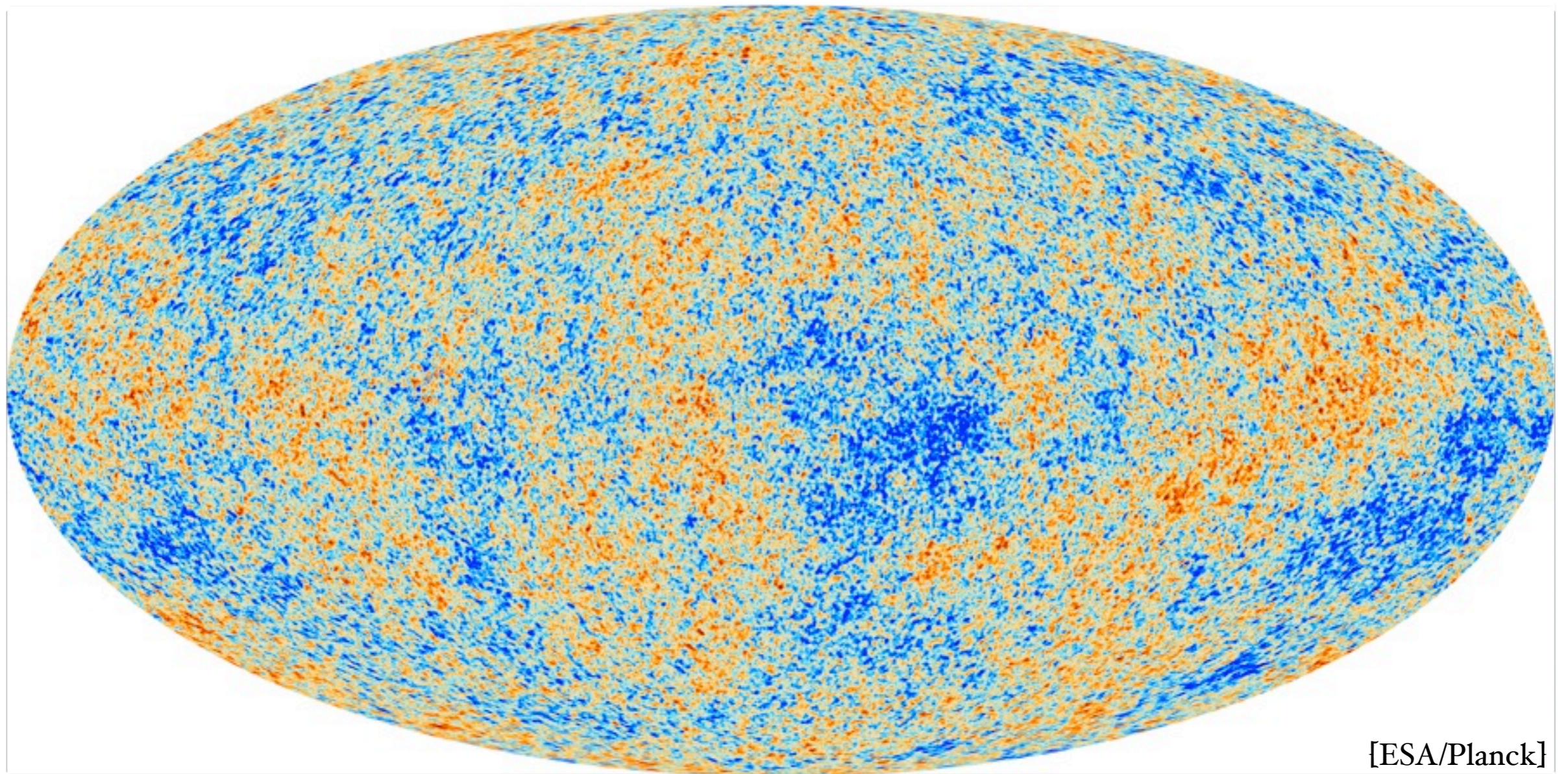
- ❖ Inflation: primordial bispectrum (e.g. local $f_{\text{NL}} = 2.7 \pm 5.8$)

$$\langle \Phi(\mathbf{k}_1) \Phi(\mathbf{k}_2) \Phi(\mathbf{k}_3) \rangle = (2\pi)^3 \delta^3(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) B(k_1, k_2, k_3)$$

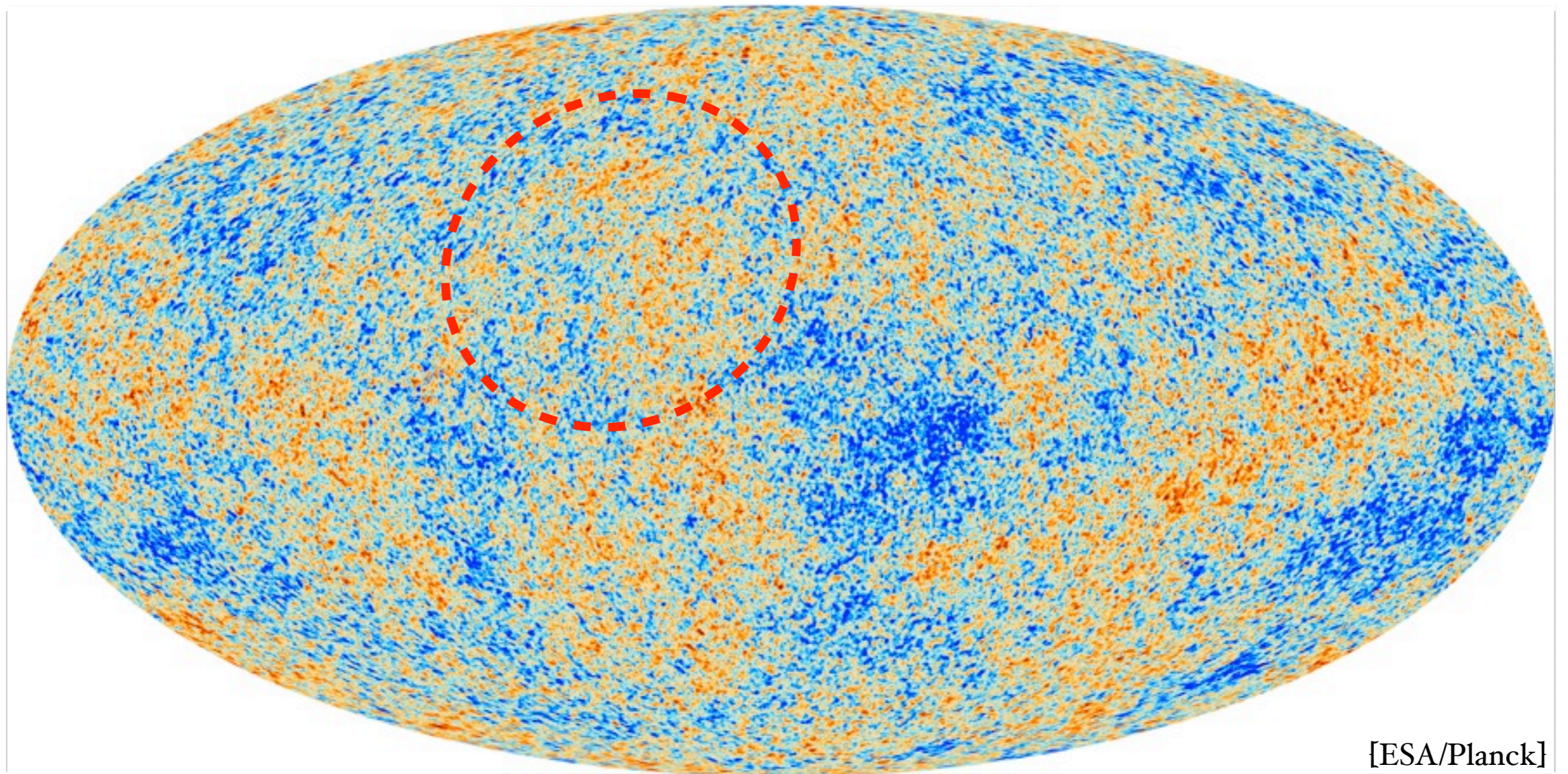
- ❖ Trispectrum $\tau_{\text{NL}} < 2800$

$$\langle a_{l_1 m_1} a_{l_2 m_2} a_{l_3 m_3} a_{l_4 m_4} \rangle, \dots$$

CMB dipole asymmetry

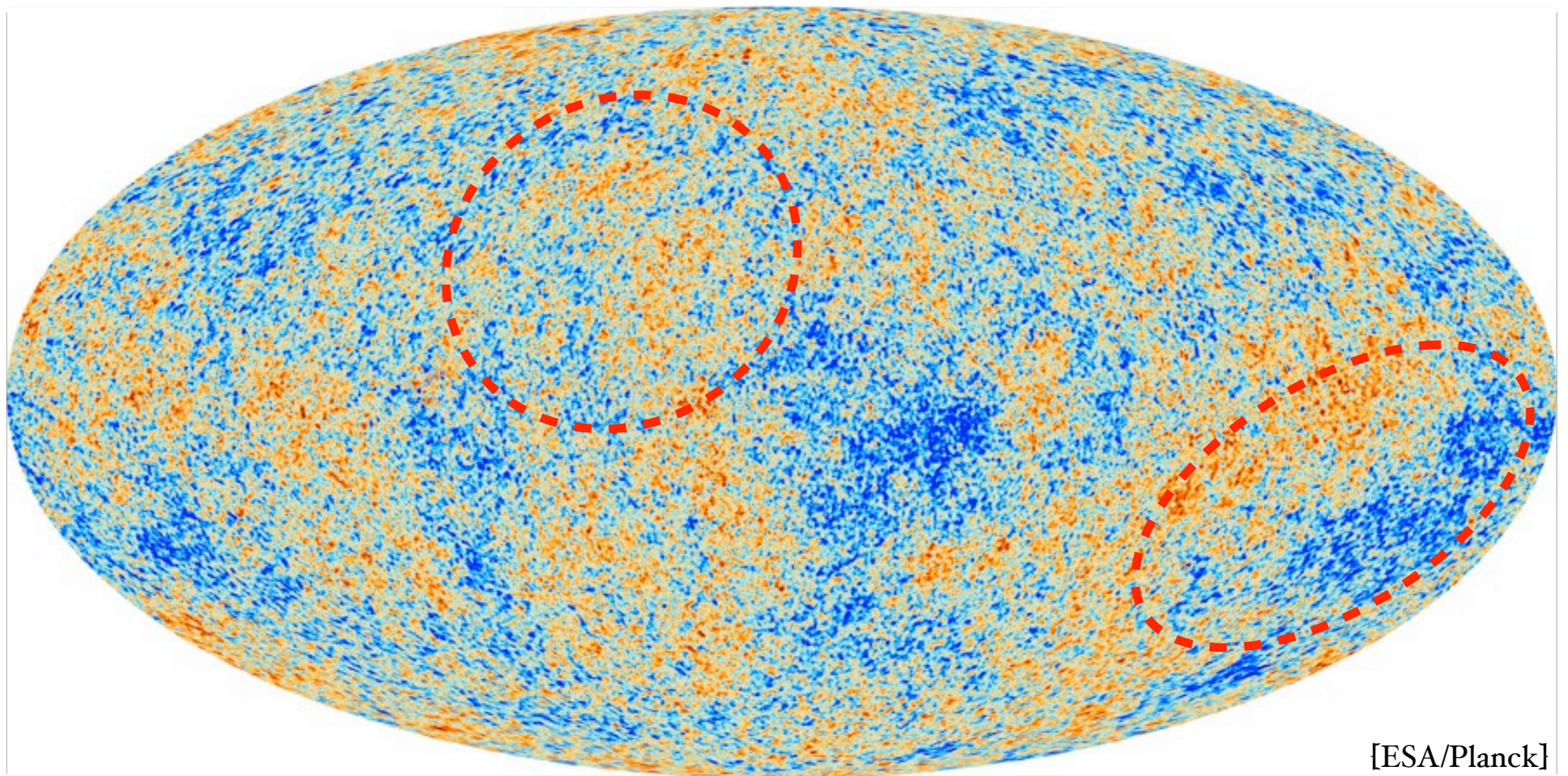


CMB dipole asymmetry



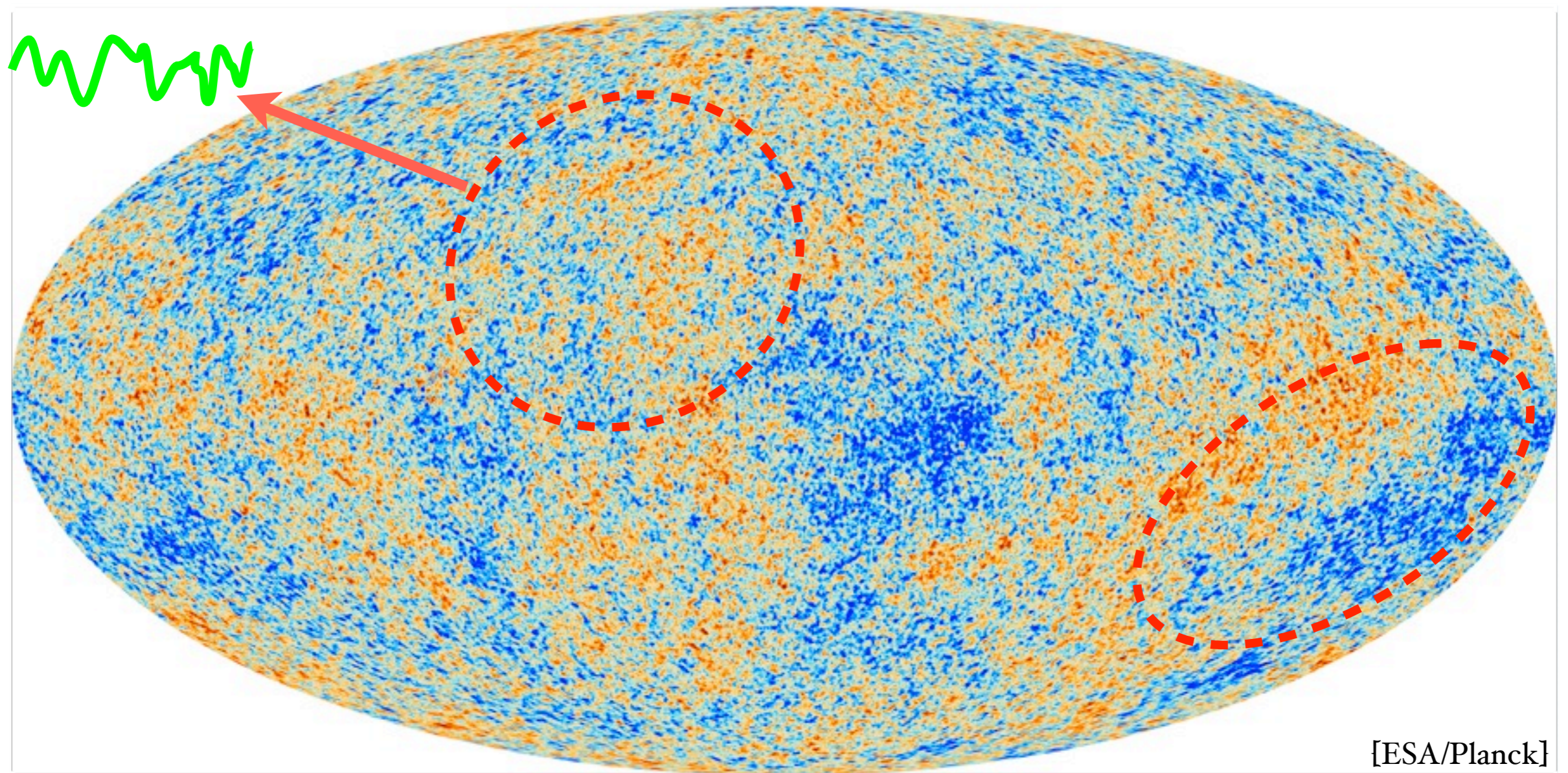
[ESA/Planck]

CMB dipole asymmetry

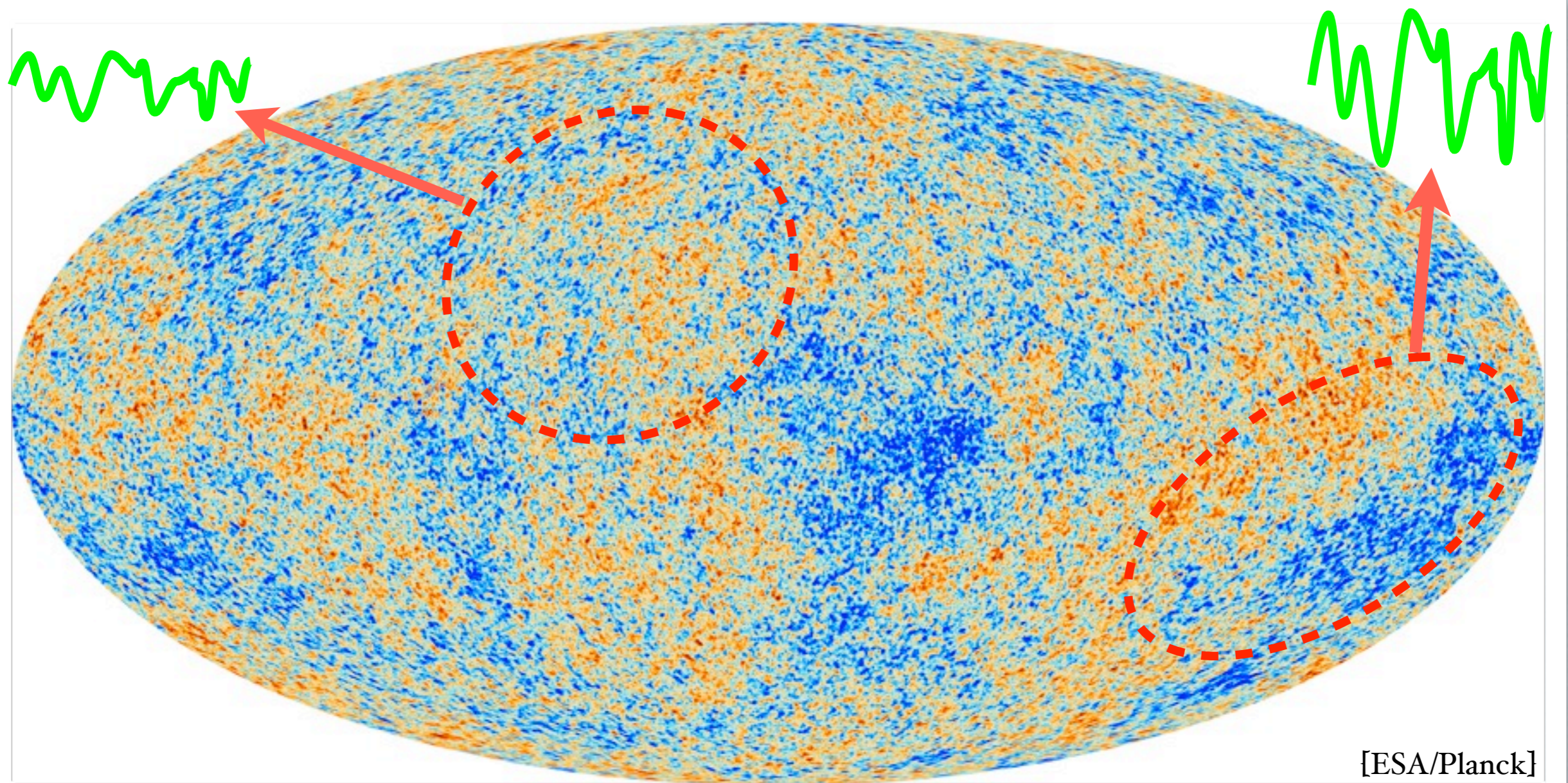


[ESA/Planck]

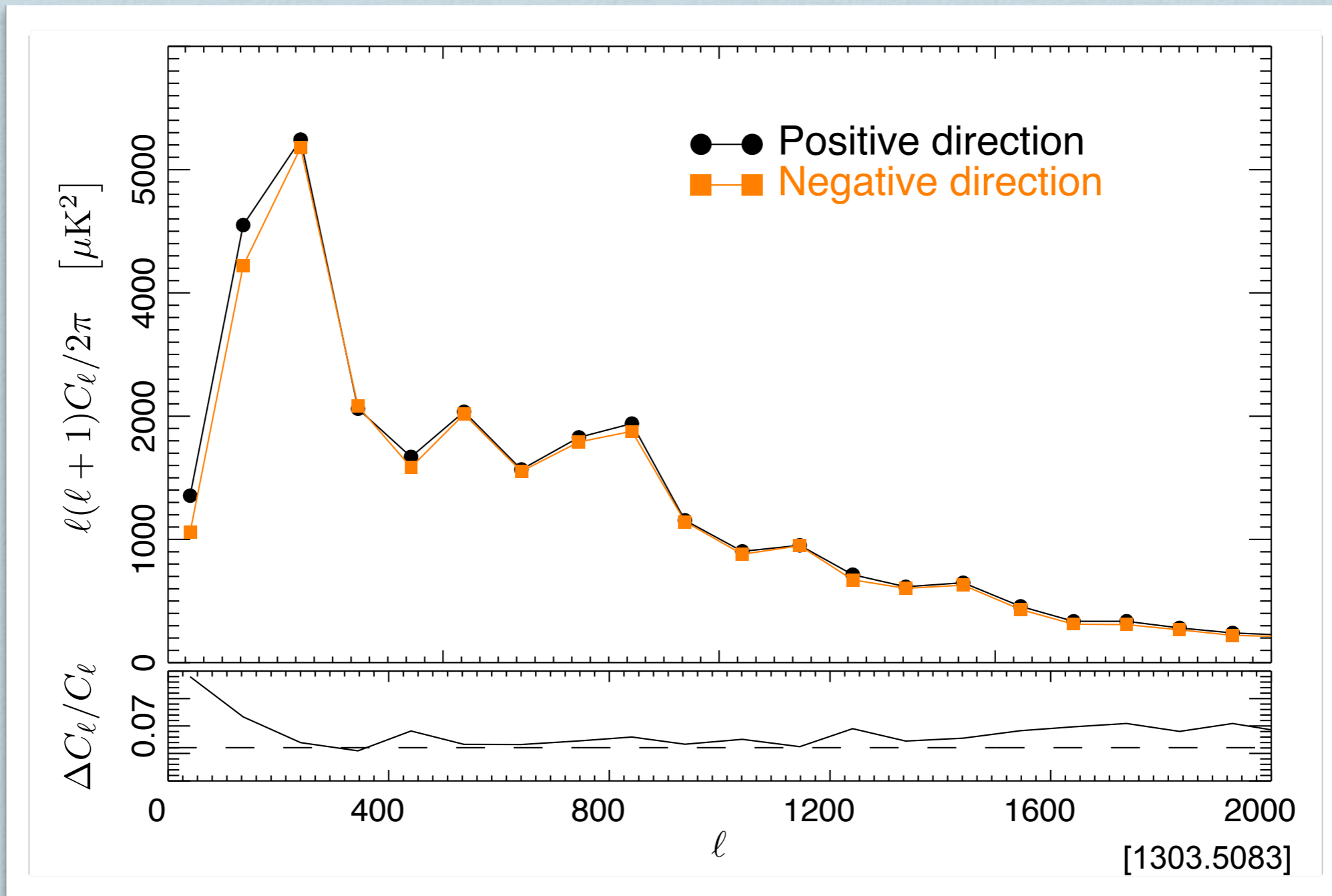
CMB dipole asymmetry



CMB dipole asymmetry



CMB dipole asymmetry



Isocurvature perturbations

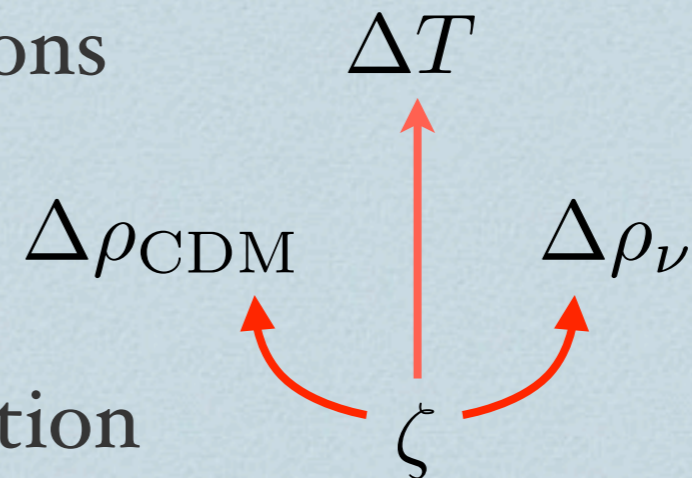
- ❖ CMB temperature perturbations ΔT
- ❖ Other perturbations $\Delta\rho_{\text{CDM}}$ $\Delta\rho_\nu$

Isocurvature perturbations

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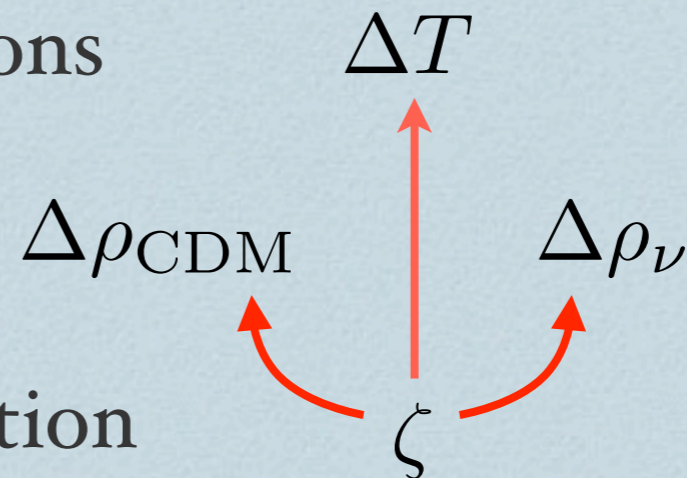
Isocurvature perturbations

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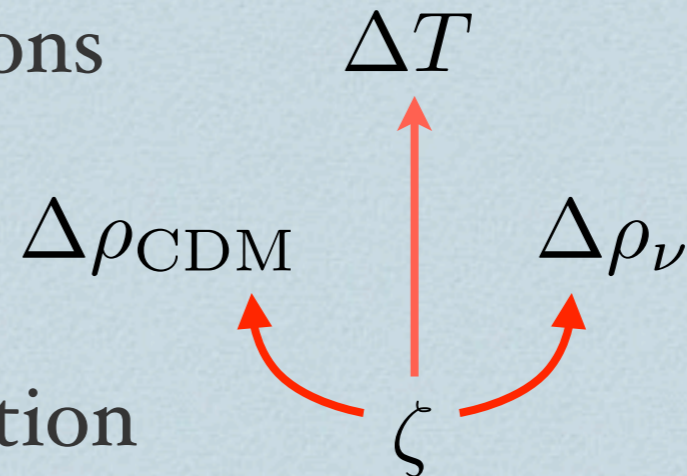
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- ❖ Adiabatic: curvature perturbation
- ❖ Isocurvature: more than one degree of freedom during inflation



Isocurvature perturbations

- ❖ CMB temperature perturbations
- ❖ Other perturbations
- ❖ Adiabatic: curvature perturbation
- ❖ Isocurvature: more than one degree of freedom during inflation
- ❖ Constrain multi-field inflation



Inflation checklist

❖ CMB power spectrum

$$P_{\zeta} = 2.196 \times 10^{-9}$$

❖ Spectral index

$$n_s = 0.9603 \pm 0.0073$$

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Standard Model Lagrangian Density

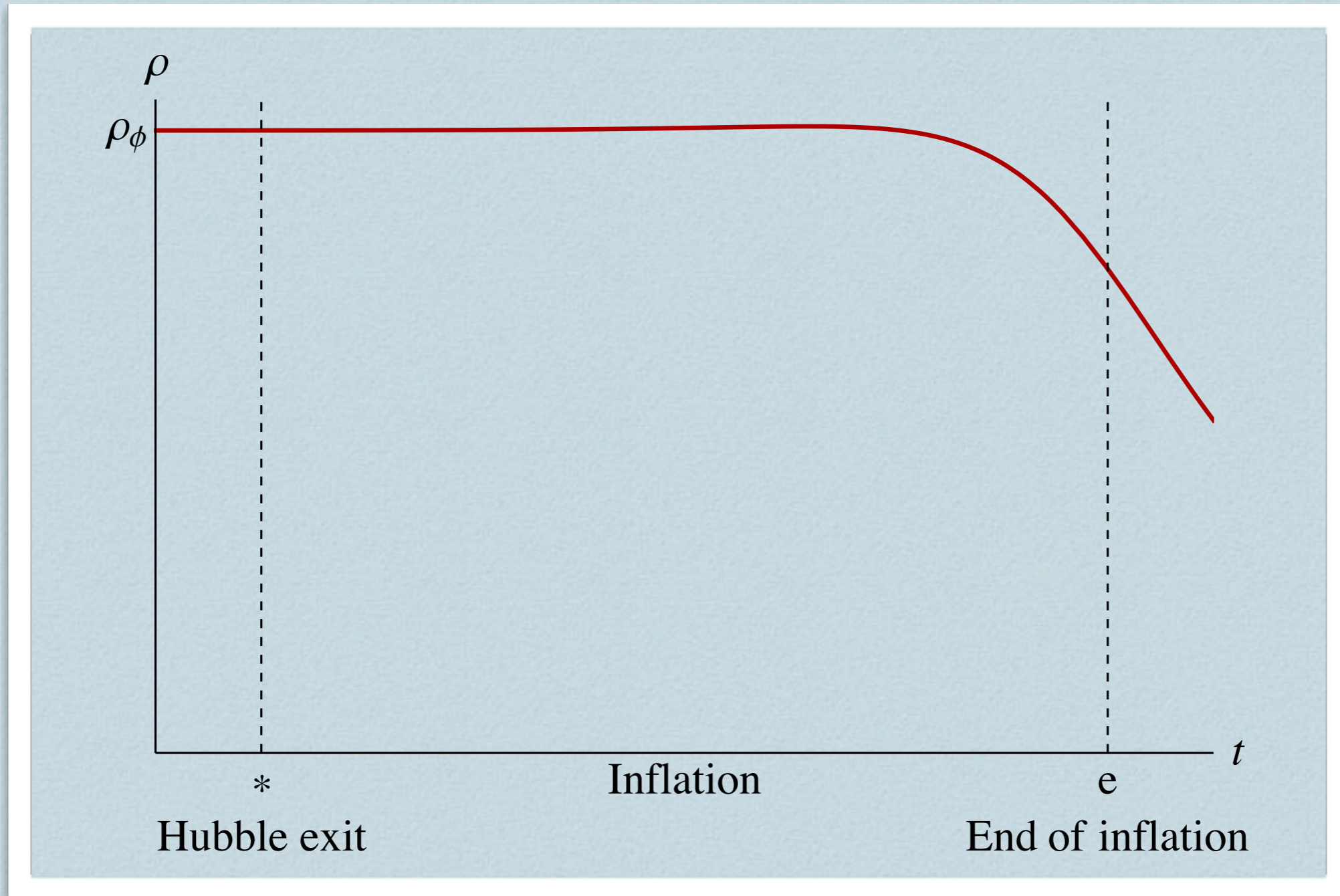
$$\begin{aligned}
& -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e + \\
& \frac{1}{2}ig_s^2 (\bar{q}_i^\sigma \gamma^\mu q_j^\sigma) g_\mu^a + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
& M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2}\partial_\mu H \partial_\mu H - \\
& \frac{1}{2}m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w^2} M \phi^0 \phi^0 - \beta_h \left[\frac{2M^2}{g^2} + \right. \\
& \left. \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right] + \frac{2M^4}{g^2} \alpha_h - igc_w [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - \\
& W_\nu^+ W_\mu^-) - Z_\nu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - \\
& W_\nu^- \partial_\nu W_\mu^+)] - igs_w [\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - \\
& W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)] - \frac{1}{2}g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \\
& \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^- W_\nu^+ + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\nu^0 W_\mu^+ W_\nu^-) + \\
& g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\nu W_\mu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - \\
& W_\nu^+ W_\mu^-) - 2A_\mu Z_\mu^0 W_\nu^+ W_\nu^-] - g\alpha [H^3 + H\phi^0 \phi^0 + 2H\phi^+ \phi^-] - \\
& \frac{1}{8}g^2 \alpha_h [H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2] - \\
& gMW_\mu^+ W_\mu^- H - \frac{1}{2}g\frac{M}{c_w^2} Z_\mu^0 Z_\mu^0 H - \frac{1}{2}ig[W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - \\
& W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)] + \frac{1}{2}g[W_\mu^+ (H\partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\mu^- (H\partial_\mu \phi^+ - \\
& \phi^+ \partial_\mu H)] + \frac{1}{2}g\frac{1}{c_w} (Z_\mu^0 (H\partial_\mu \phi^0 - \phi^0 \partial_\mu H) - ig\frac{s_w^2}{c_w} MZ_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \\
& igs_w MA_\mu (W_\mu^+ \phi^- - W_\mu^- \phi^+) - ig\frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + \\
& igs_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4}g^2 W_\mu^+ W_\mu^- [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \\
& \frac{1}{4}g^2 \frac{1}{c_w^2} Z_\mu^0 Z_\mu^0 [H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + \\
& W_\mu^- \phi^+) - \frac{1}{2}ig^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\
& W_\mu^- \phi^+) + \frac{1}{2}ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\
& g^1 s_w^2 A_\mu A_\mu \phi^+ \phi^- - \bar{e}^\lambda (\gamma^\partial + m_e^\lambda) e^\lambda - \bar{\nu}^\lambda \gamma^\partial \nu^\lambda - \bar{u}_j^\lambda (\gamma^\partial + m_u^\lambda) u_j^\lambda - \bar{d}_j^\lambda (\gamma^\partial + \\
& m_d^\lambda) d_j^\lambda + igs_w A_\mu [-(\bar{e}^\lambda \gamma e^\lambda) + \frac{2}{3}(\bar{u}_j^\lambda \gamma u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma d_j^\lambda)] + \frac{ig}{4c_w} Z_\mu^0 [(\bar{\nu}^\lambda \gamma^\mu (1 + \\
& \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - 1 - \gamma^5) u_j^\lambda) + \\
& (\bar{d}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 - \gamma^5) d_j^\lambda)] + \frac{ig}{2\sqrt{2}} W_\mu^+ [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (1 + \\
& \gamma^5) C_{\lambda\kappa} d_j^\kappa)] + \frac{ig}{2\sqrt{2}} W_\mu^- [(\bar{e}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\lambda\kappa}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda)] + \\
& \frac{ig}{2\sqrt{2}} \frac{m_e^\lambda}{M} [-\phi^+ (\bar{\nu}^\lambda (1 - \gamma^5) e^\lambda) + \phi^- (\bar{e}^\lambda (1 + \gamma^5) \nu^\lambda)] - \frac{g}{2} \frac{m_e^\lambda}{M} [H(\bar{e}^\lambda e^\lambda) + \\
& i\phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda)] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa) + m_u^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \\
& \gamma^5) d_j^\kappa) + \frac{ig}{2M\sqrt{2}} \phi^- [m_d^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_u^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \gamma^5) u_j^\kappa) - \\
& \frac{g}{2} \frac{m_u^\lambda}{M} H(\bar{u}_j^\lambda u_j^\lambda) - \frac{g}{2} \frac{m_d^\lambda}{M} H(\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_d^\lambda}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{ig}{2} \frac{m_d^\lambda}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \\
& \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - \frac{M^2}{c_w^2}) X^0 + \bar{Y} \partial^2 Y + \\
& igc_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + igs_w W_\mu^+ (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ Y) + \\
& igc_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \partial_\mu \bar{X}^0 X^+) + igs_w W_\mu^- (\partial_\mu \bar{X}^- Y - \partial_\mu \bar{Y} X^+) + \\
& igc_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^+ - \partial_\mu \bar{X}^- X^-) + igs_w A_\mu (\partial_\mu \bar{X}^+ X^+ - \partial_\mu \bar{X}^- X^-) - \\
& \frac{1}{2}gM[\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w^2} \bar{X}^0 X^0 H] + \frac{1-2c_w^2}{2c_w} igM[\bar{X}^+ X^0 \phi^+ - \\
& \bar{X}^- X^0 \phi^-] + \frac{1}{2c_w} igM[\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + igMs_w[\bar{X}^0 X^- \phi^+ - \\
& \bar{X}^0 X^+ \phi^-] + \frac{1}{2}igM[\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0]
\end{aligned}$$

Standard Model Lagrangian Density

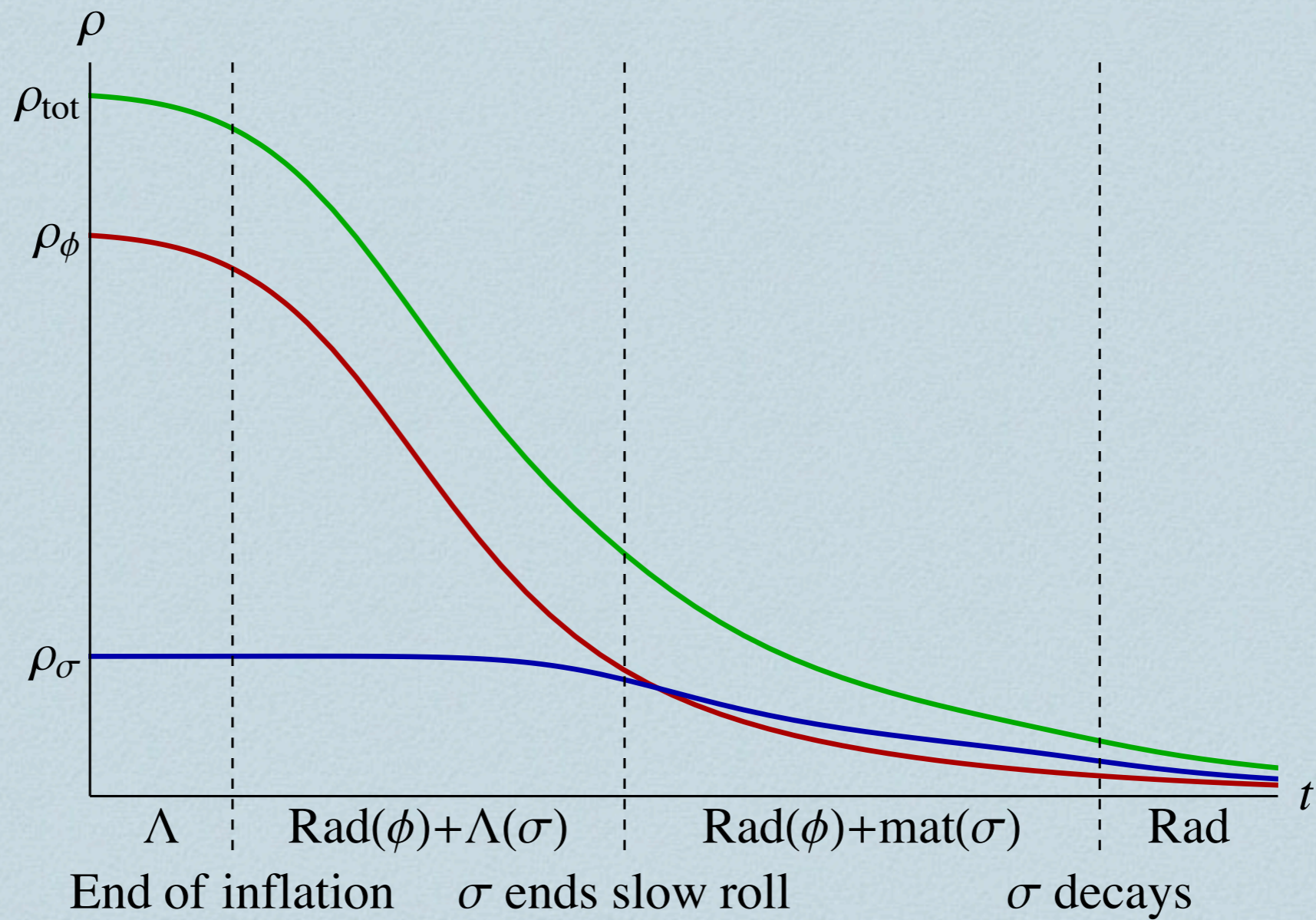
$$\begin{aligned}
 & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e + \\
 & \frac{1}{2}ig_s^2 (\bar{q}_i^\sigma \gamma^\mu q_j^\sigma) g_\mu^a + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
 & M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2}\partial_\mu H \partial_\mu H - \\
 & \frac{1}{2}m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w^2} M \phi^0 \phi^0 - \beta_h \left[\frac{2M^2}{g^2} + \right. \\
 & \left. \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right] + \frac{2M^4}{g^2} \alpha_h - igc_w [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - \\
 & W_\nu^+ W_\mu^-) - Z_\nu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - \\
 & W_\nu^- \partial_\nu W_\mu^+)] - igs_w [\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - \\
 & W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)] - \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^- W_\nu^+ + \\
 & \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^- W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\nu^0 W_\mu^+ Z_\mu^0 W_\nu^-) + \\
 & g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\nu W_\mu^+ W_\nu^-) - g^2 c_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - \\
 & W_\nu^+ W_\mu^-) - 2A_\mu Z_\nu^0 W_\mu^+ W_\nu^-] + \frac{1}{2}M[H^3 + H\phi^0 \phi^0 + 2H\phi^+ \phi^-] - \\
 & \frac{1}{8}g^2 \alpha_h [H^4 + (\phi^0)^4 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^+)^2 + 2(\phi^-)^2] - \\
 & \frac{g^2}{2} W_\mu^+ W_\nu^- W_\mu^- W_\nu^+ - \frac{1}{2}g \frac{M}{c_w^2} Z_\mu^0 Z_\mu^0 H - \frac{1}{2}ig[W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) + \\
 & W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)] + \frac{1}{2}g[W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\mu^- (\phi^+ \partial_\mu H - \\
 & H \partial_\mu \phi^+)] + \frac{1}{2}g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - \frac{1}{c_w} (W_\mu^+ \phi^- - W_\mu^- \phi^+)) - \\
 & igs_w M A_\mu (W_\mu^+ \phi^- - W_\mu^- \phi^+) - ig \frac{1}{2c_w} (\phi^+ \phi^- - \phi^- \partial_\mu \phi^+ + \phi^+ \partial_\mu \phi^-) - \\
 & igs_w A_\mu (\phi^- \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^-) - \frac{1}{2}M^2 W_\mu^+ W_\mu^- [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \\
 & \frac{2}{c_w^2} M^2 (2c_w^2 \phi^+ \phi^- + (\phi^0)^2) - \frac{1}{2}M^2 Z_\mu^0 \phi^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \\
 & \frac{1}{2}g^2 s_w^2 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w^2 (W_\mu^- \phi^+ - W_\mu^+ \phi^-) - g^2 \frac{s_w}{c_w} (2c_w^2 Z_\mu^0 A_\mu \phi^+ \phi^- - \\
 & g^2 s_w^2 A_\mu \phi^+ \phi^-) + \frac{1}{2}g^2 s_w^2 (2c_w^2 Z_\mu^0 A_\mu \phi^+ \phi^- - g^2 s_w^2 A_\mu \phi^+ \phi^-) - \\
 & g^2 s_w^2 (A_\mu \phi^+ \phi^-) + \frac{1}{2}g^2 s_w^2 (2c_w^2 Z_\mu^0 A_\mu \phi^+ \phi^- - g^2 s_w^2 A_\mu \phi^+ \phi^-) - \\
 & m_d^\lambda (\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) + (\bar{d}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda) + \frac{ig}{\sqrt{2}} Z_\mu^0 (\bar{u}_j^\lambda \gamma^\mu u_j^\lambda - \\
 & \bar{d}_j^\lambda \gamma^\mu d_j^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (1 - \gamma^5) \nu_j^\lambda) + \\
 & (\bar{d}_j^\lambda \gamma^\mu (-\frac{8}{3}s_w^2 - \gamma^5) d_j^\lambda) + \frac{ig}{2\sqrt{2}} W_\mu^+ [(\bar{e}^\lambda \gamma^\mu \nu^\lambda) + (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda)] + \\
 & \frac{ig}{2\sqrt{2}} \frac{m_\lambda^2}{M} [-\phi^+ (\bar{e}^\lambda \gamma^\mu \nu^\lambda) + \phi^- (\bar{e}^\lambda (1 + \gamma^5) \nu^\lambda)] - \frac{g m_\lambda^2}{2} [H(\bar{e}^\lambda e^\lambda) + \\
 & \frac{ig}{2M\sqrt{2}} W_\mu^+ \phi^+ [-m_d^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\lambda) + m_u^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \\
 & \gamma^5) d_j^\lambda)] + \frac{ig}{2M\sqrt{2}} \phi^- [m_d^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\lambda) - m_u^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \gamma^5) u_j^\lambda) - \\
 & \frac{g m_\lambda^2}{2} H(\bar{u}_j^\lambda u_j^\lambda) - \frac{g m_\lambda^2}{2} H(\bar{d}_j^\lambda d_j^\lambda) + \frac{ig m_\lambda^2}{2} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{ig m_\lambda^2}{2} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \\
 & \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - \frac{M^2}{c_w^2}) X^0 + \bar{Y} \partial^2 Y + \\
 & igc_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + igs_w W_\mu^+ (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ Y) + \\
 & igc_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \partial_\mu \bar{X}^0 X^+) + igs_w W_\mu^- (\partial_\mu \bar{X}^- Y - \partial_\mu \bar{Y} X^+) + \\
 & igc_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^+ - \partial_\mu \bar{X}^- X^-) + igs_w A_\mu (\partial_\mu \bar{X}^+ X^+ - \partial_\mu \bar{X}^- X^-) - \\
 & \frac{1}{2}gM[\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w^2} \bar{X}^0 X^0 H] + \frac{1-2c_w^2}{2c_w} igM[\bar{X}^+ X^0 \phi^+ - \\
 & \bar{X}^- X^0 \phi^-] + \frac{1}{2c_w} igM[\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + igMs_w[\bar{X}^0 X^- \phi^+ - \\
 & \bar{X}^0 X^+ \phi^-] + \frac{1}{2}igM[\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0]
 \end{aligned}$$



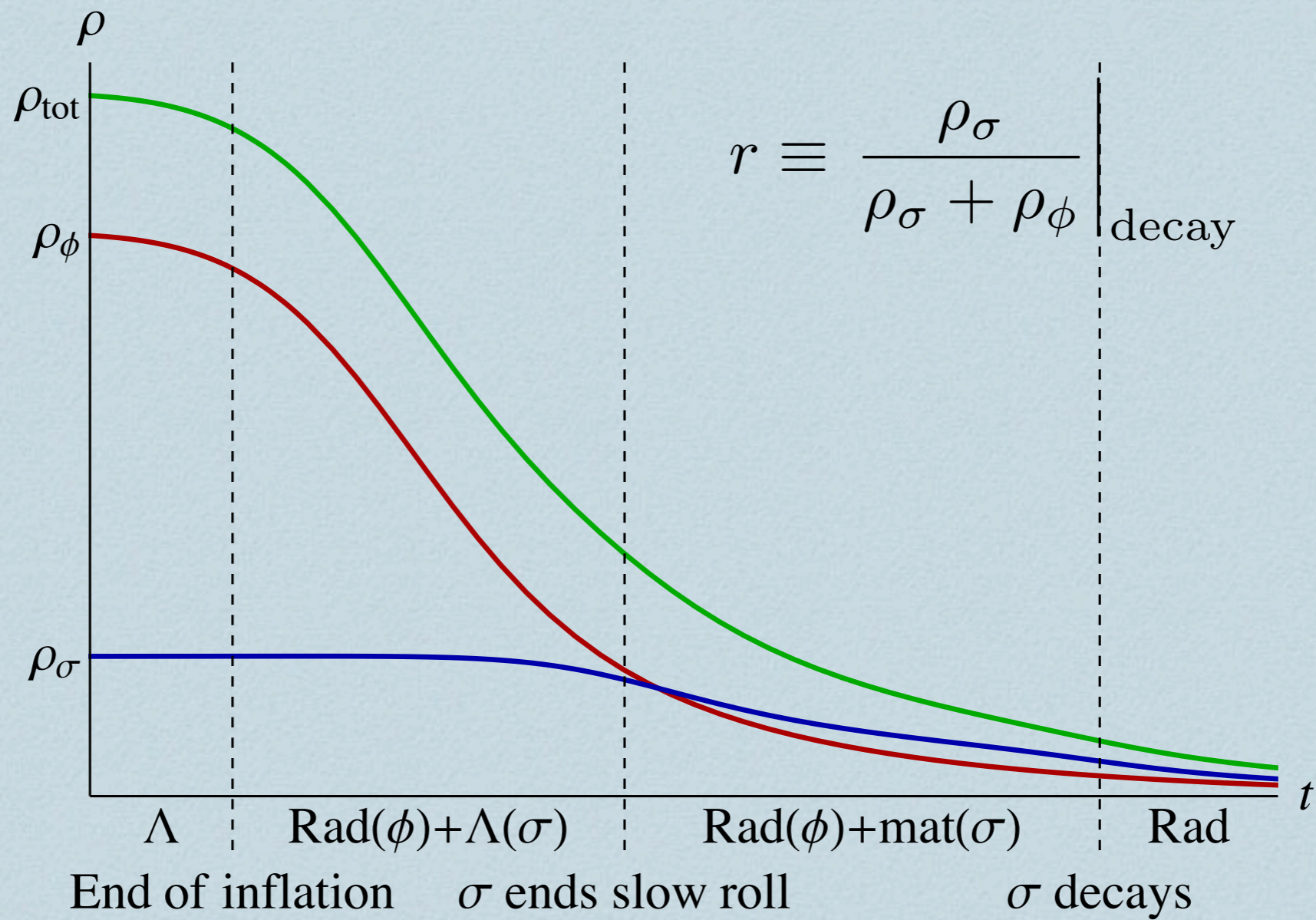
Single-field slow roll inflation



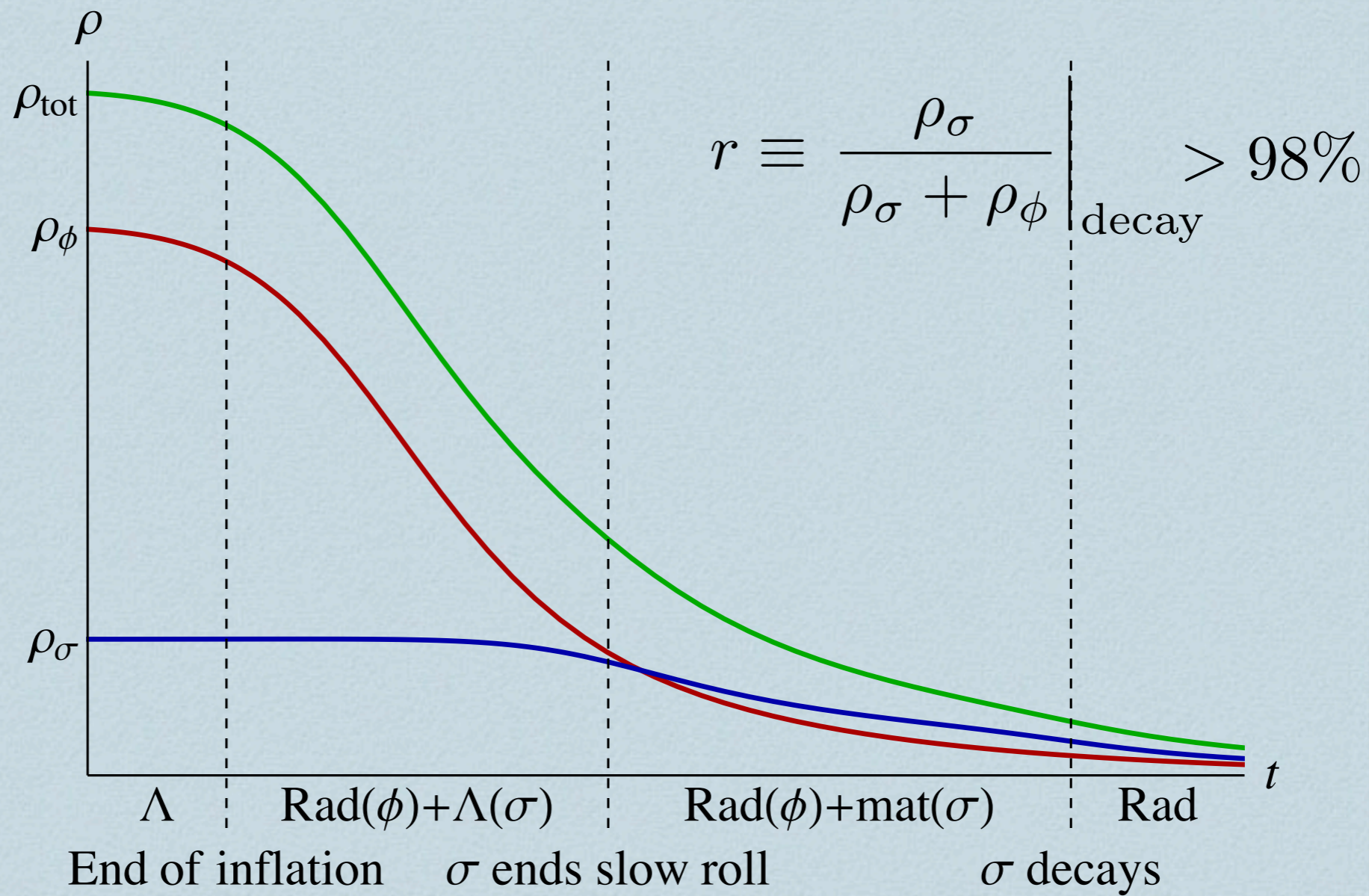
Curvaton



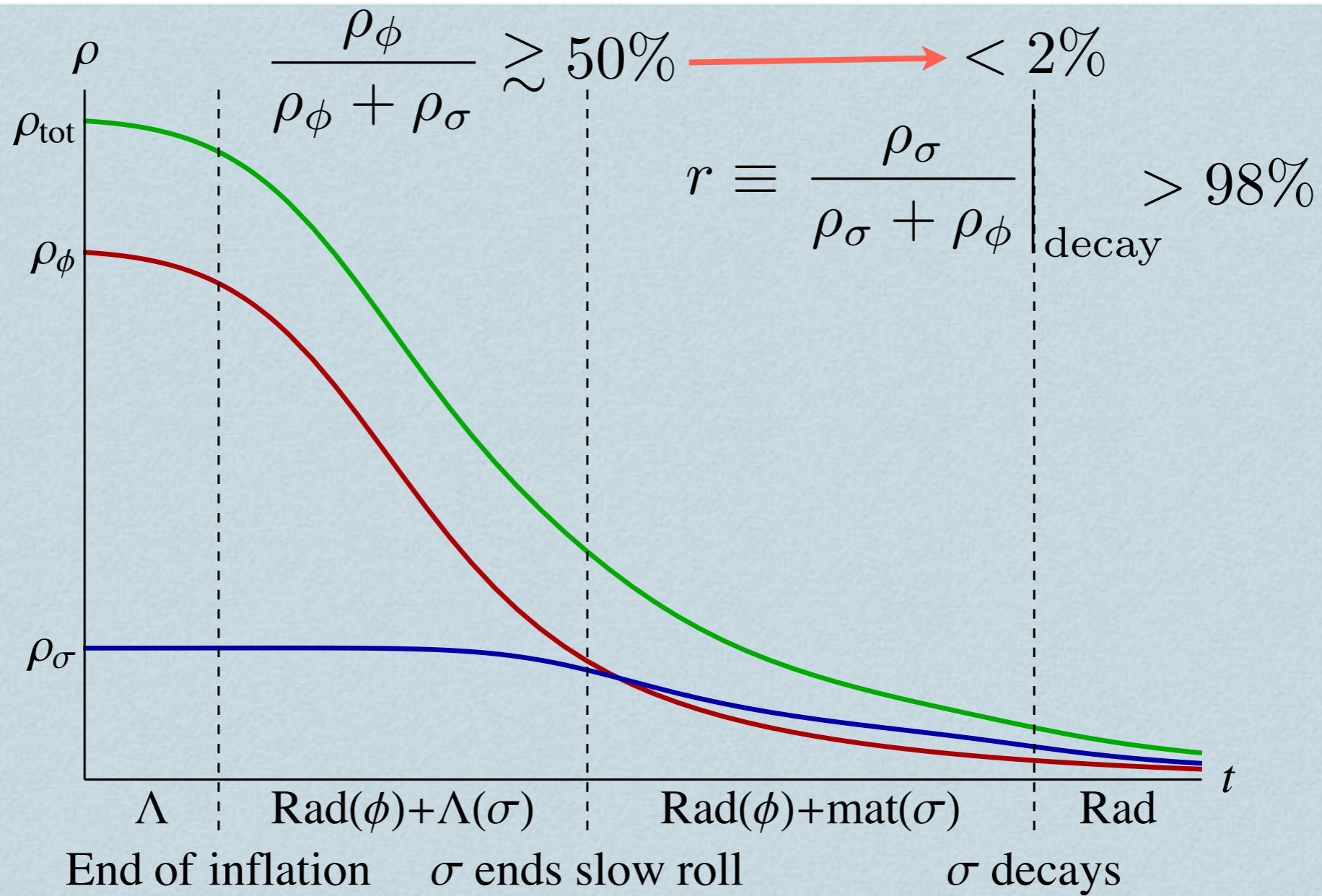
Curvaton



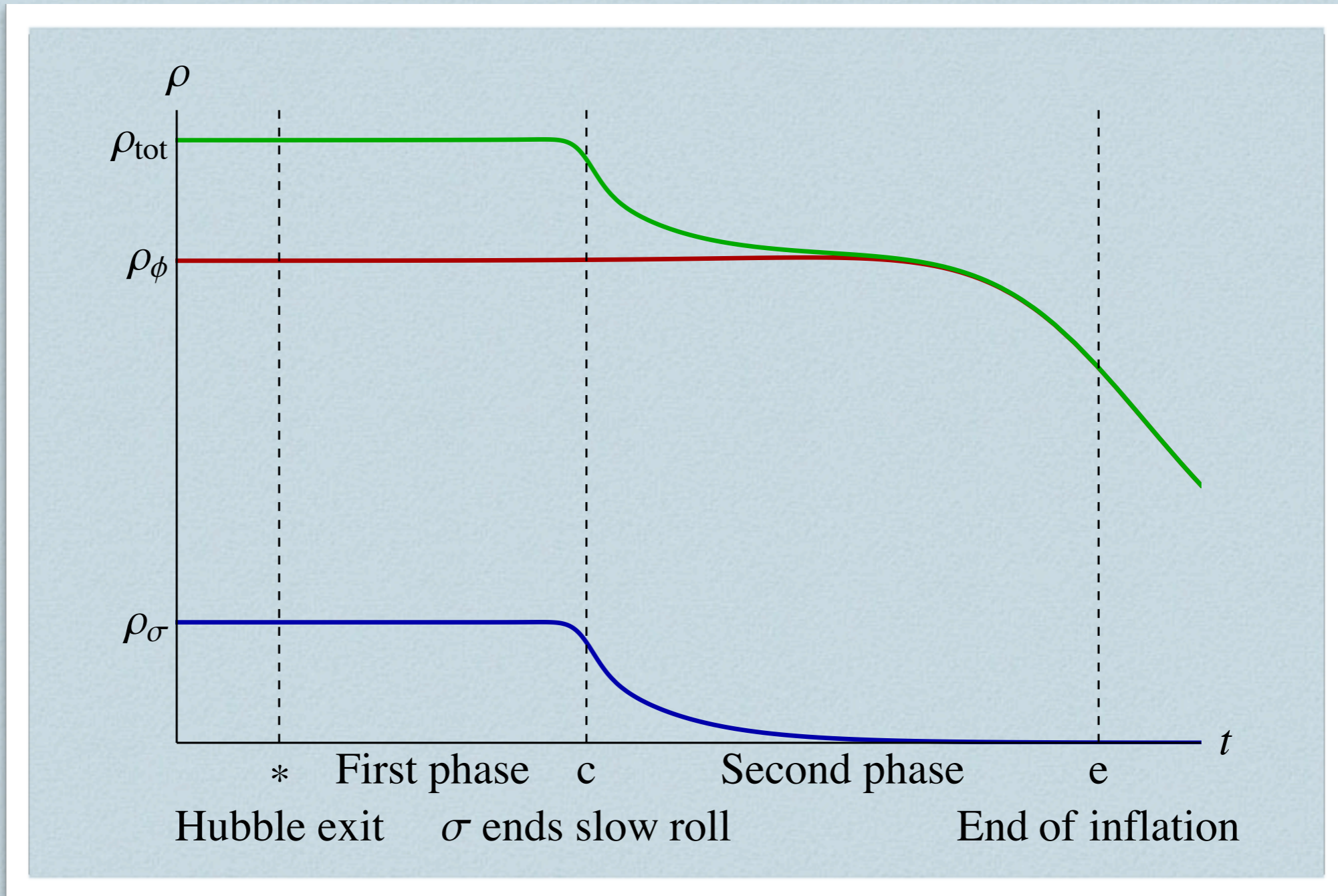
Curvaton



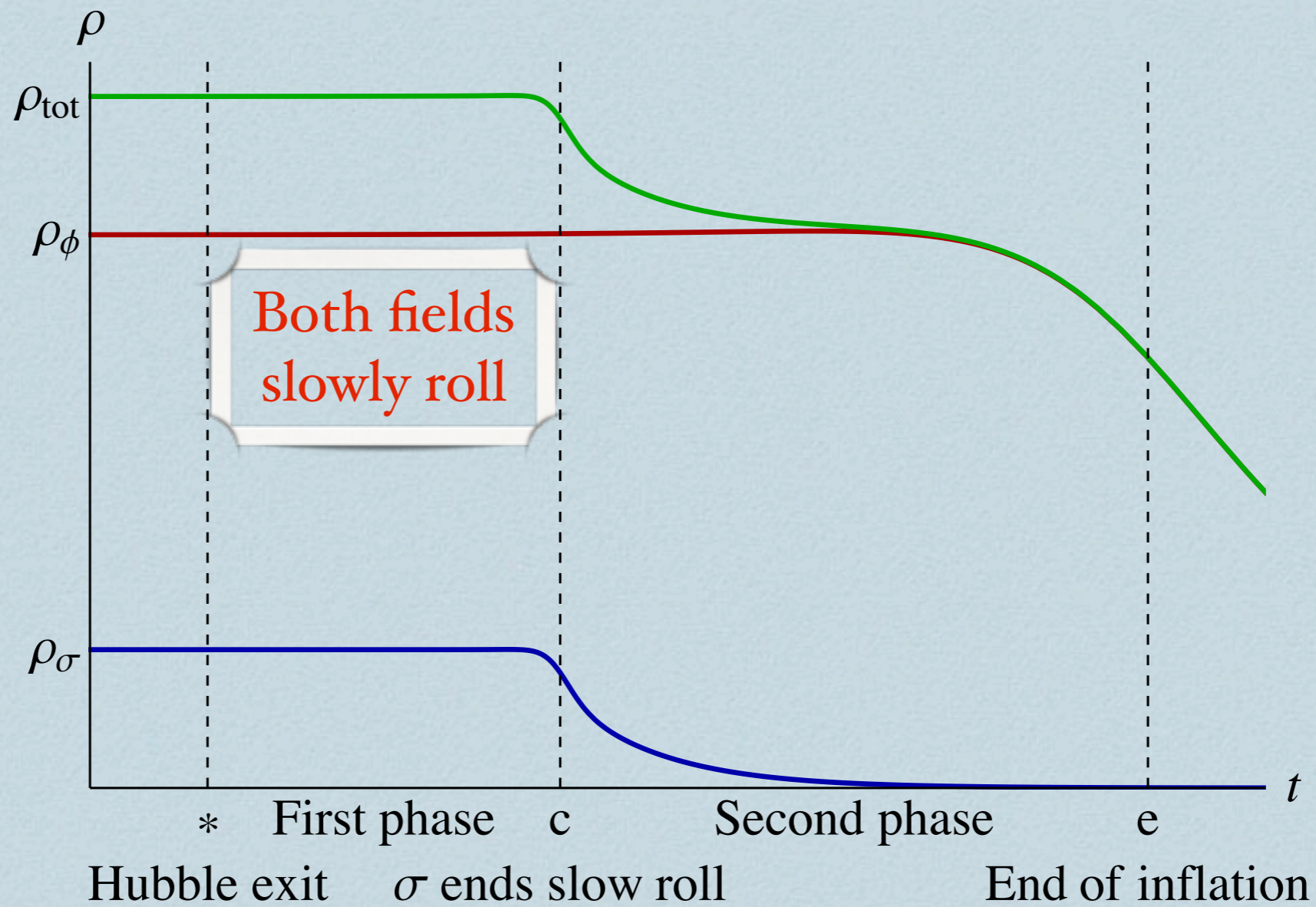
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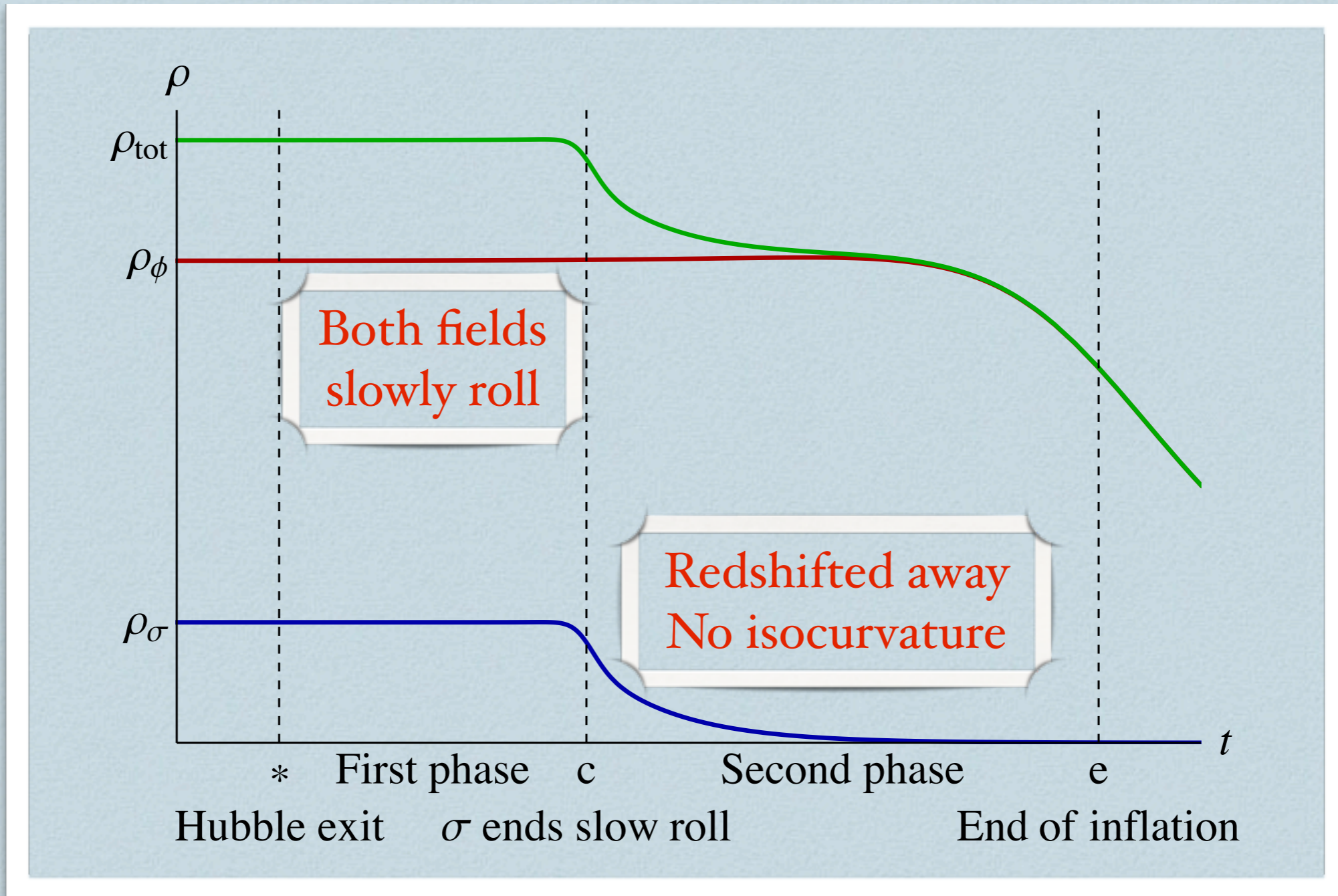
Spectator



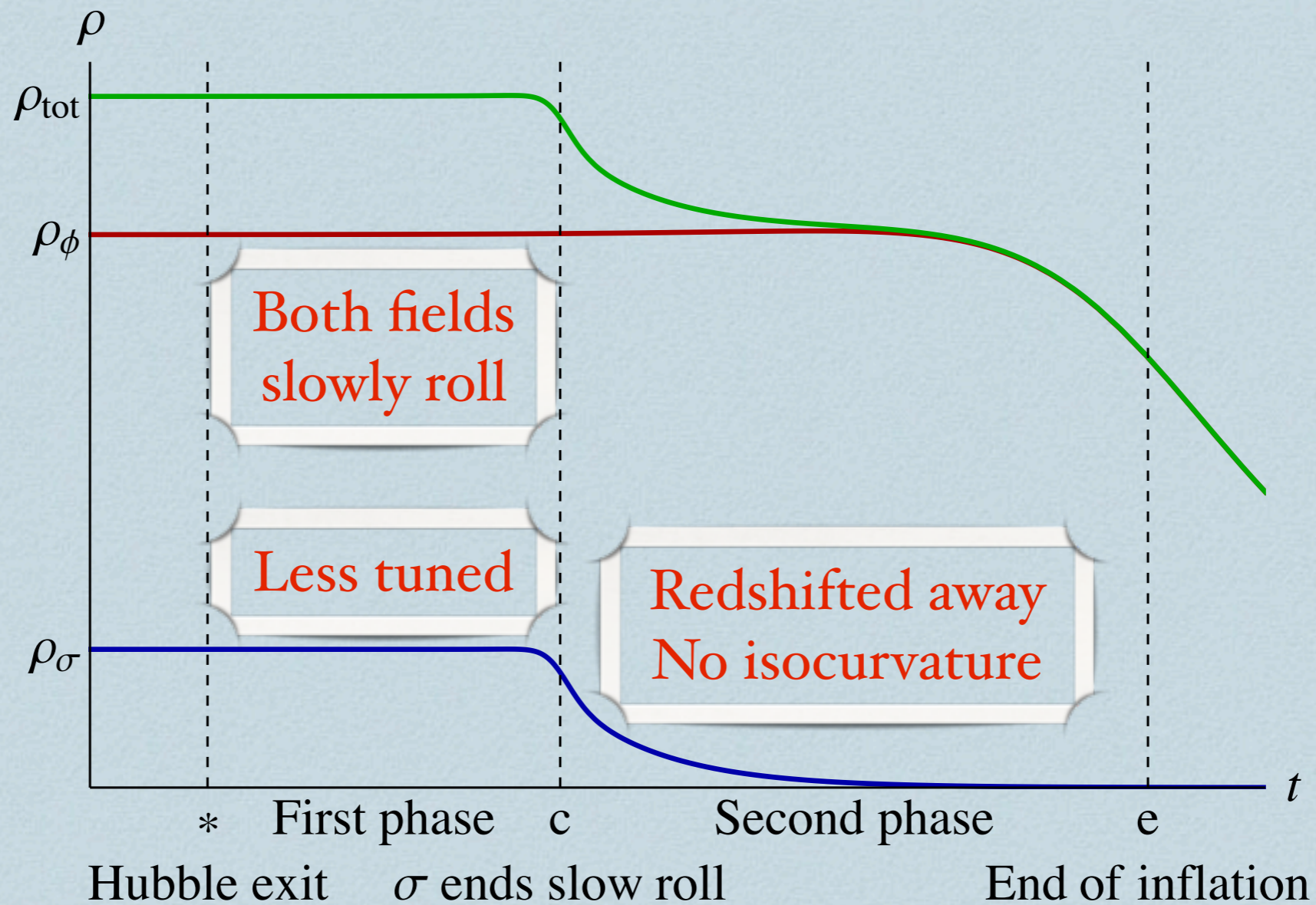
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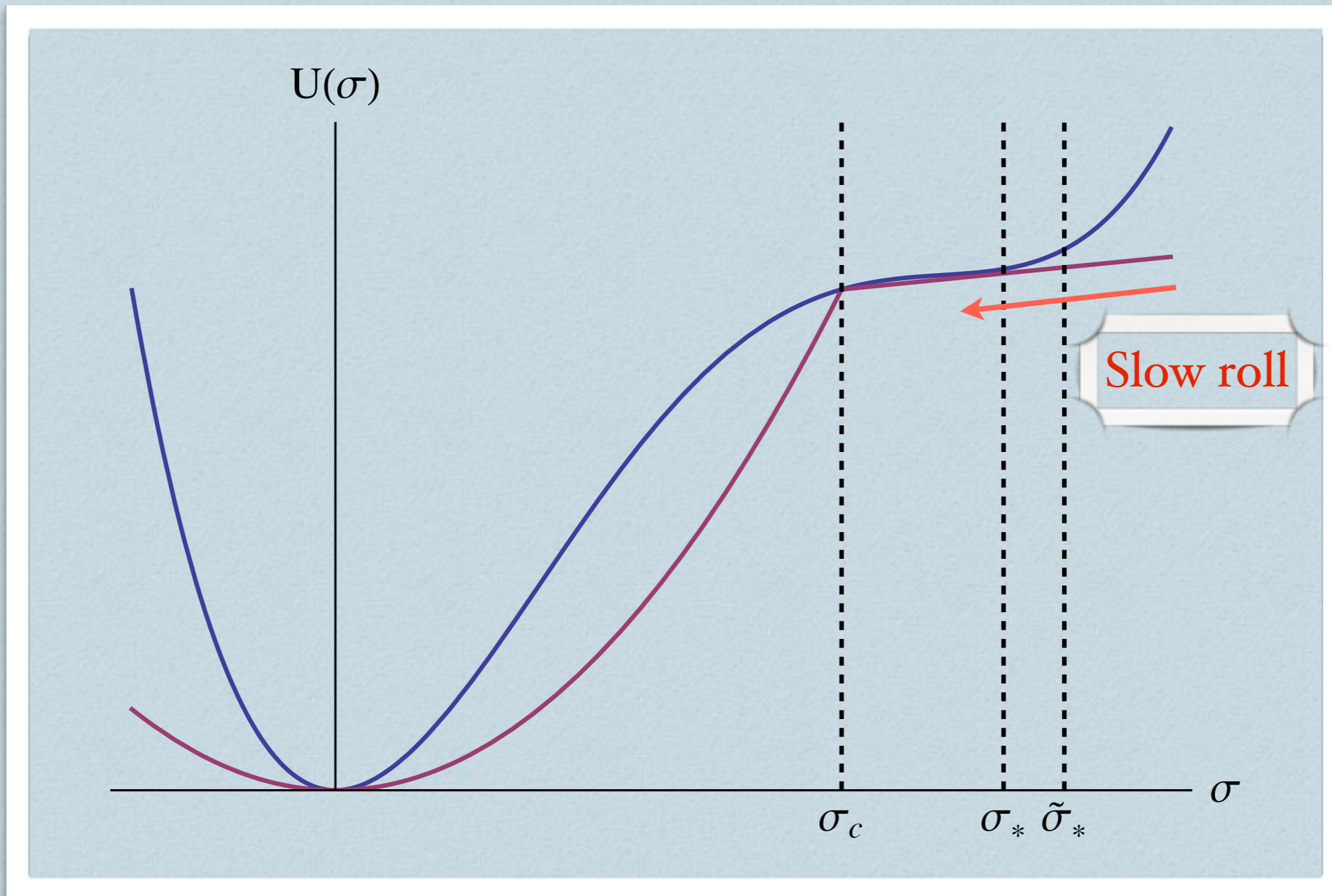
Spectator



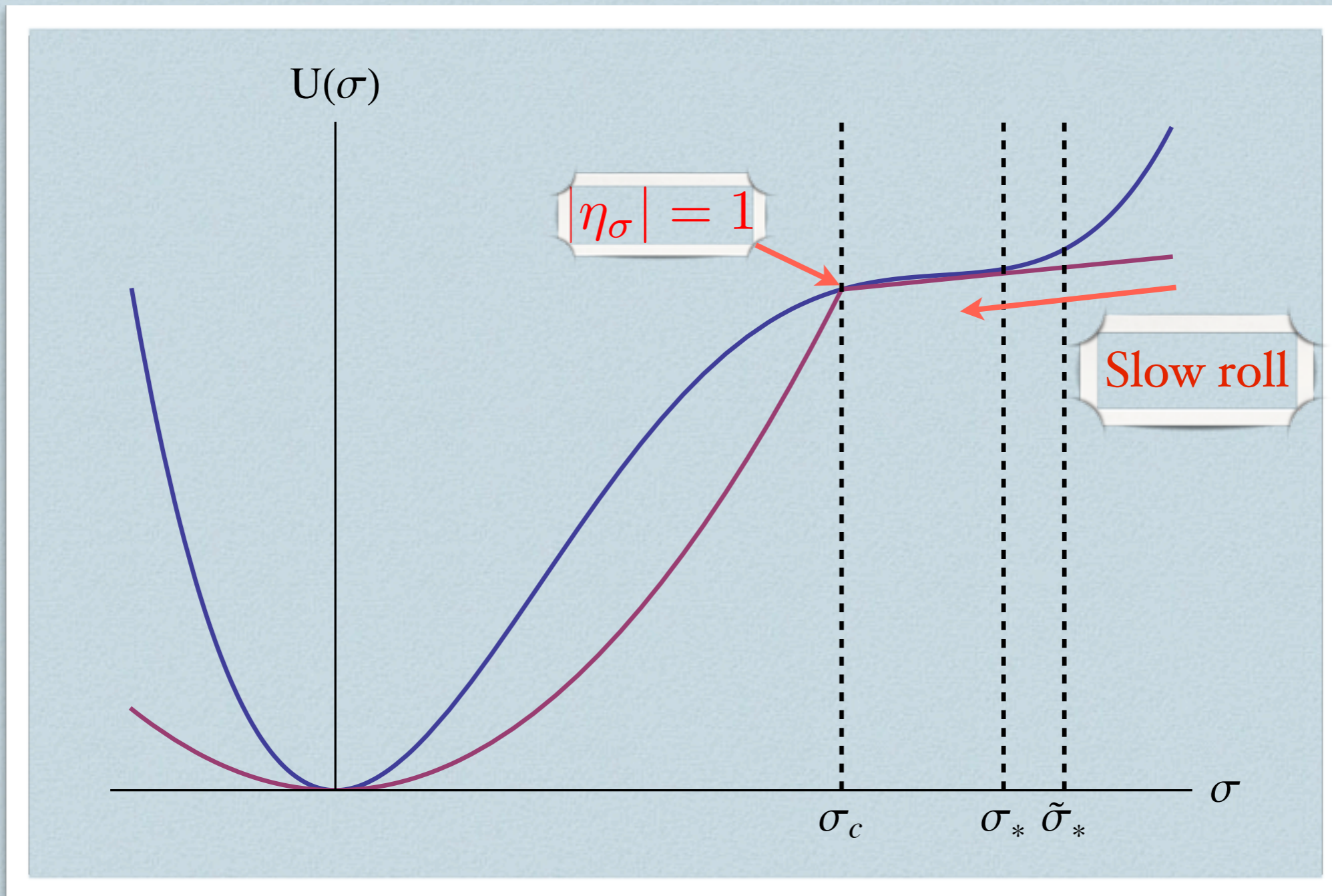
A spectator should:

- ❖ Not affect inflation dynamics when perturbed/removed
 - ❖ Subdominate the energy density
 - ❖ Not couple to the inflaton(s) (except minimally by gravity)
- ❖ Dominate (or contribute significant) curvature perturbations
- ❖ End slow roll during inflation, after the Hubble exit of the relevant scales

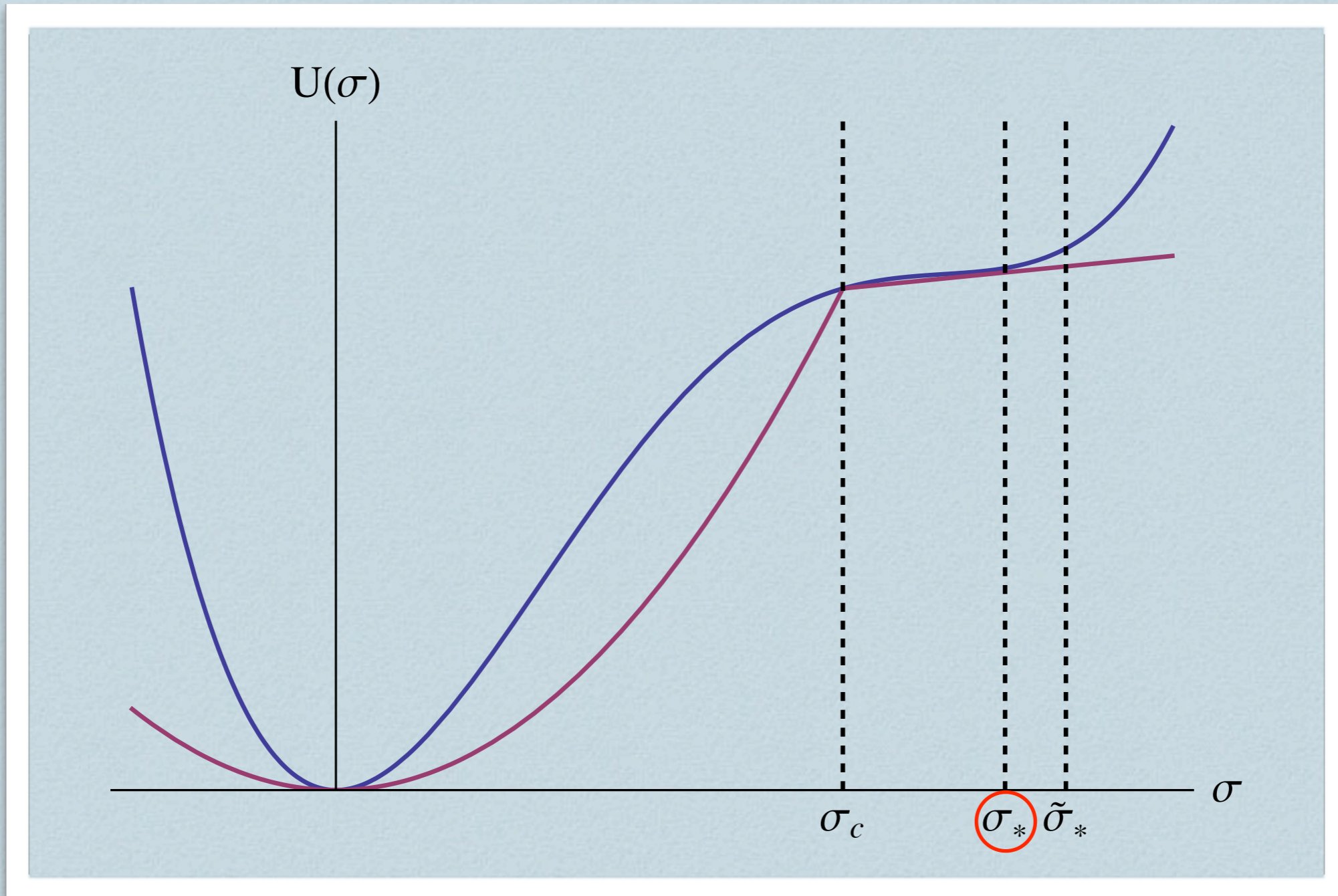
Typical potential



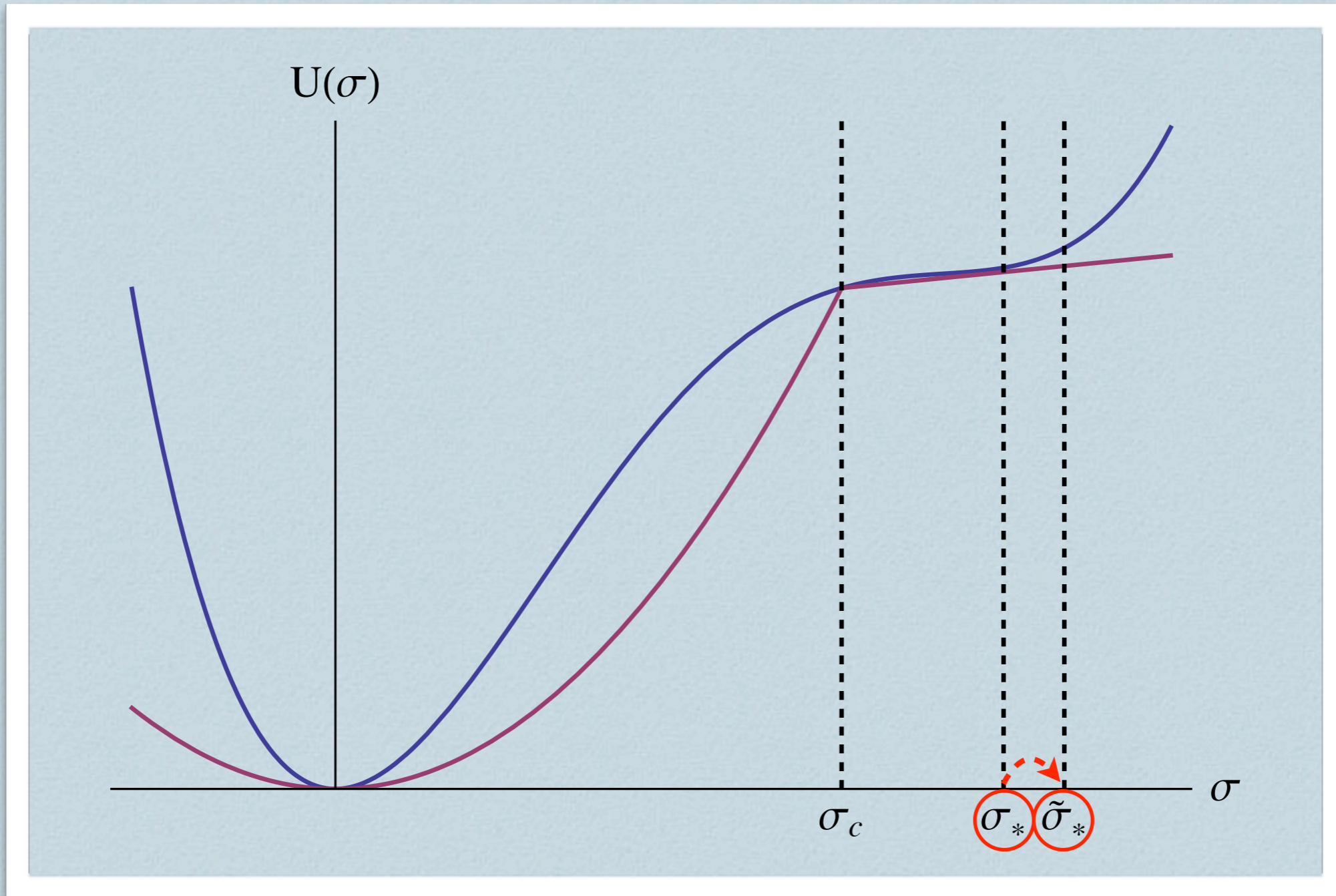
Typical potential



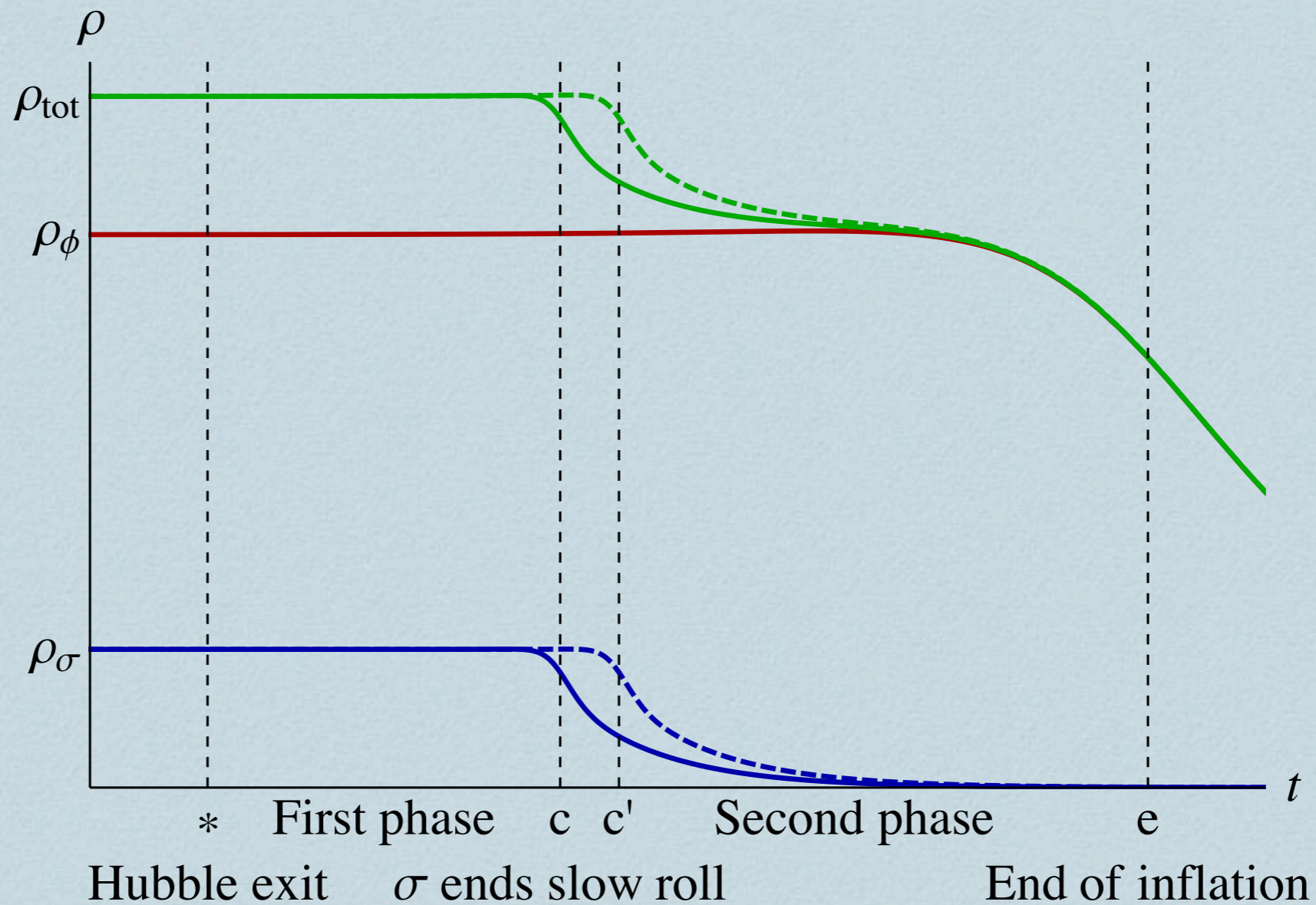
Typical potential



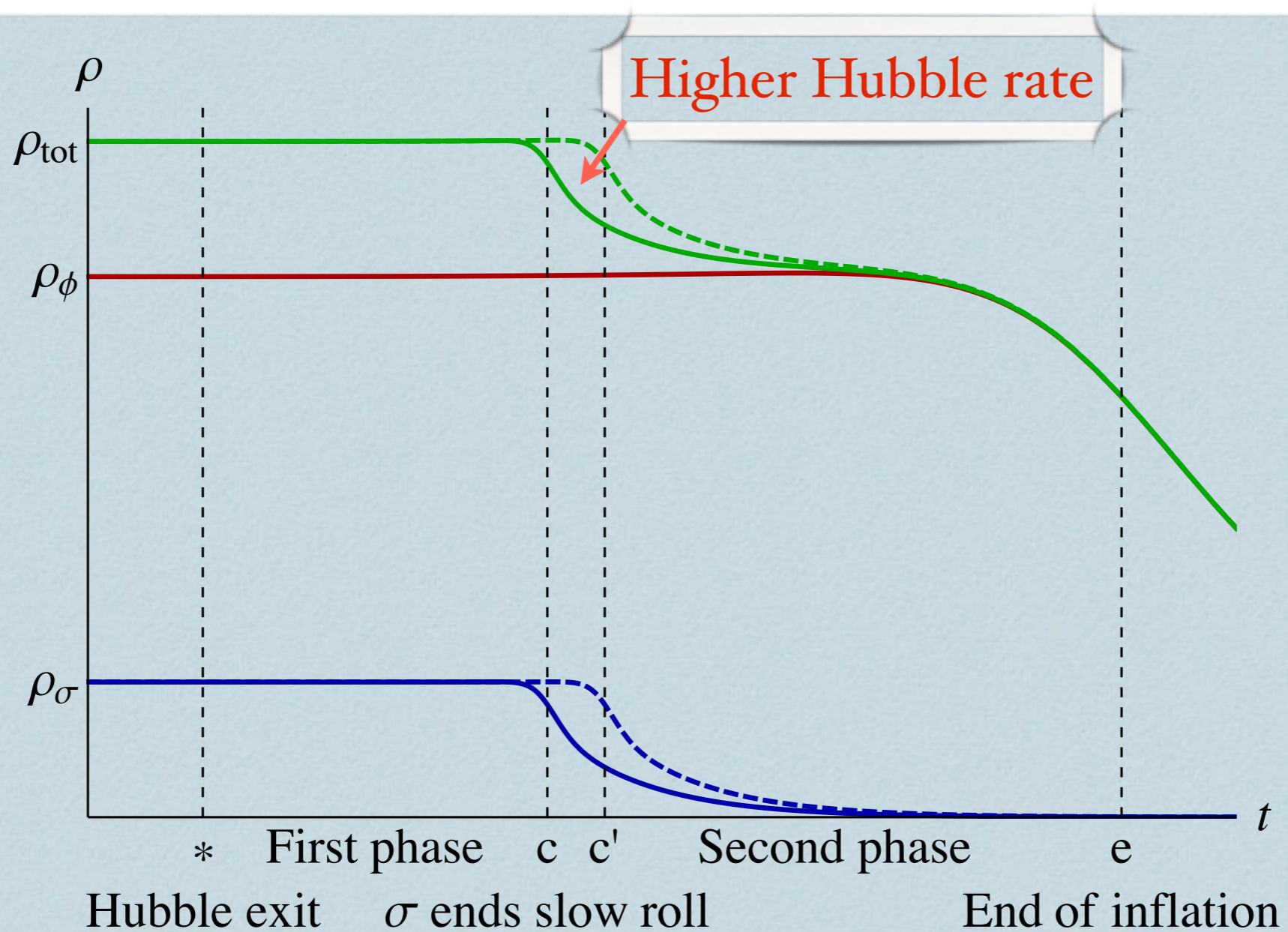
Typical potential



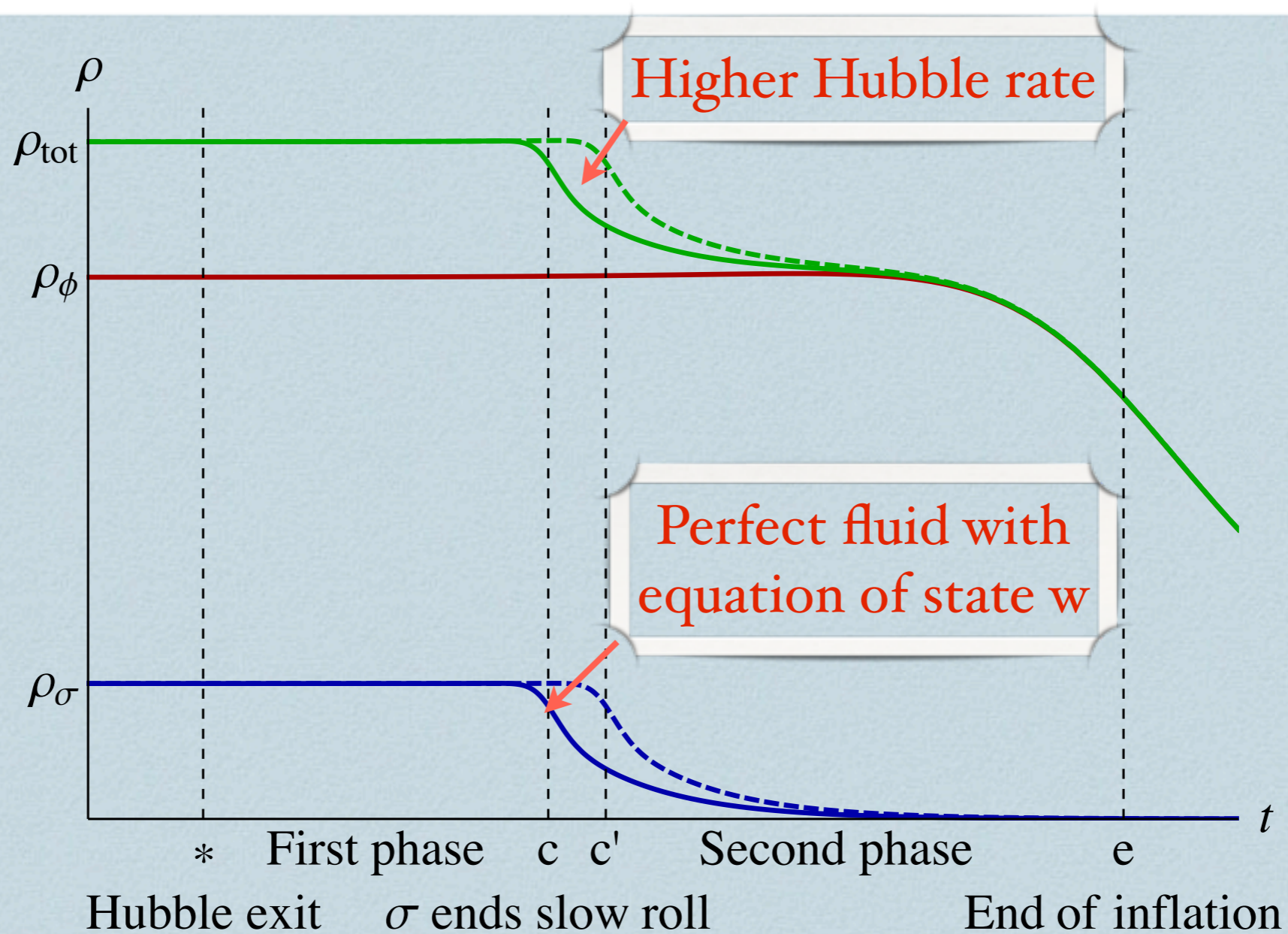
Shifting boundary



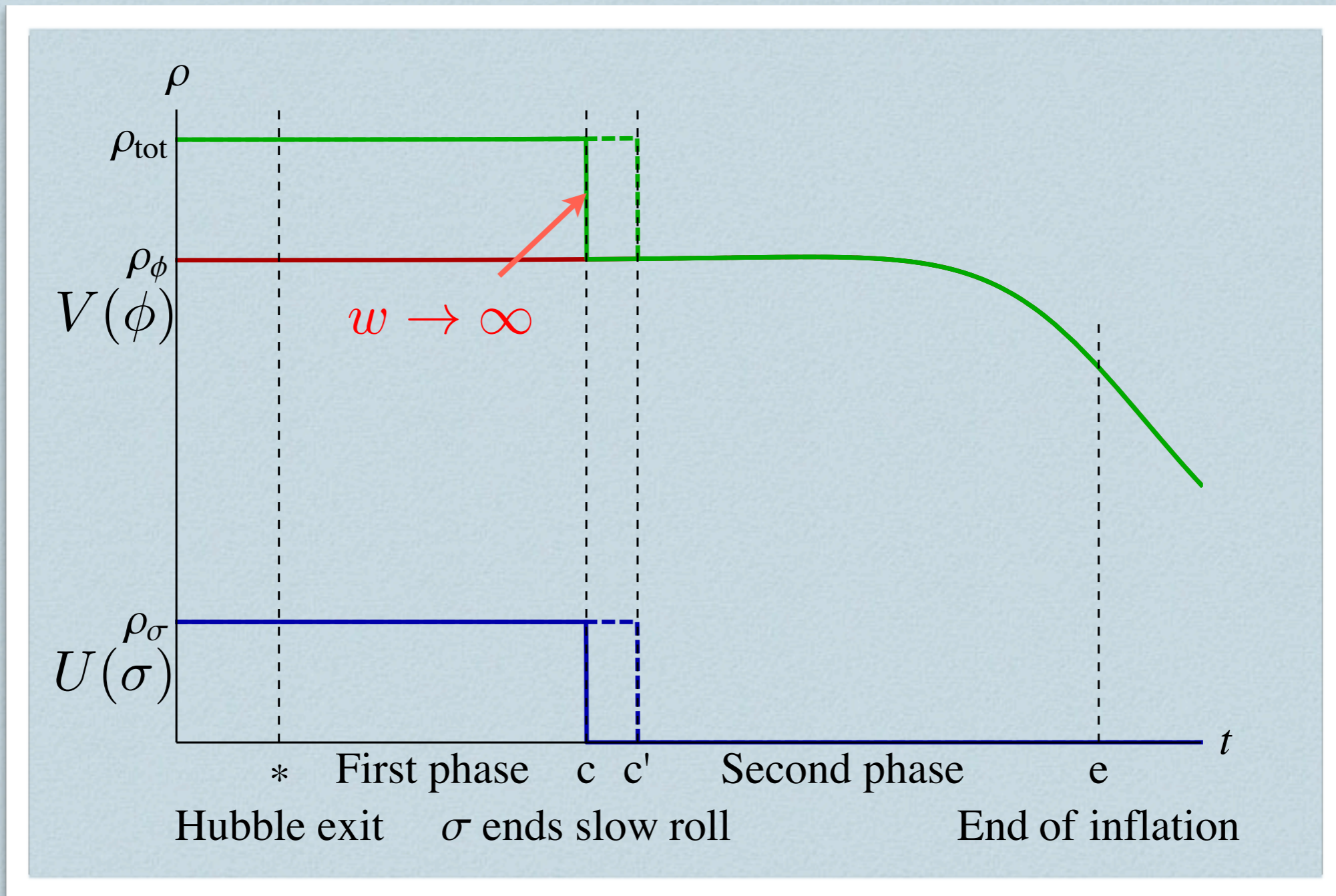
Shifting boundary



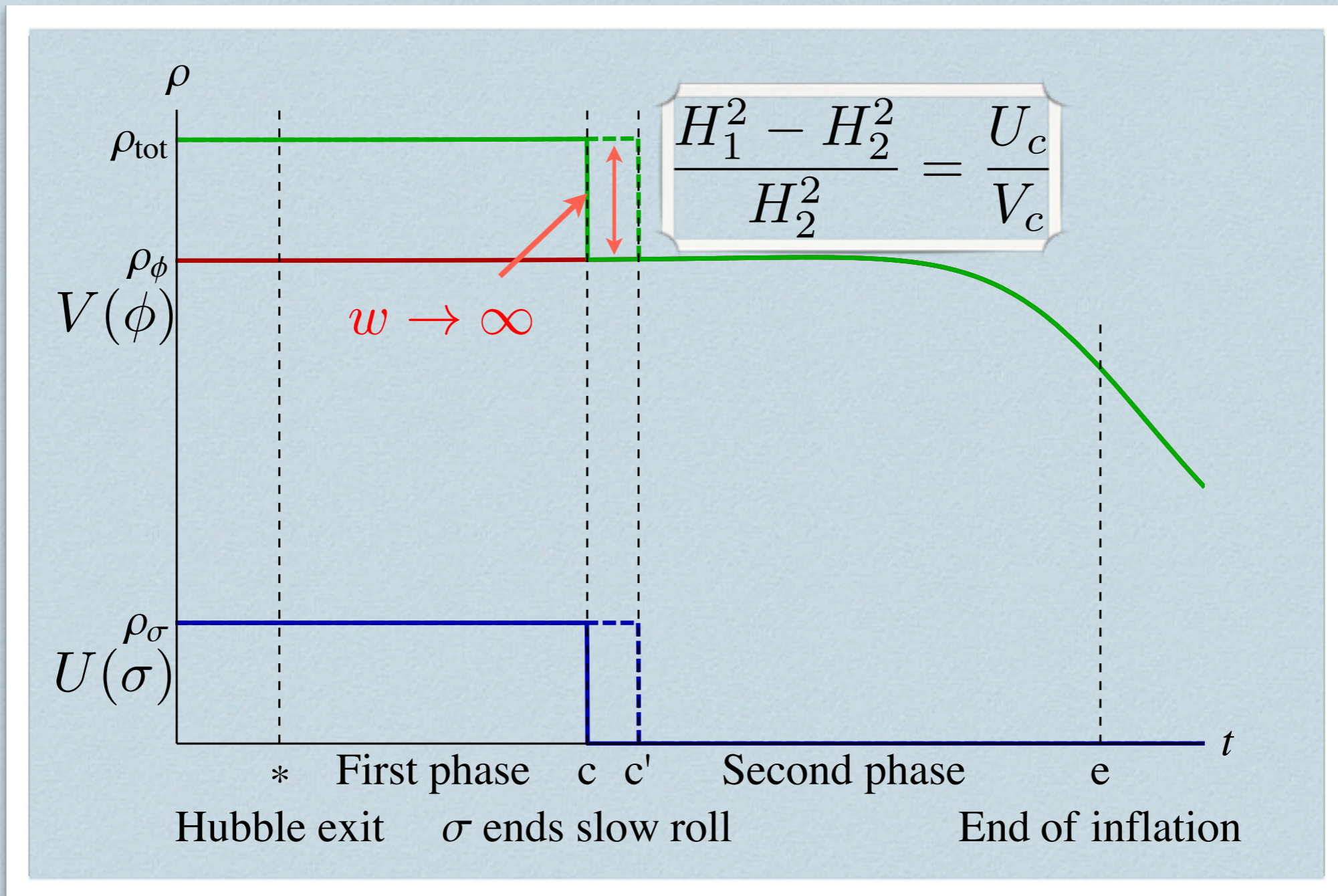
Shifting boundary



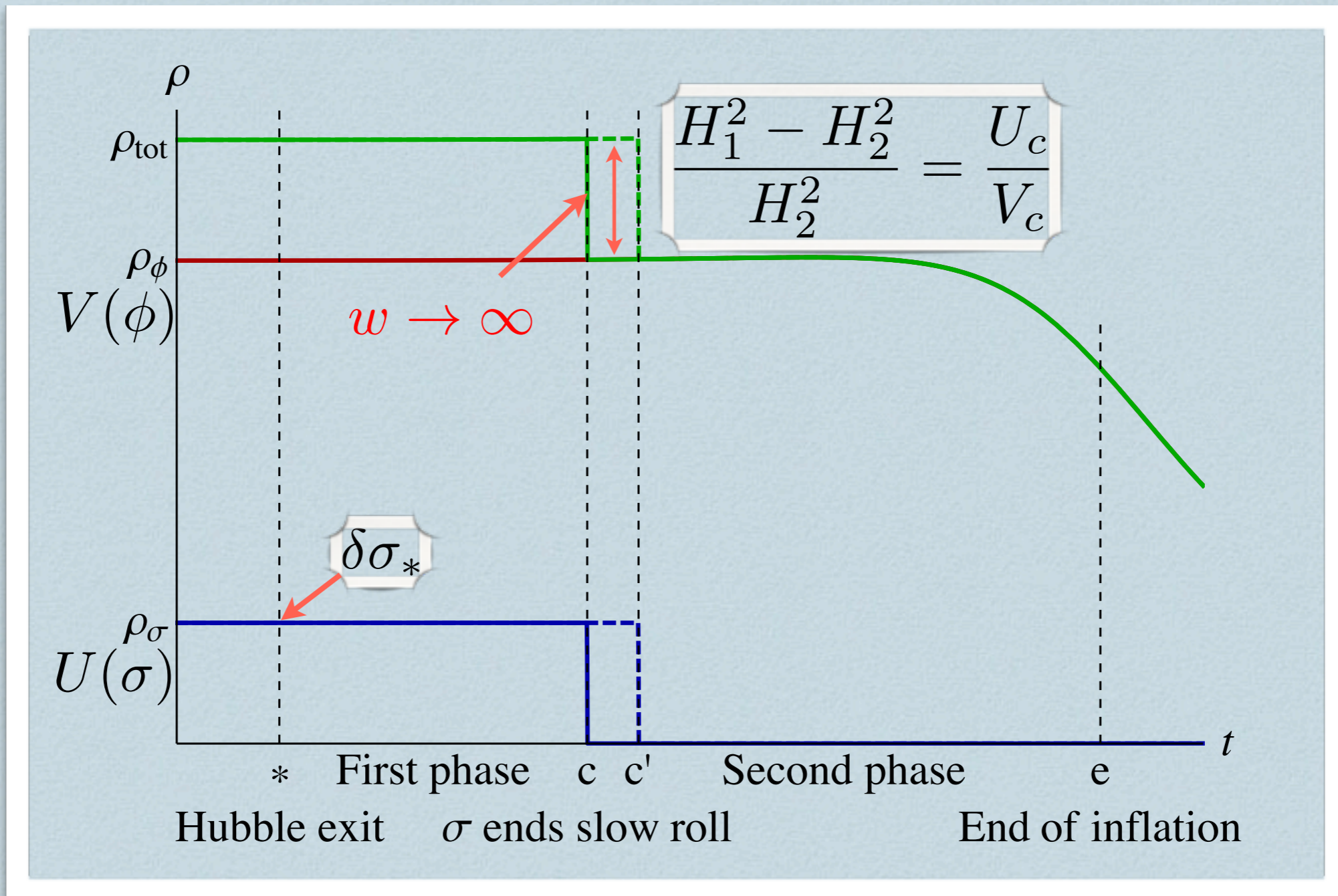
Approximated boundary



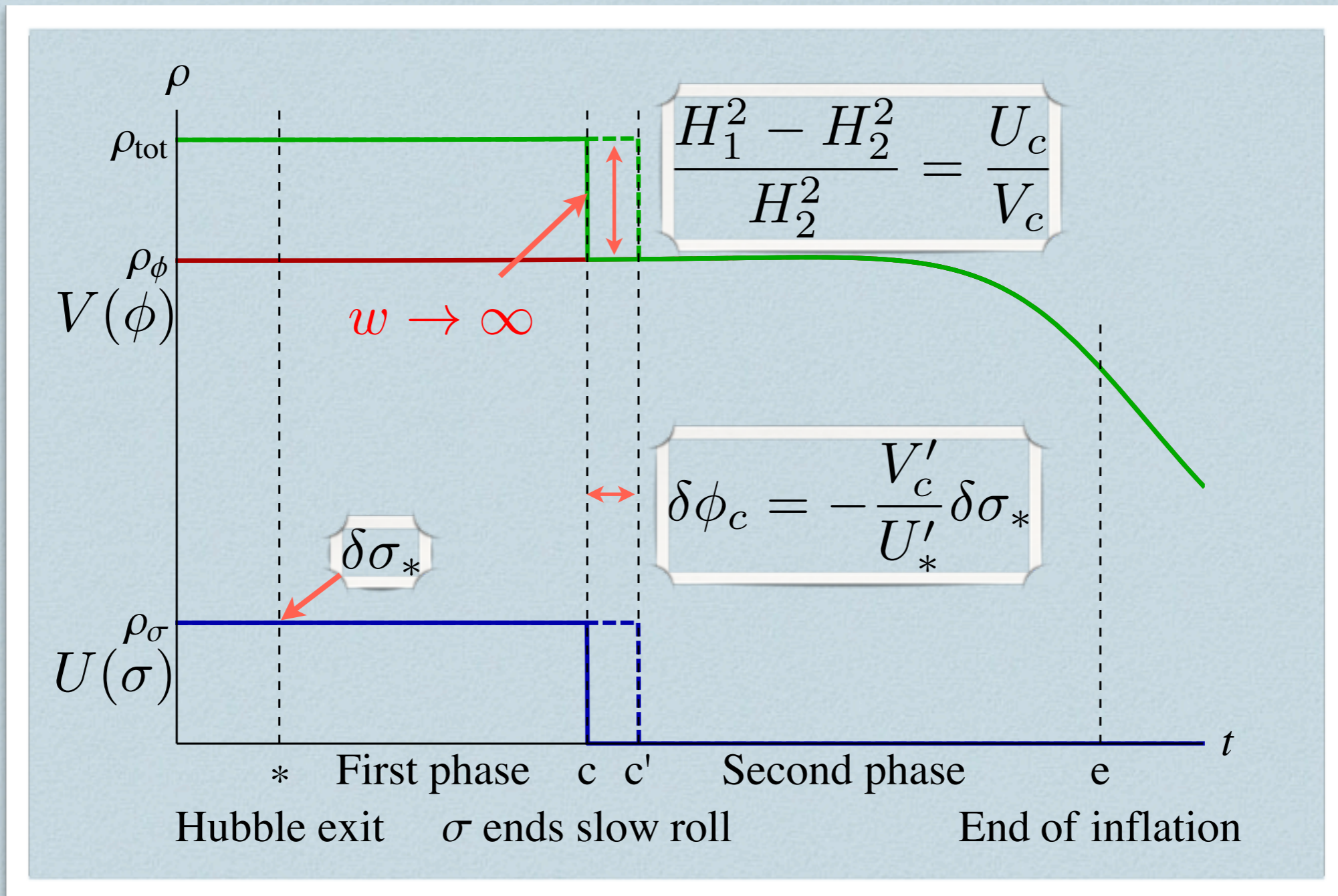
Approximated boundary



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Power spectrum

$$V_{\text{tot}} = V(\phi) + U(\sigma)$$

$$\delta N = N_\sigma \delta \sigma_* \quad N_\sigma = \frac{8\pi U_*}{M_p^2 U'_*} \left(1 + \mathcal{O}(\epsilon) + \mathcal{O}(\eta) \right)$$

$$\epsilon_\phi \equiv \frac{M_p^2 V'^2}{16\pi(U + V)^2}$$

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Spectator produces significant perturbations
when its potential is relatively flatter: $\frac{U_*'}{U_*} \lesssim \frac{V_*'}{V_*}$

Non-Gaussianity

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Curvaton: $f_{\text{NL}} \sim \frac{1}{r}$

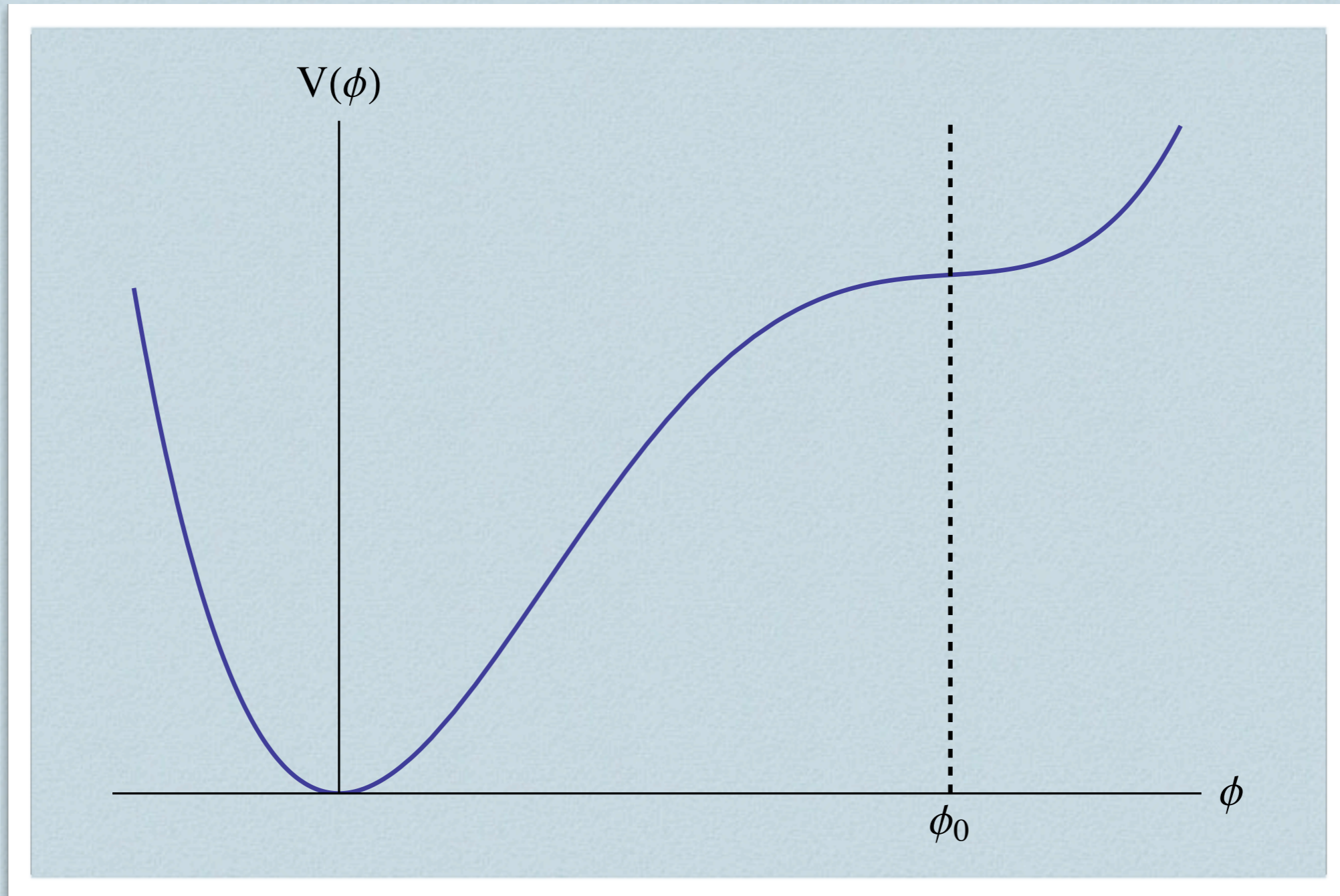
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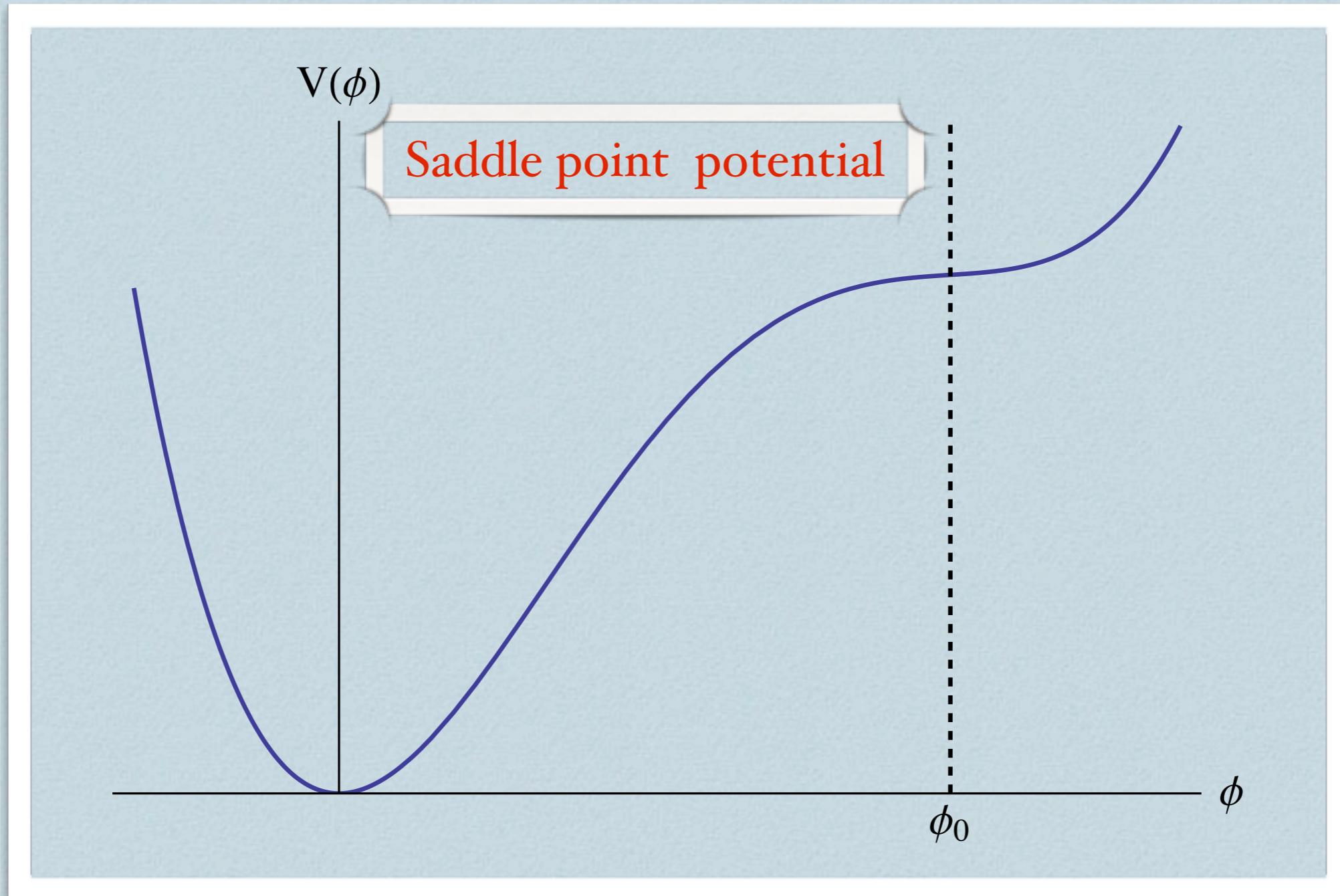
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Smaller non-Gaussianity than Curvaton: $f_{\text{NL}} \sim \frac{1}{r}$

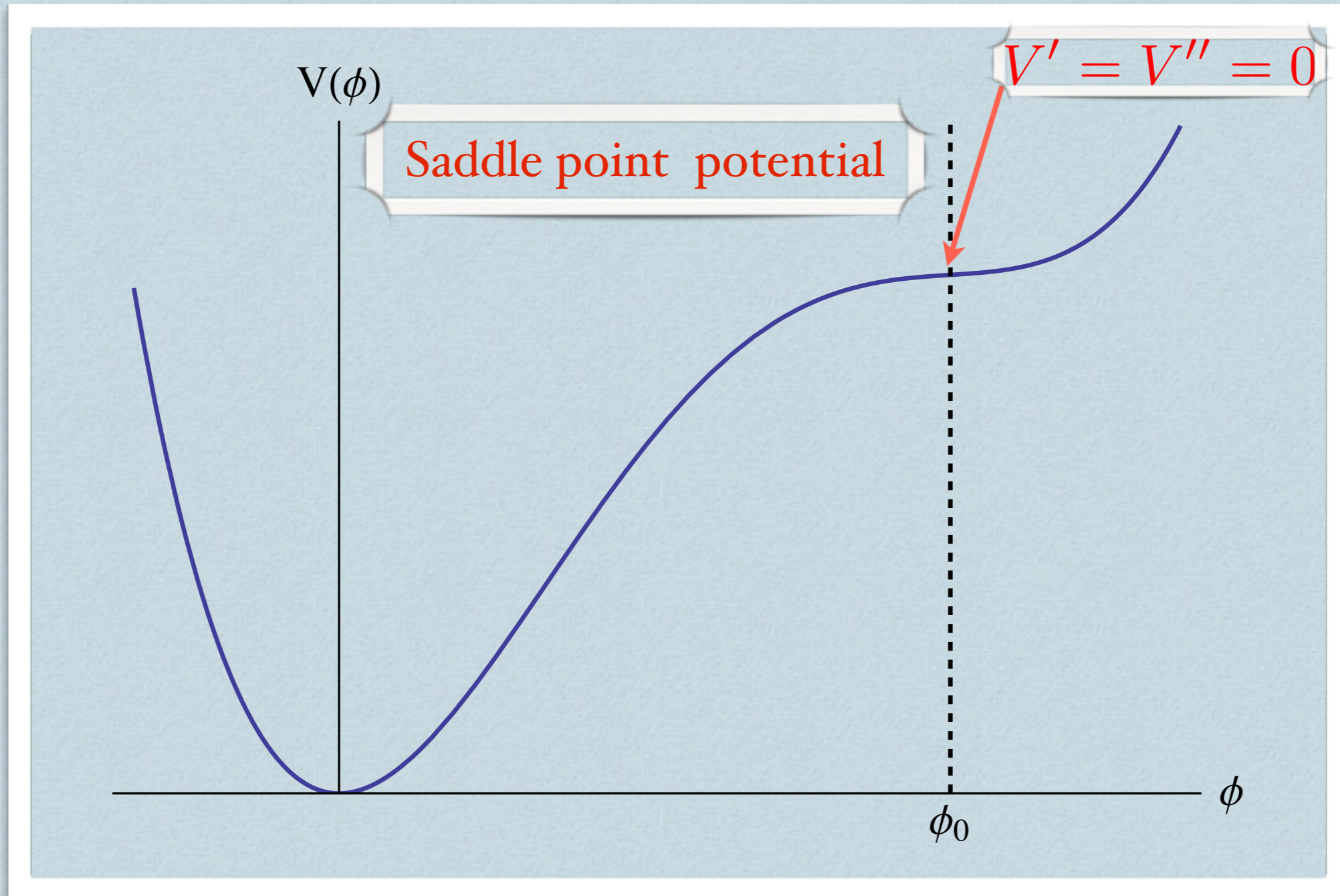
MSSM flat direction inflaton



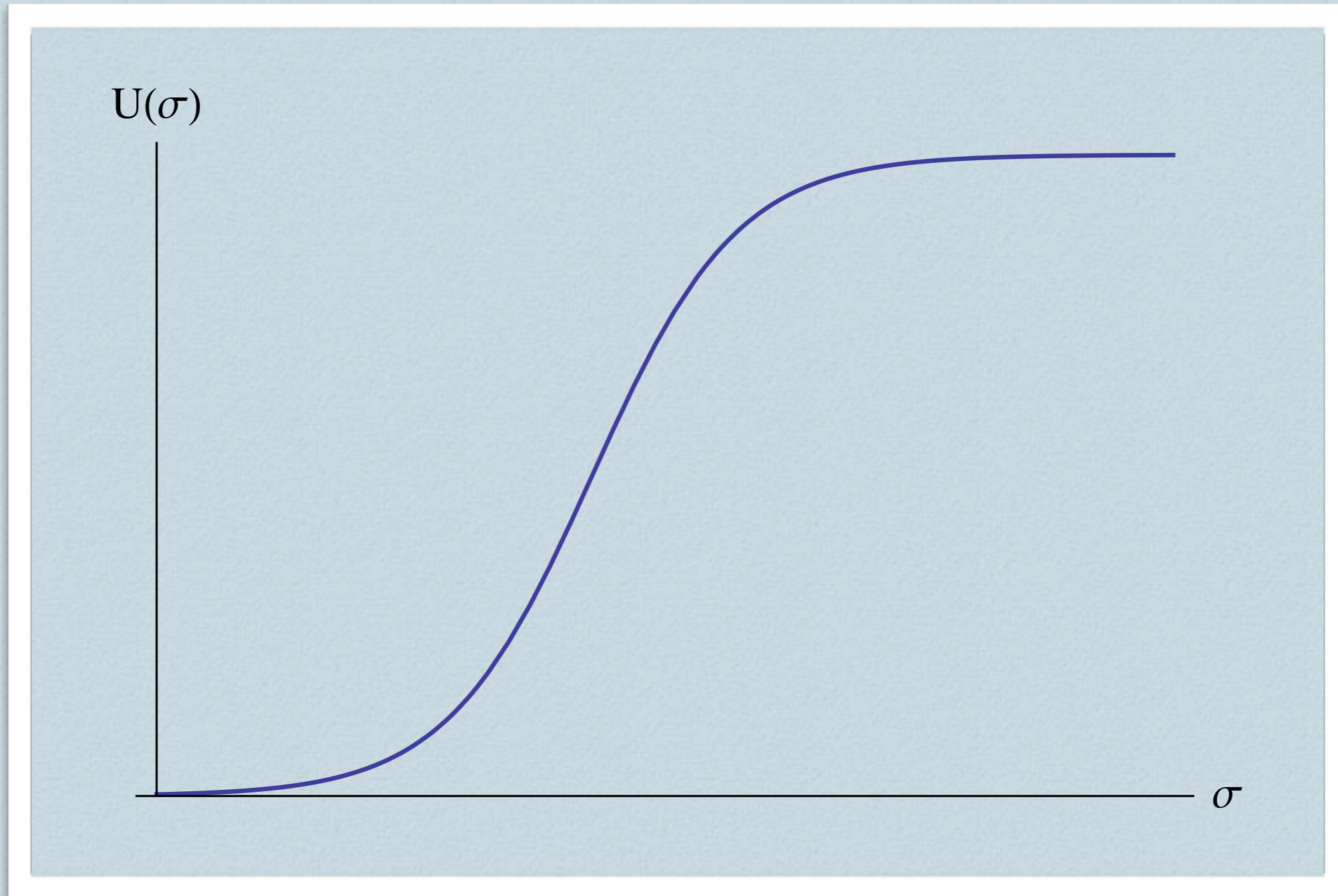
MSSM flat direction inflaton



MSSM flat direction inflaton



Hyperbolic tangent spectator



Major results

$$V(\phi) = \frac{1}{2}m^2|\phi|^2 - \frac{2mh}{3\sqrt{3}}\phi^3 + \frac{h^2}{12}|\phi|^4$$

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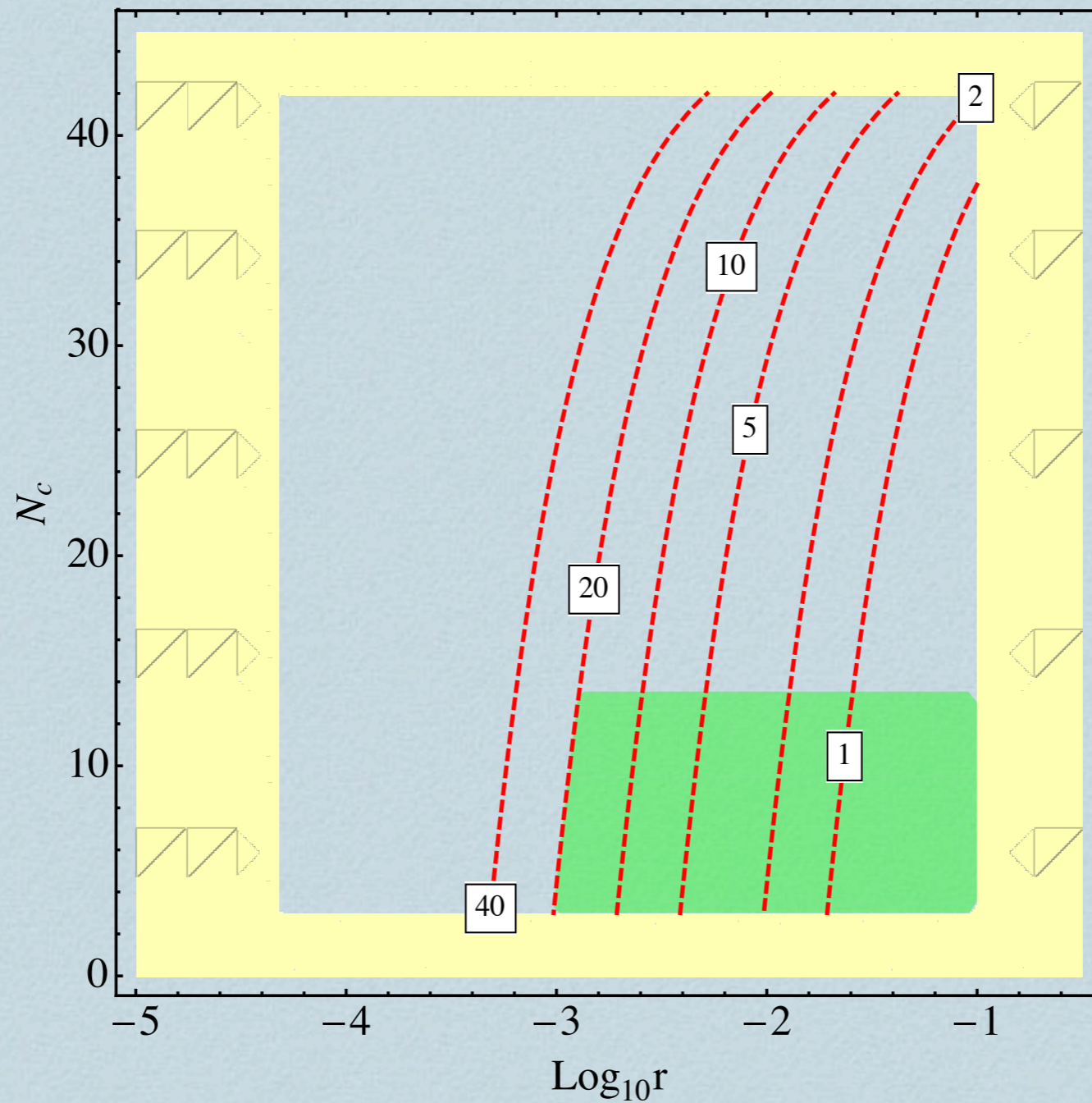
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Parameter space



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❖ No

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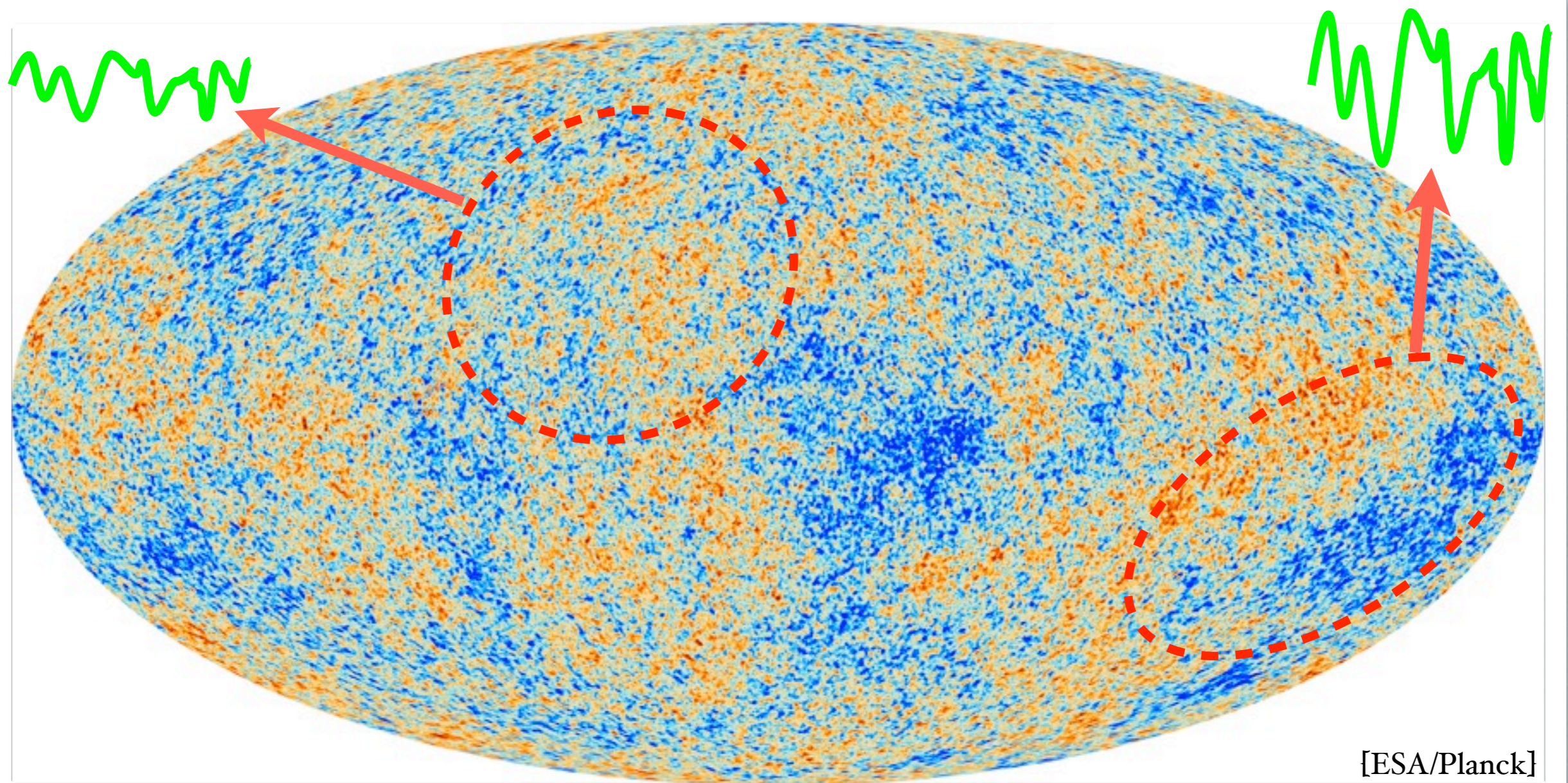
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CMB dipole asymmetry



[ESA/Planck]

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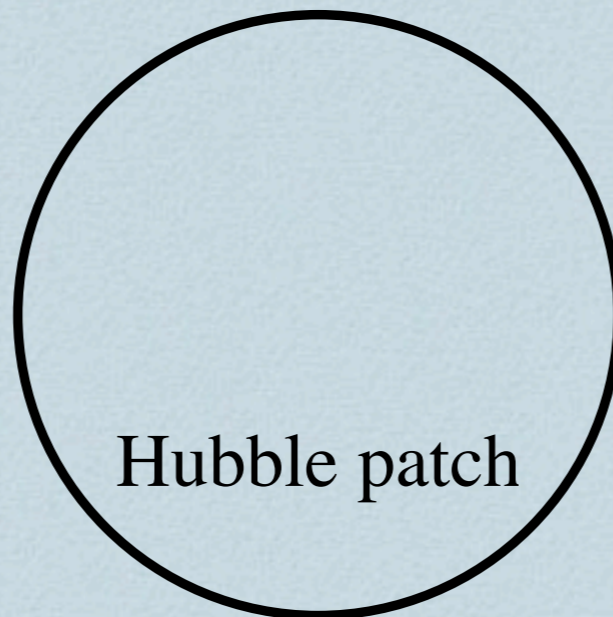
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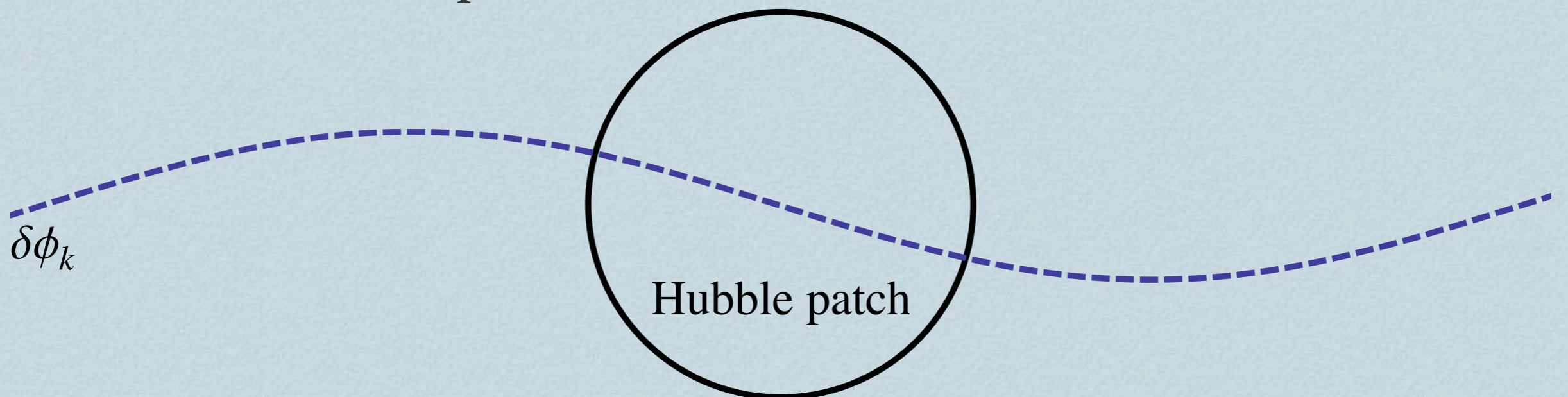
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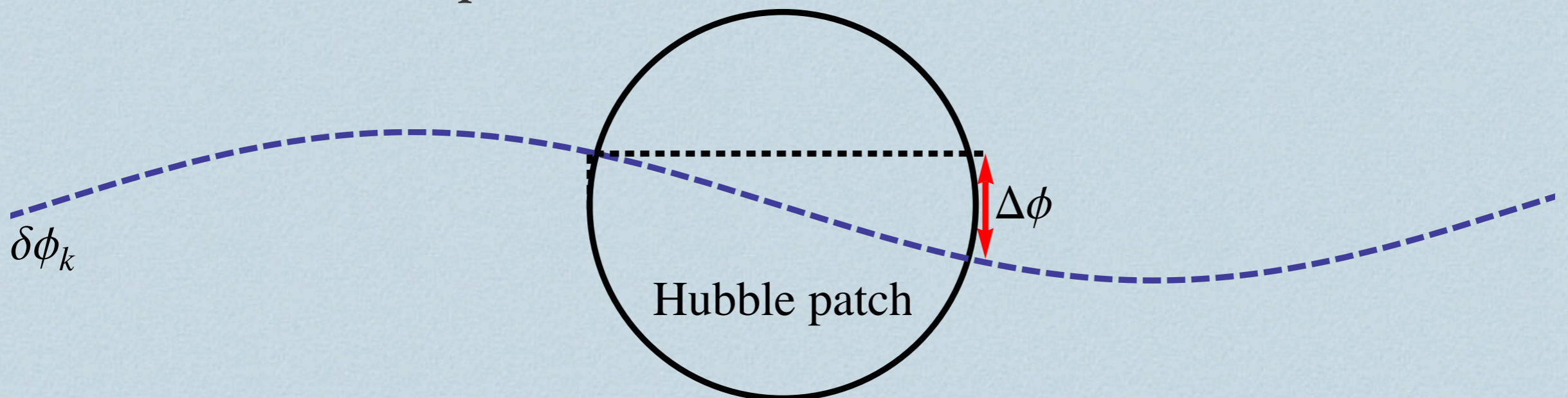
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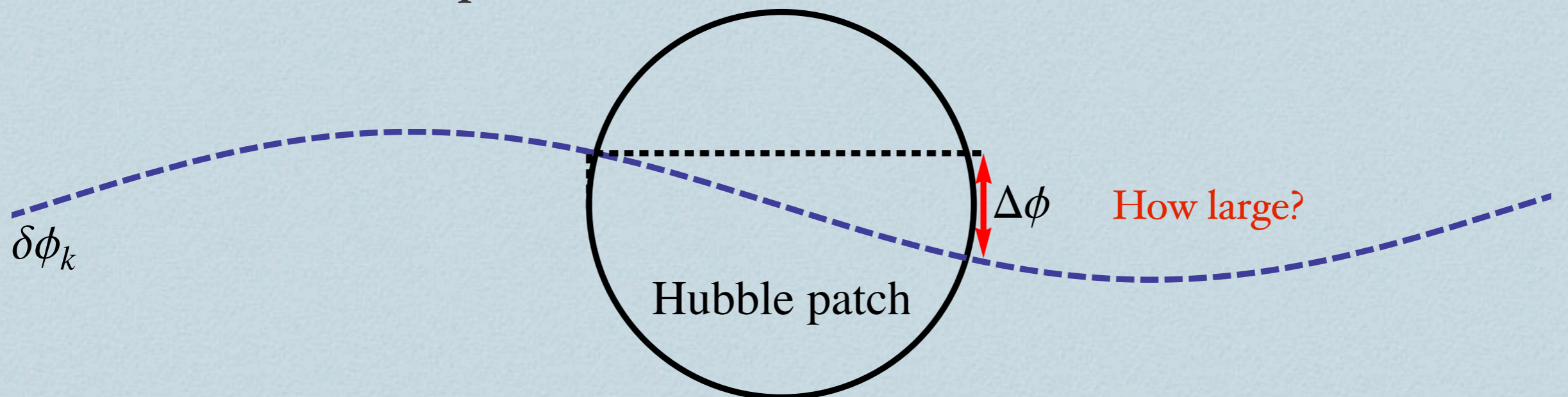
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- ❖ Planck result: $A = 0.07 \pm 0.02$
- ❖ Possible explanation: very large scale perturbations
- ❖ Alternative explanations



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Non-Gaussianity dependence

- ❖ Dependence on primordial local non-Gaussianity
 - ❖ Single perturbation source:

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- ❖ Single perturbation source:

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σ generates curvature perturbations
and gains very large scale perturbations

Non-Gaussianity dependence

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❖ Single perturbation source:

$$A = \frac{3}{5} \frac{|\Delta\sigma|}{\sqrt{P_{\delta\sigma_*}}} |f_{\text{NL}}| \sqrt{P_\zeta}$$

❖ Multi perturbation sources:

$$A < \frac{|\Delta\sigma|}{2\sqrt{P_{\delta\sigma_*}}} \sqrt{\tau_{\text{NL}} P_\zeta}$$

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$$f_{\text{NL}} = 2.7 \pm 11.6$$

$$A = \frac{3}{5} \frac{|\Delta\sigma|}{\sqrt{P_{\delta\sigma_*}}} |f_{\text{NL}}| \sqrt{P_{\zeta}}$$

$$\frac{|\Delta\sigma|}{\sqrt{P_{\delta\sigma_*}}} > 174$$

❖ Multi perturbation sources:

$$\tau_{\text{NL}} < 2800$$

$$A < \frac{|\Delta\sigma|}{2\sqrt{P_{\delta\sigma_*}}} \sqrt{\tau_{\text{NL}} P_{\zeta}}$$

$$\frac{|\Delta\sigma|}{\sqrt{P_{\delta\sigma_*}}} > 56$$

Non-Gaussianity dependence

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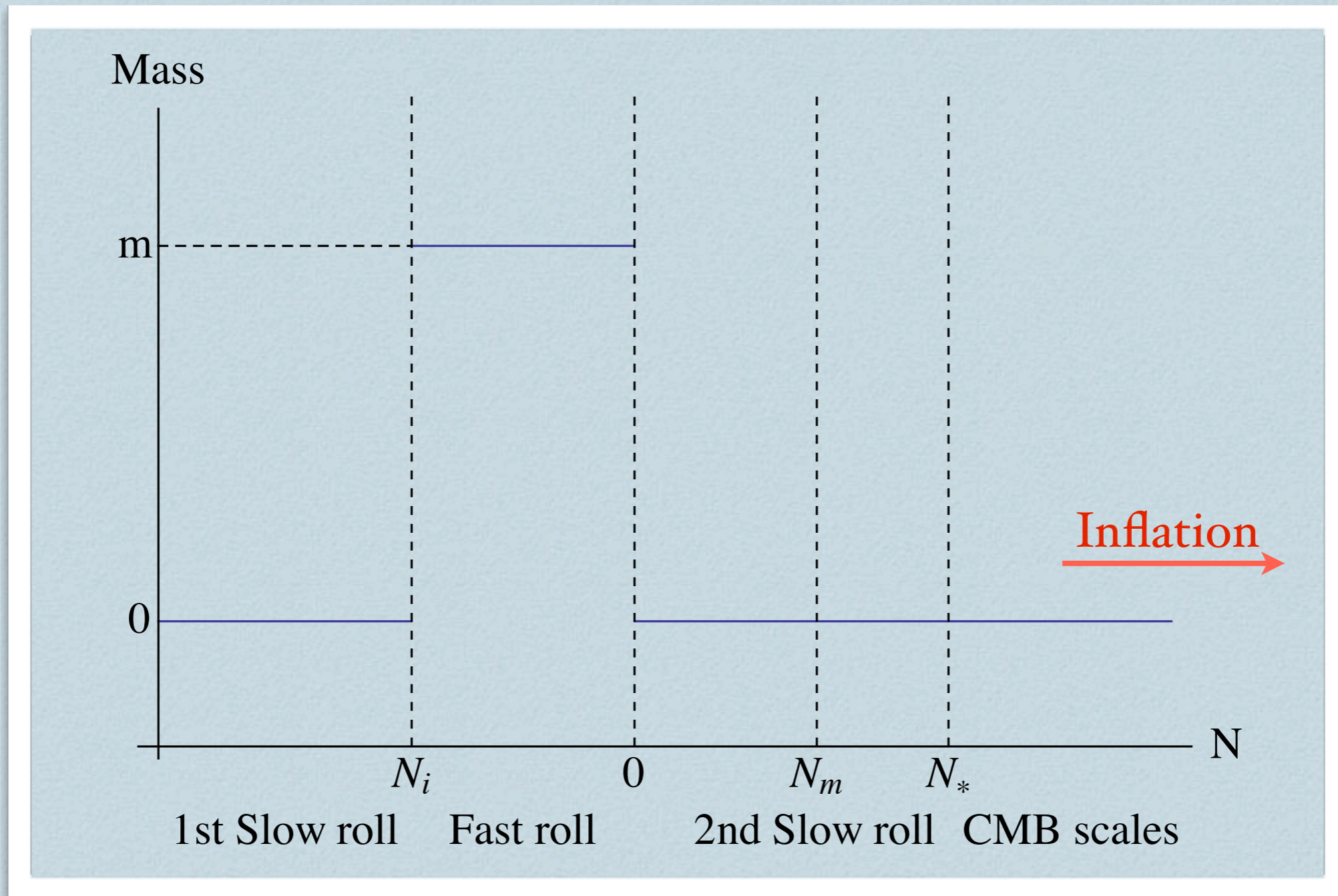
$$A = \frac{3}{5} \frac{|\Delta\sigma|}{\sqrt{P_{\delta\sigma_*}}} |f_{\text{NL}}| \sqrt{P_\zeta} \quad \frac{|\Delta\sigma|}{\sqrt{P_{\delta\sigma_*}}} > 174$$

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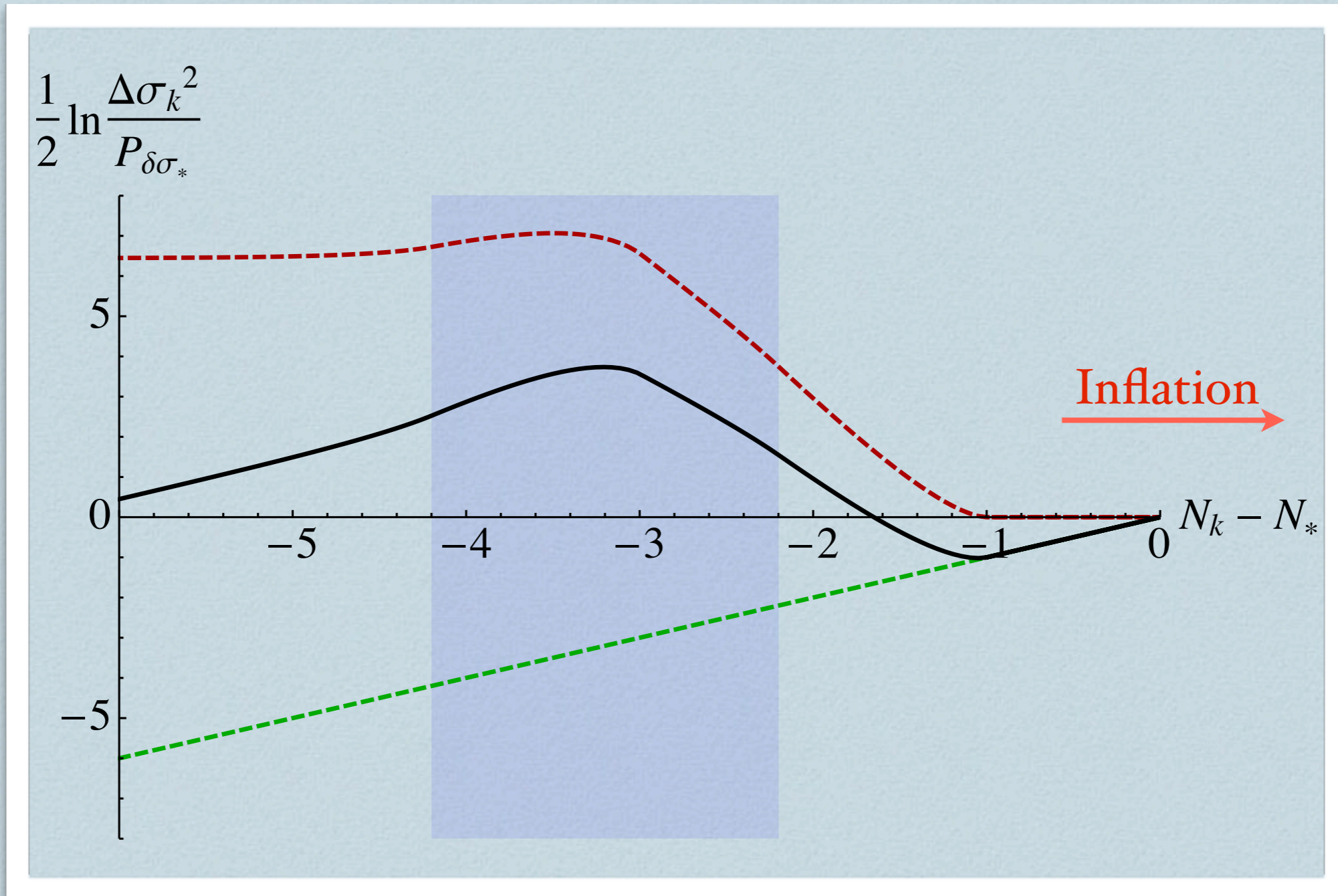
❖ Scale invariant spectrum $\frac{|\Delta\sigma|}{\sqrt{P_{\delta\sigma_*}}} \lesssim 2$ must be violated

Tachyonic fast roll enhancement



(Fast roll for the field, not inflation)

Tachyonic fast roll enhancement



(Fast roll for the field, not inflation)

Tachyonic fast roll enhancement

$$m^2 = (e^{2N_m} - 1)2H^2$$

$$N_m = 1.4$$

Tachyonic fast roll enhancement

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$$N_* - 4.2 < N < N_* - 2.4$$

$$f_{\text{NL}} = 7$$

Tachyonic fast roll enhancement

$$m^2 = (e^{2N_m} - 1)2H^2$$
$$N_* - 4.2 < N < N_* - 2.4$$
$$A = 0.07$$
$$N_m = 1.4$$
$$f_{\text{NL}} = 7$$

```
graph LR; Eq1["m^2 = (e^{2N_m} - 1)2H^2"] --> A["A = 0.07"]; Eq2["N_* - 4.2 < N < N_* - 2.4"] --> A; Eq3["N_m = 1.4"] --> A; Eq4["f_{NL} = 7"] --> A;
```

Tachyonic fast roll enhancement

$$m^2 = (e^{2N_m} - 1)2H^2$$

$N_m = 1.4$

$$N_* - 4.2 < N < N_* - 2.4$$

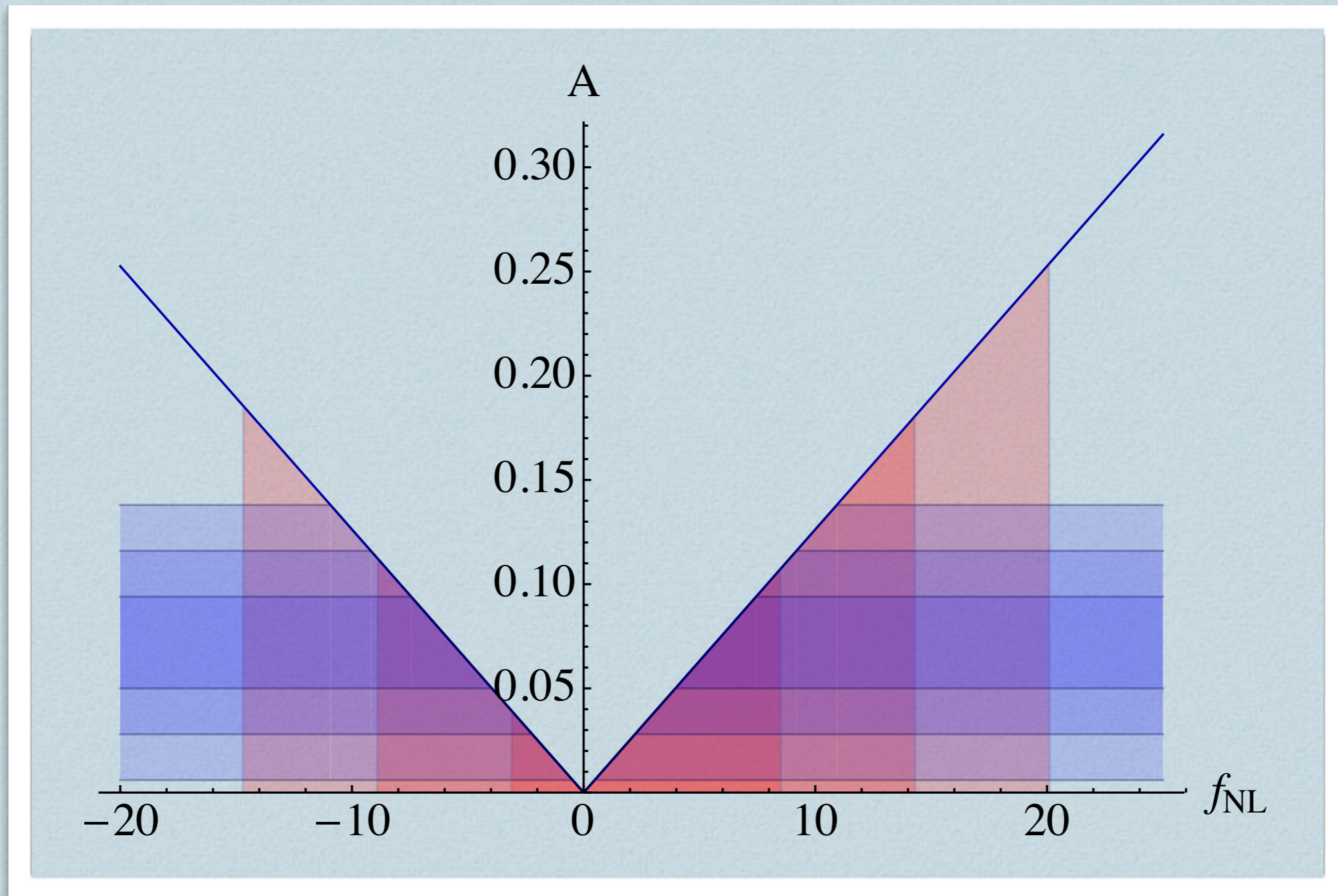
$A = 0.07$

$f_{\text{NL}} = 7$

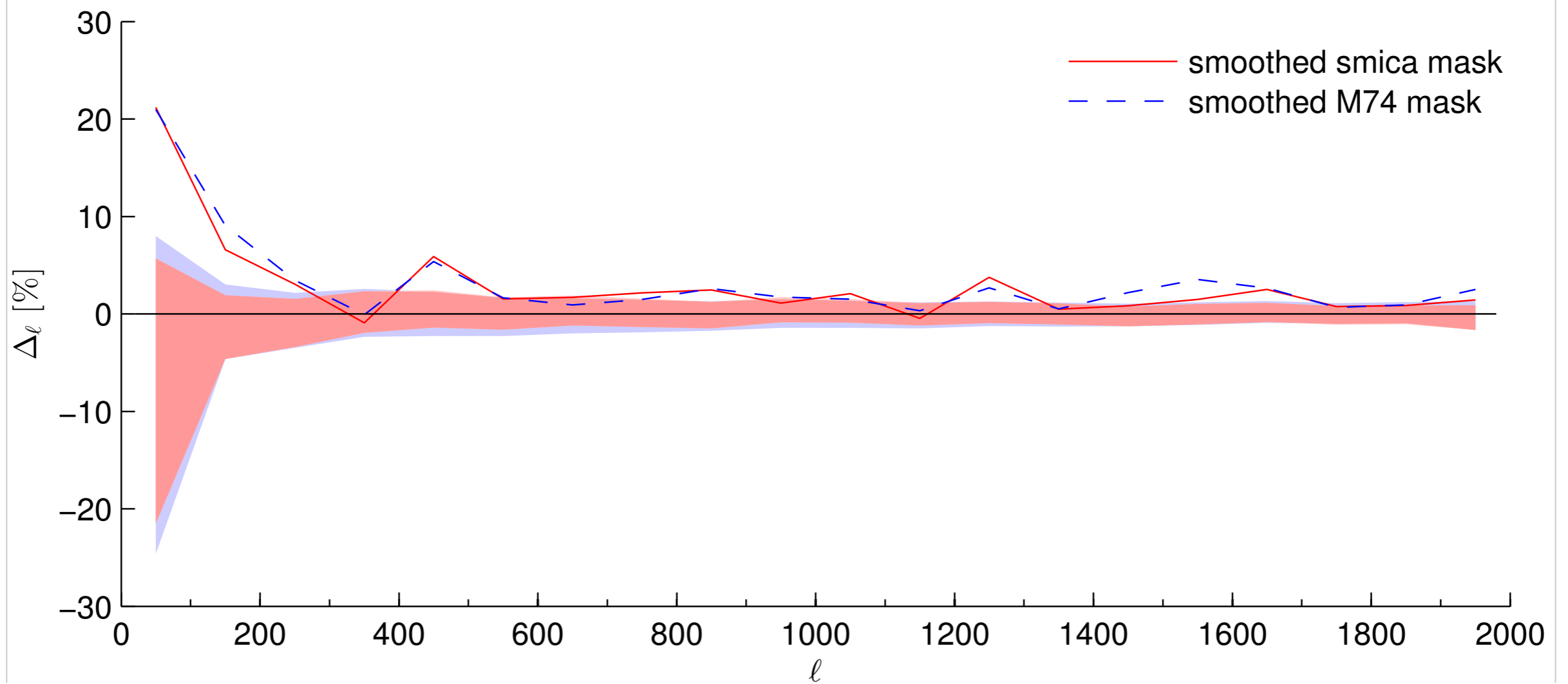
```
graph LR; m2["m^2 = (e^{2N_m} - 1)2H^2"] --> A["A = 0.07"]; Nm["N_m = 1.4"] --> A; N["N_* - 4.2 < N < N_* - 2.4"] --> A; A --> fNL["f_NL = 7"];
```

- ✓ No dipole asymmetry from small scales
- ✓ No excessive quadrupoles and octupoles

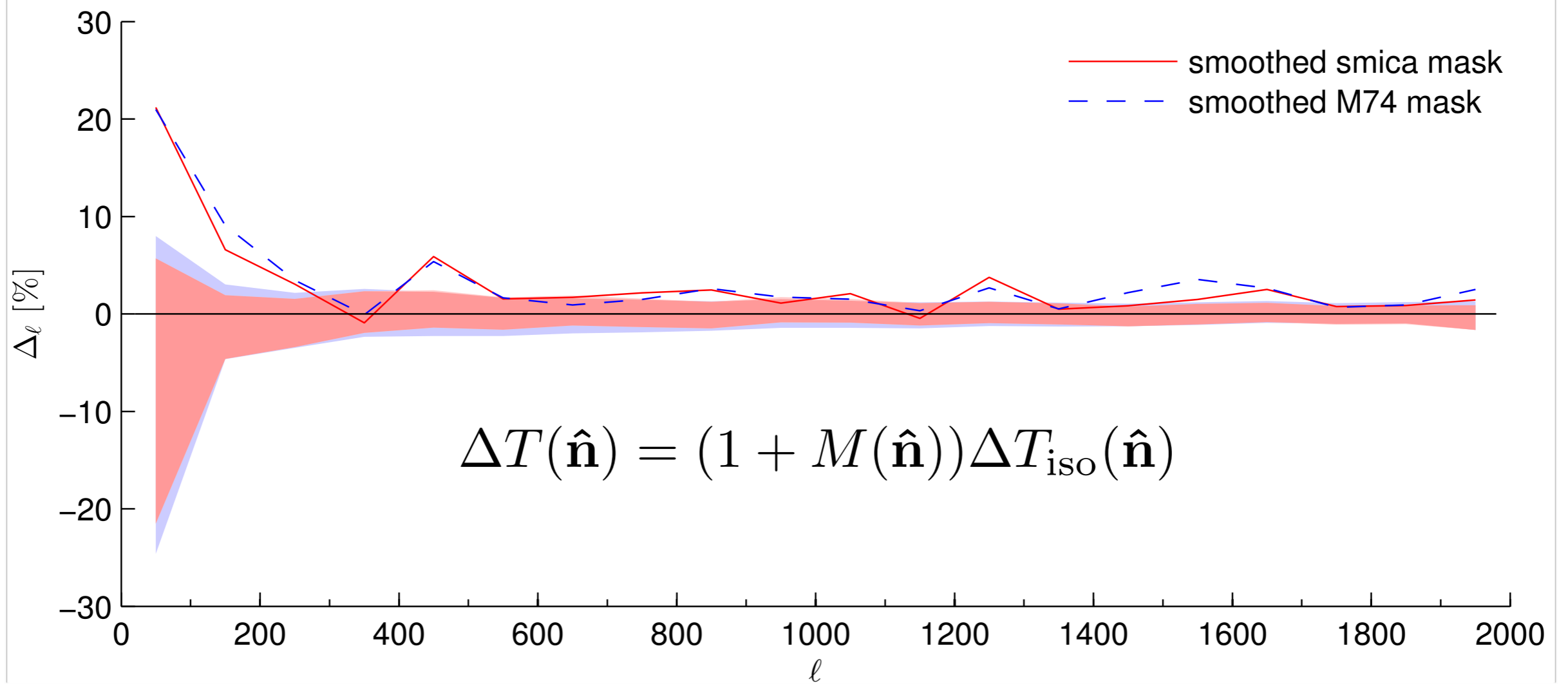
Parameter space for fast roll



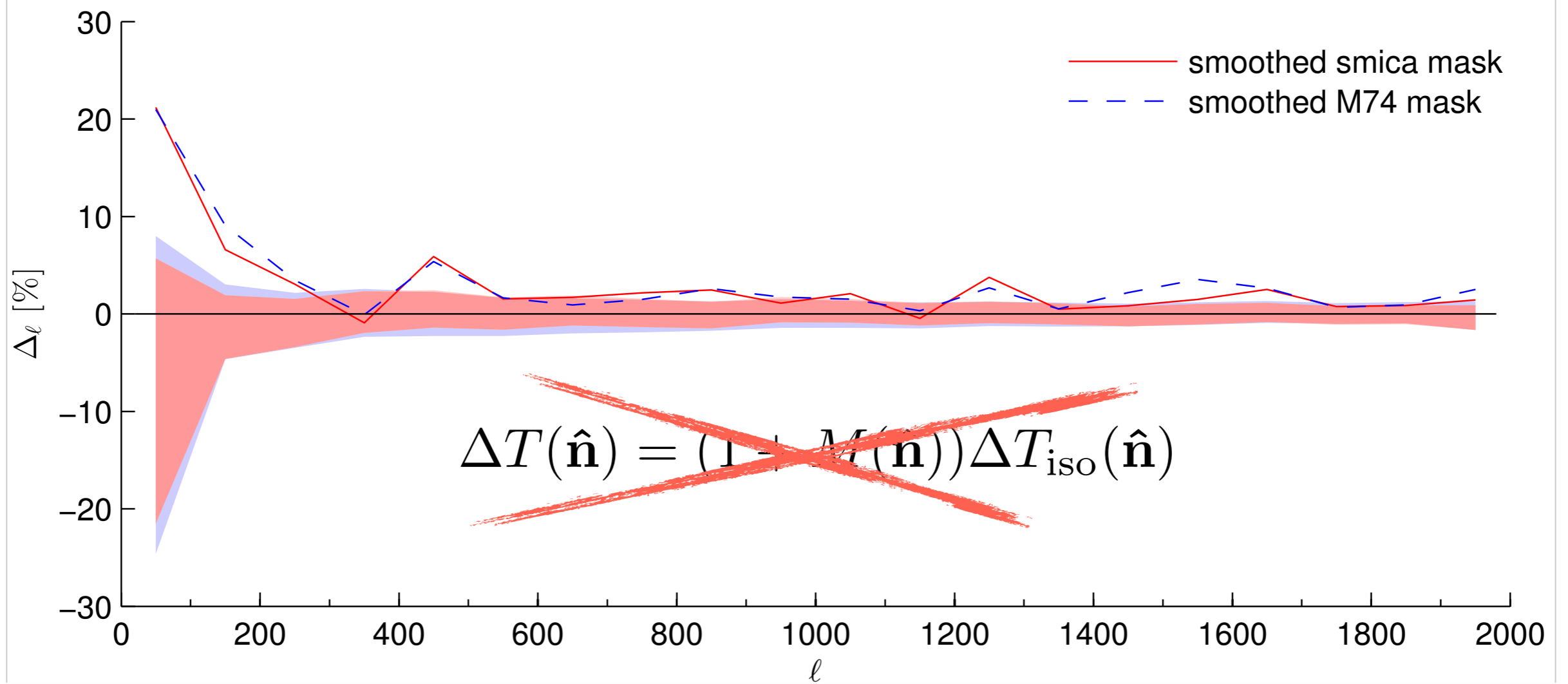
Scale dependence



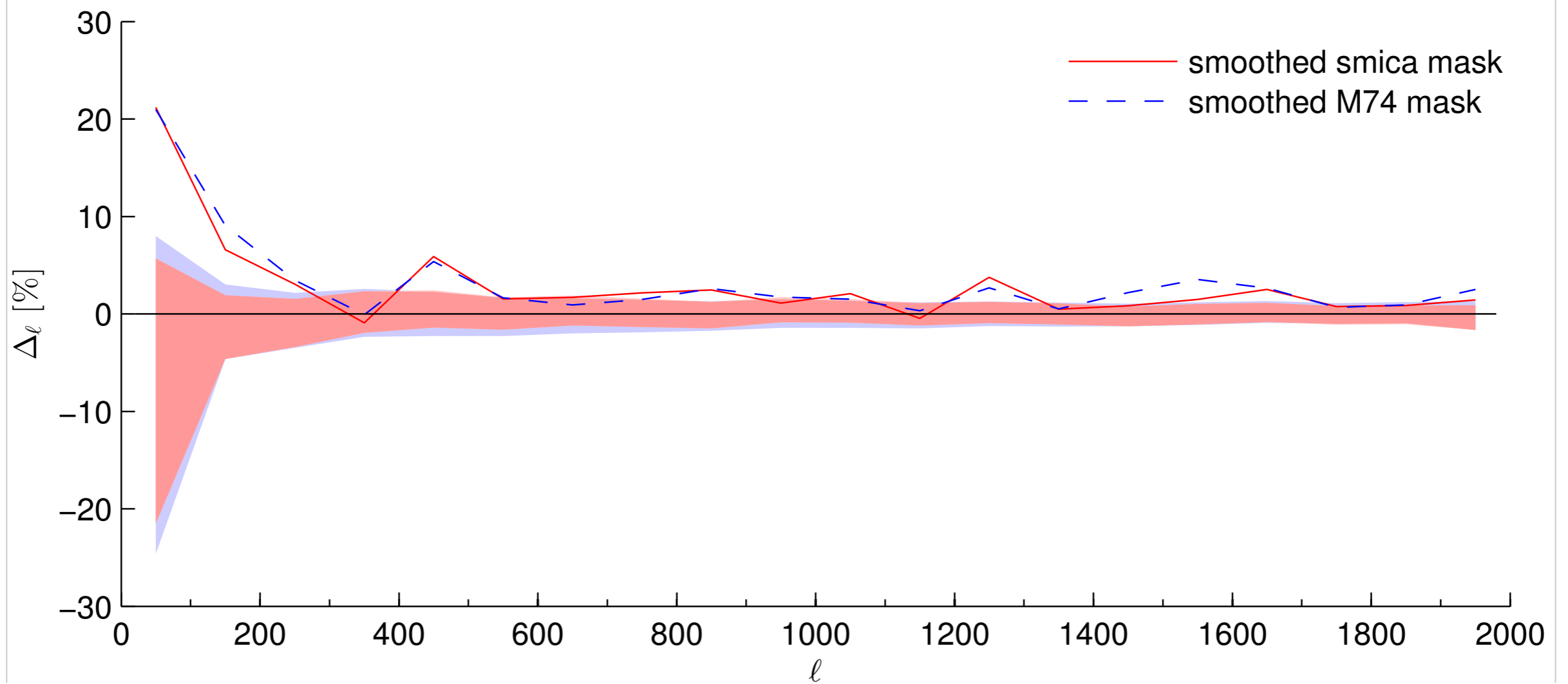
Scale dependence



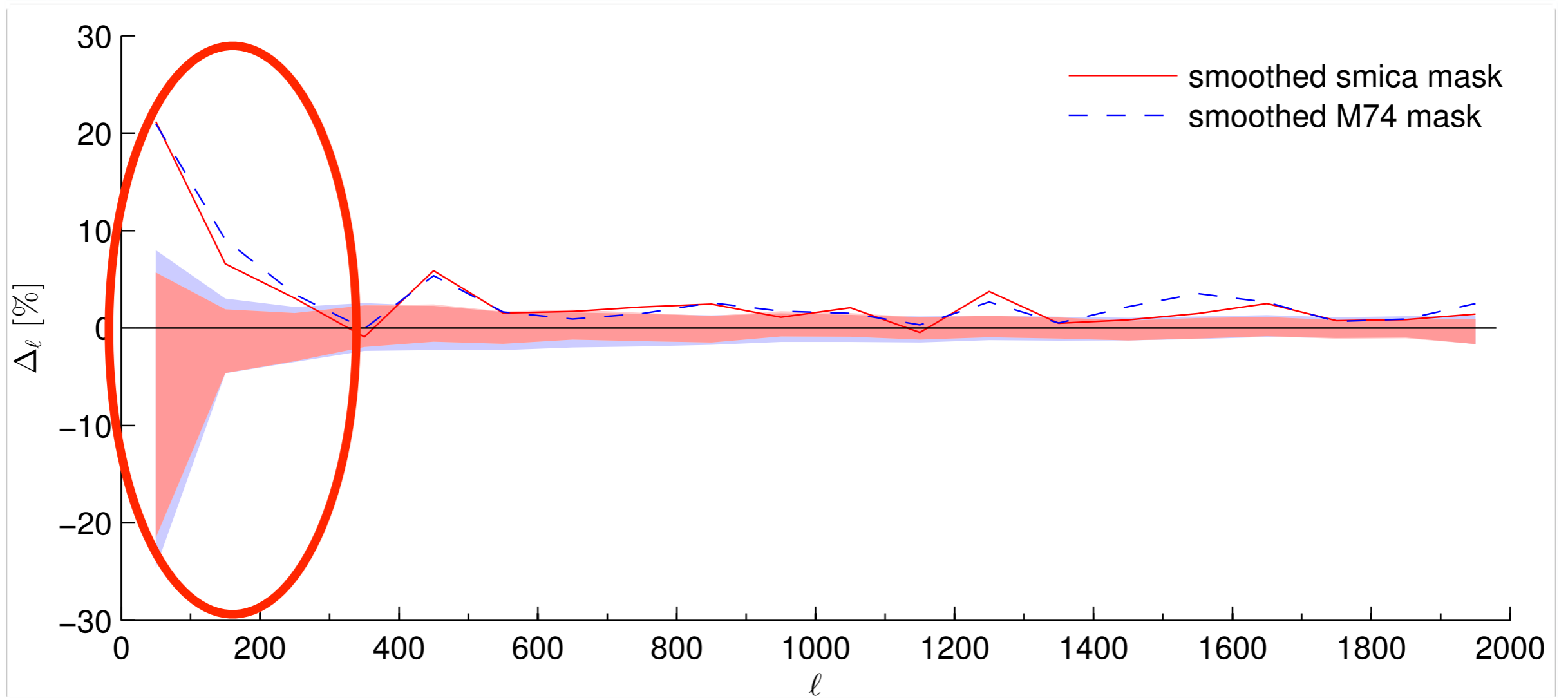
Scale dependence



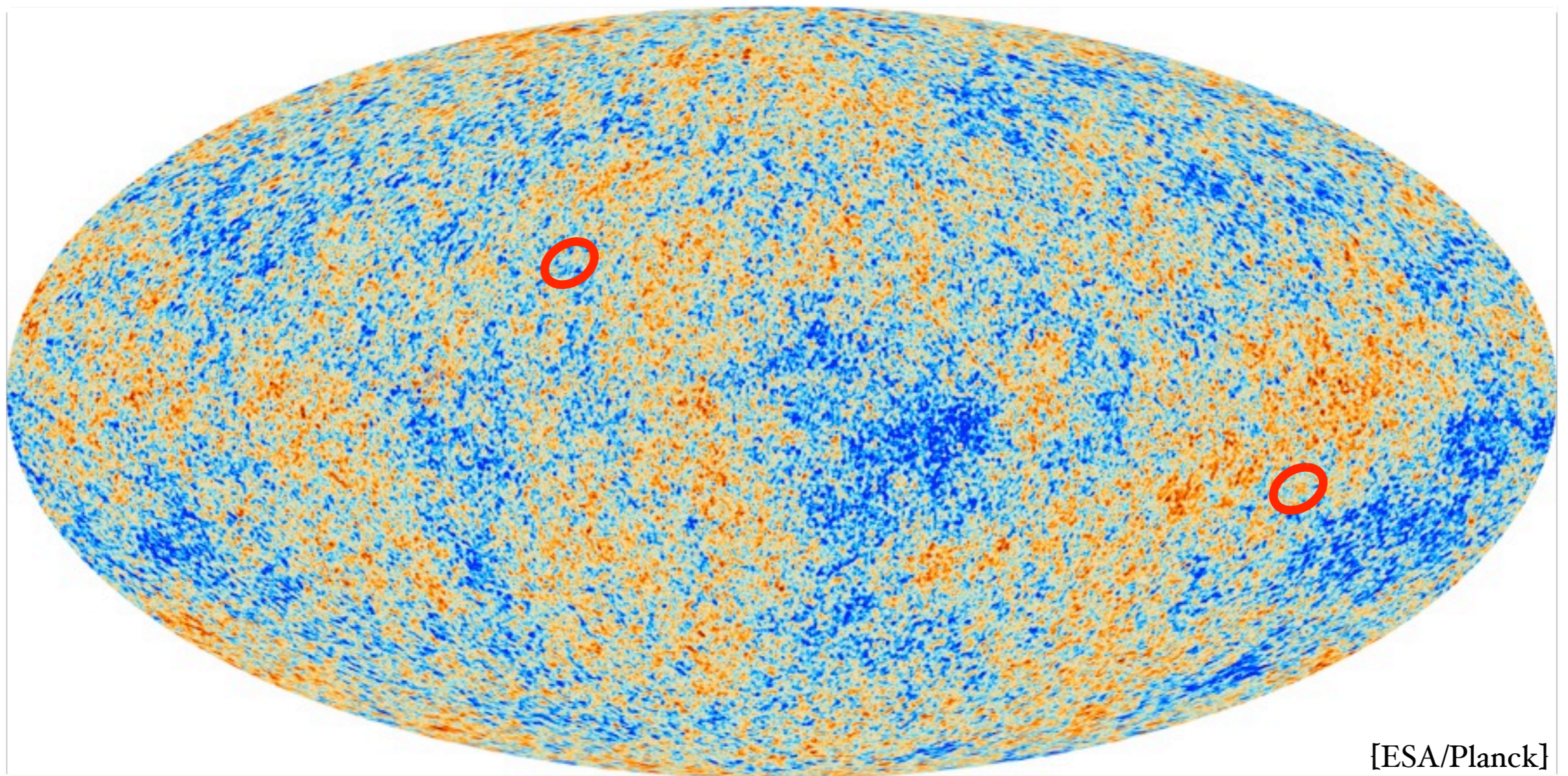
Scale dependence



Scale dependence

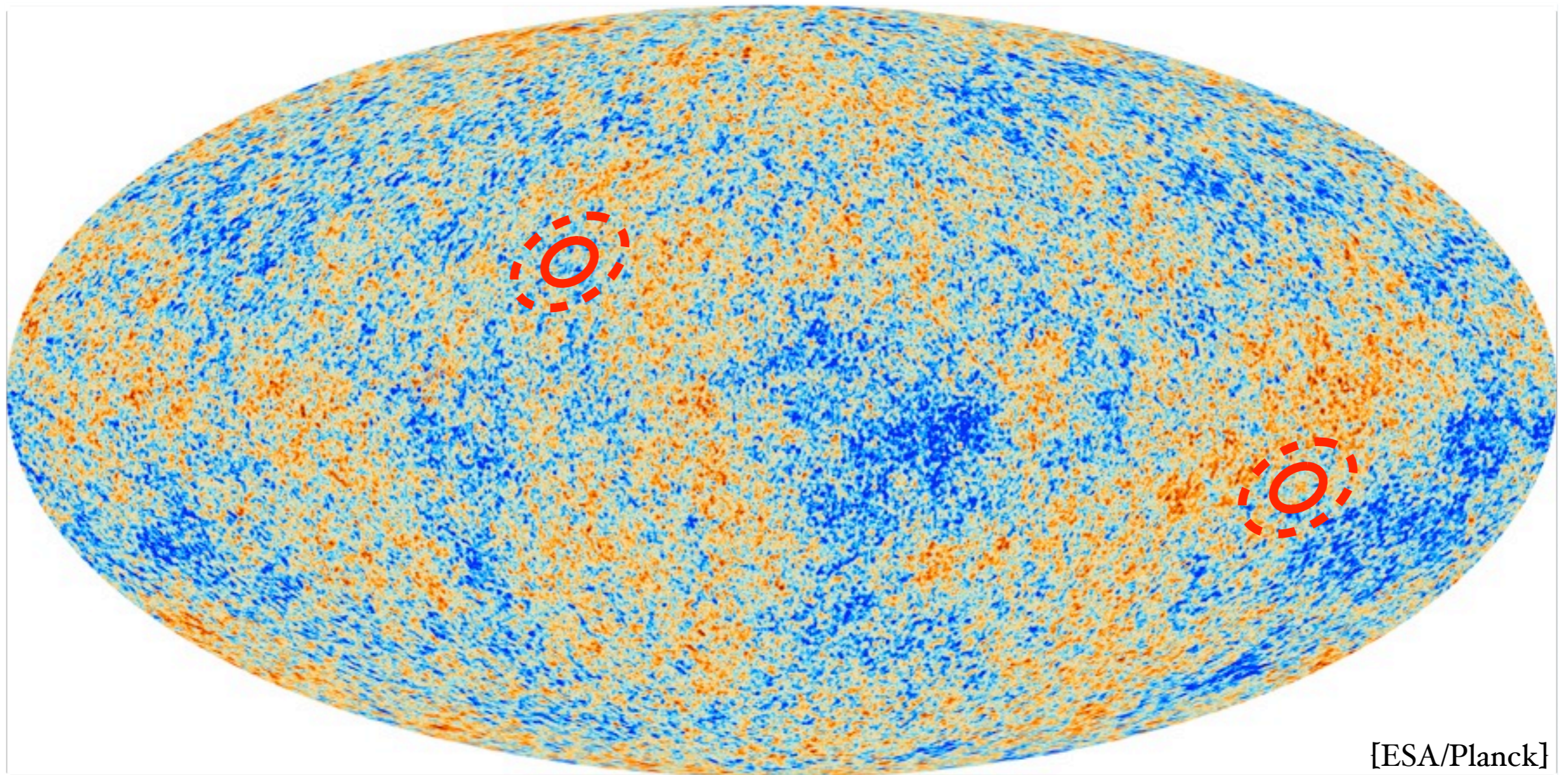


How significant?



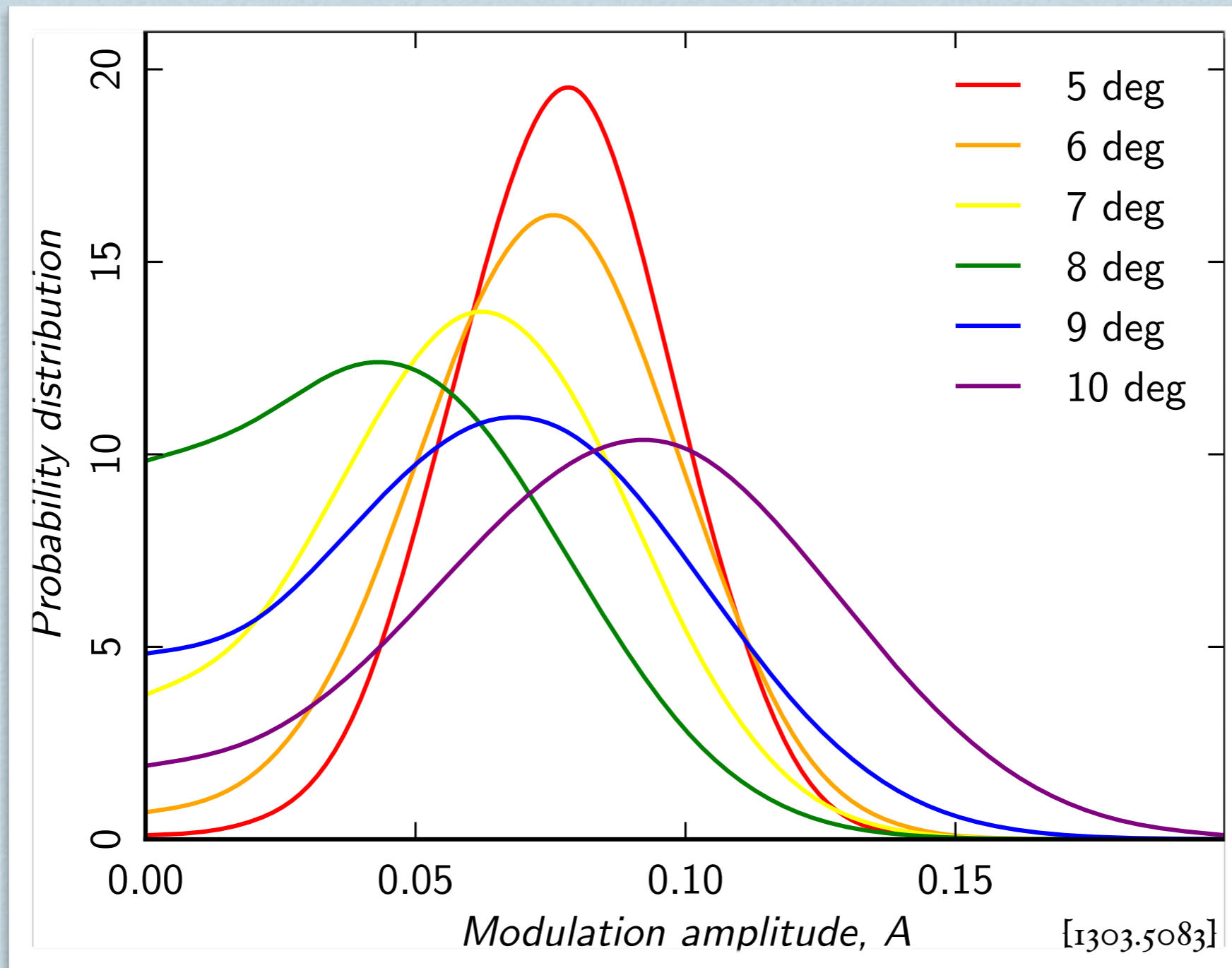
[ESA/Planck]

How significant?



[ESA/Planck]

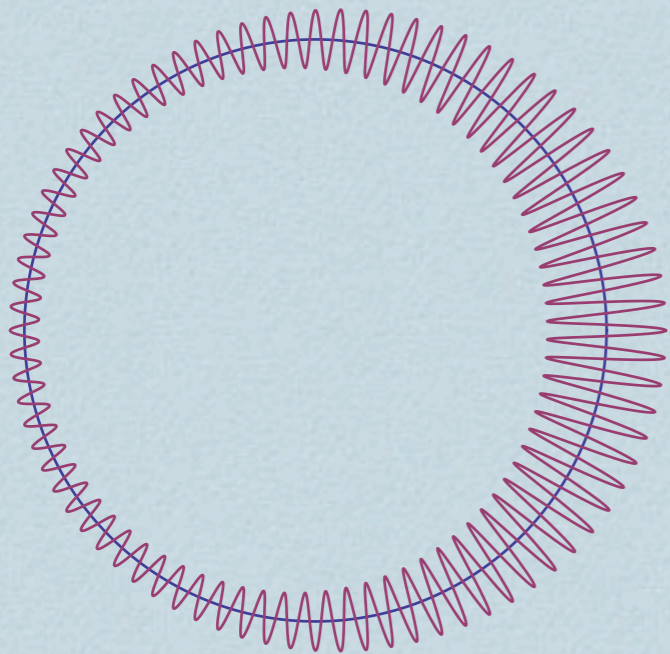
Not so significant?



Over estimate

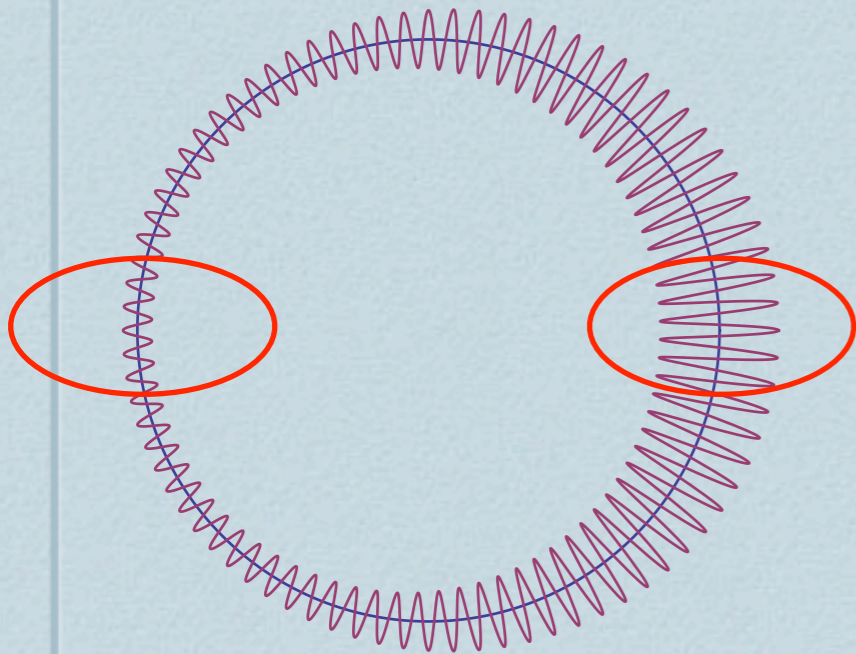
$$\Delta T(\hat{\mathbf{n}}) = (1 + A \hat{\mathbf{p}} \cdot \hat{\mathbf{n}}) \Delta T_{\text{iso}}(\hat{\mathbf{n}})$$

Over estimate



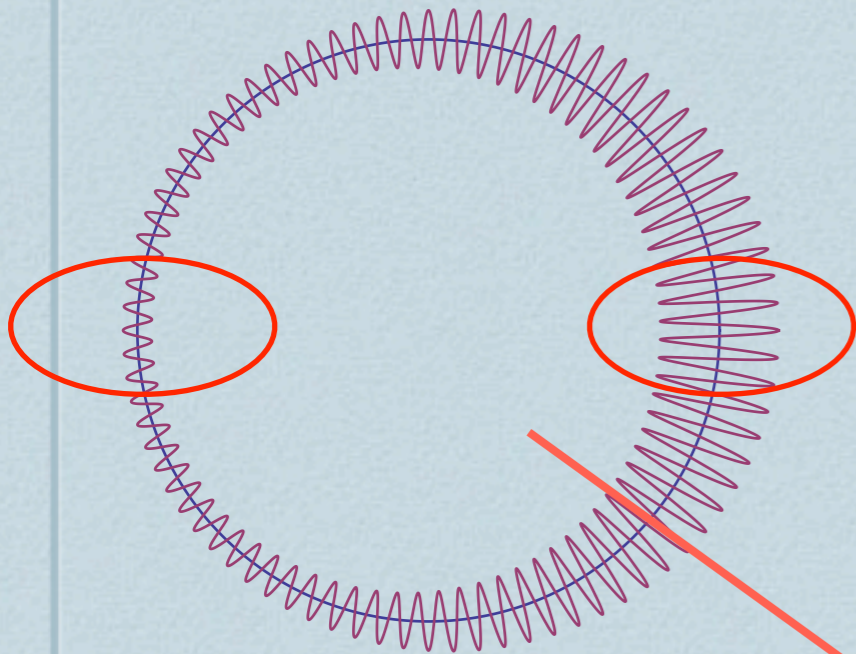
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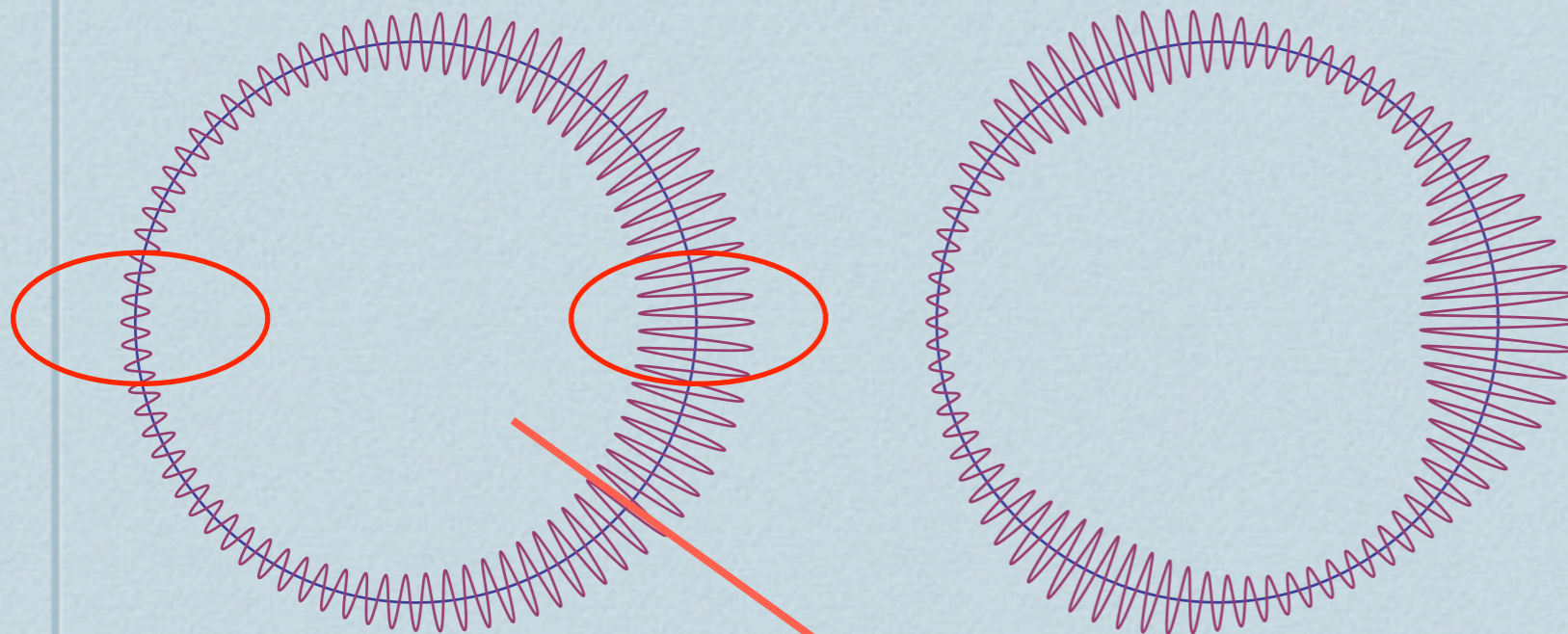
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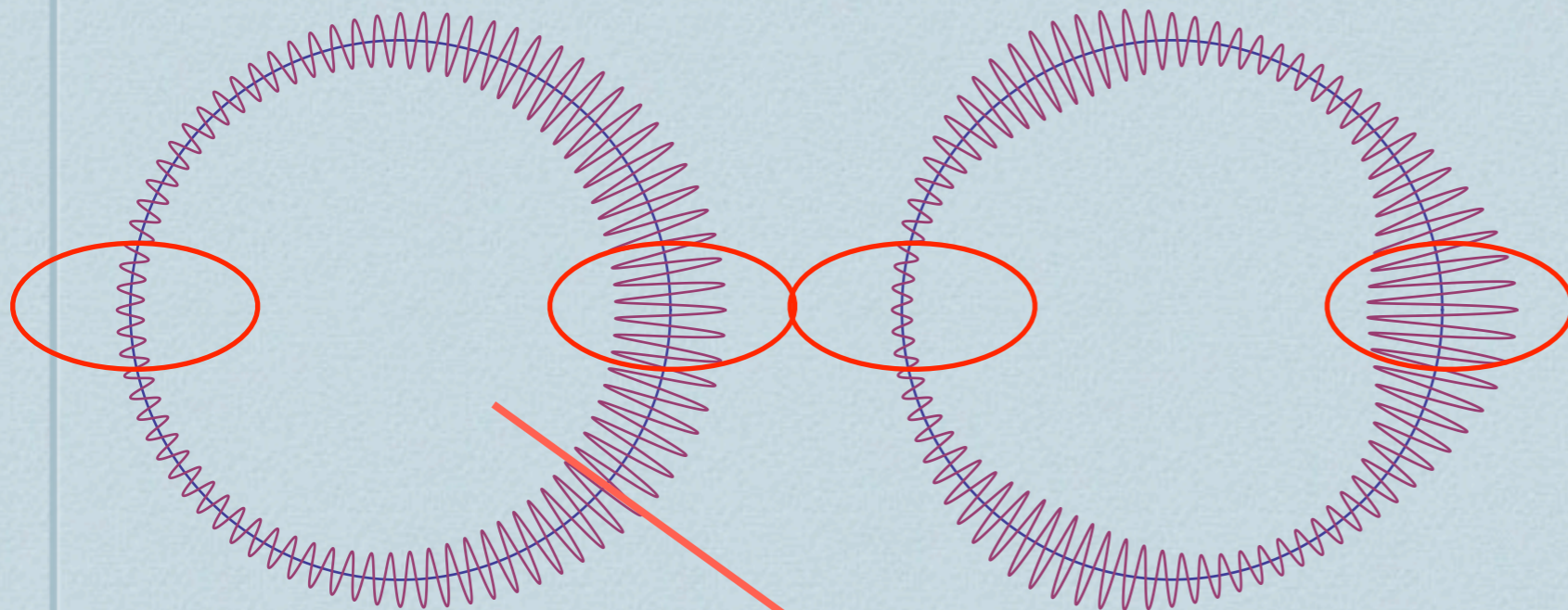
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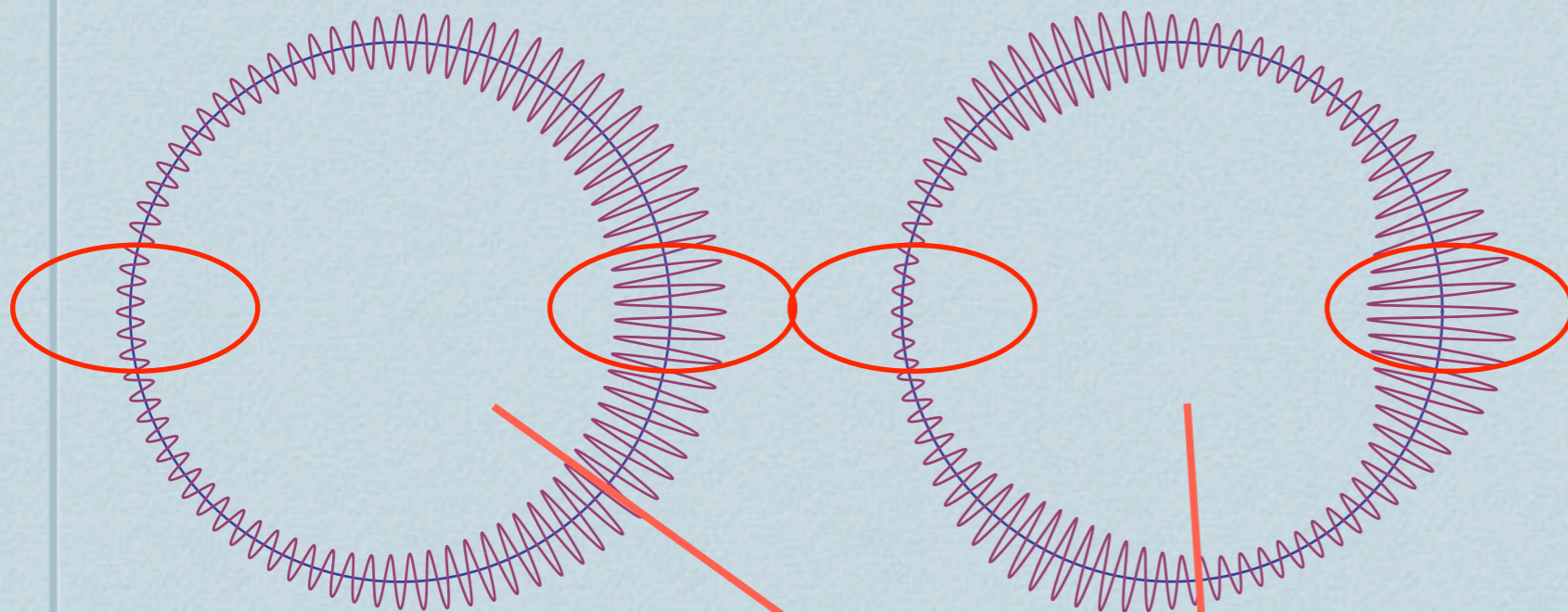
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Over estimate



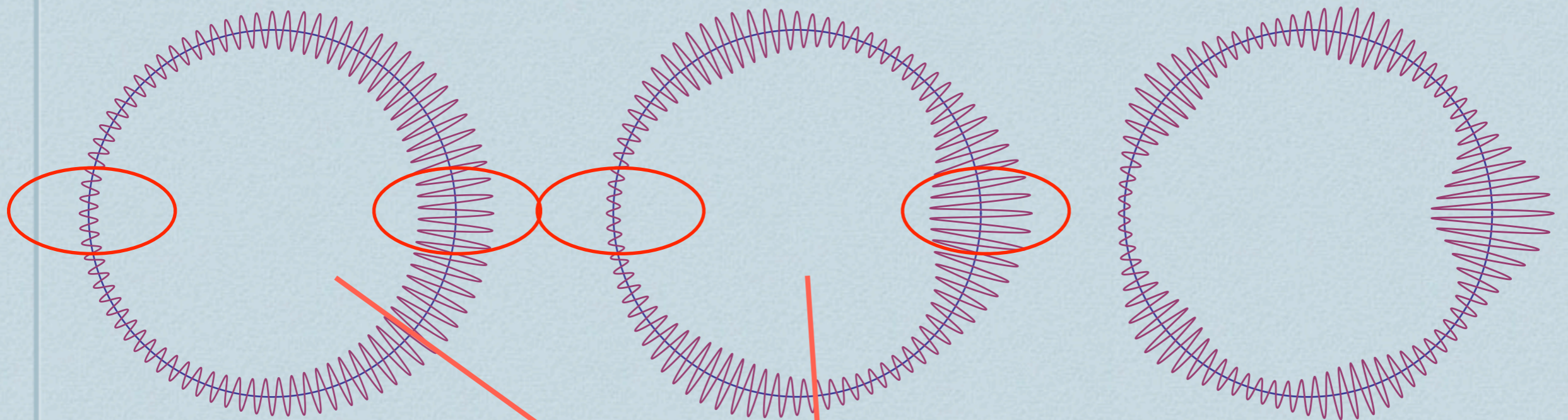
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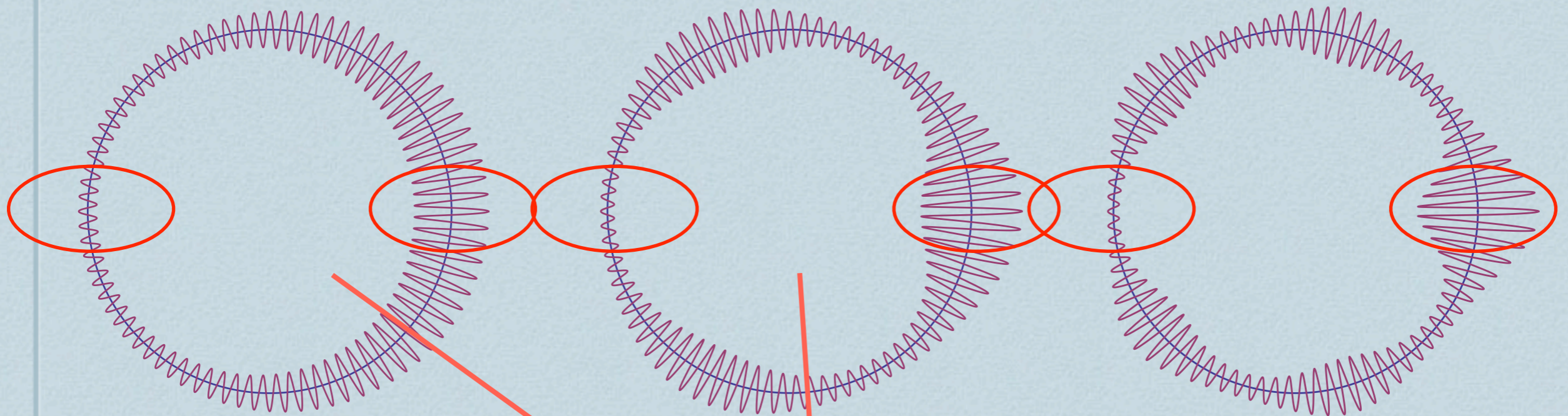
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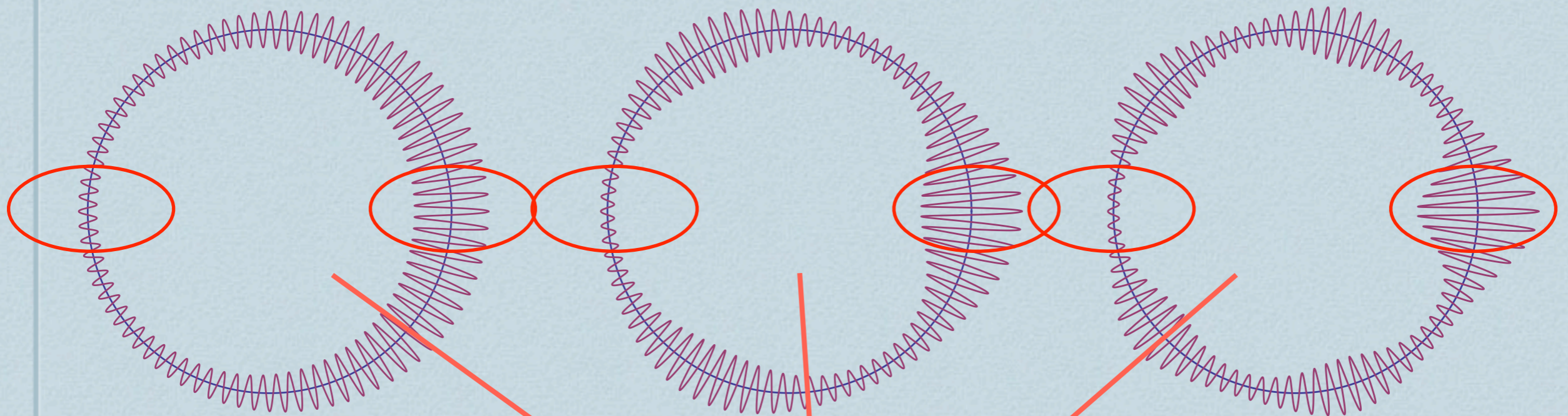
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Over estimate



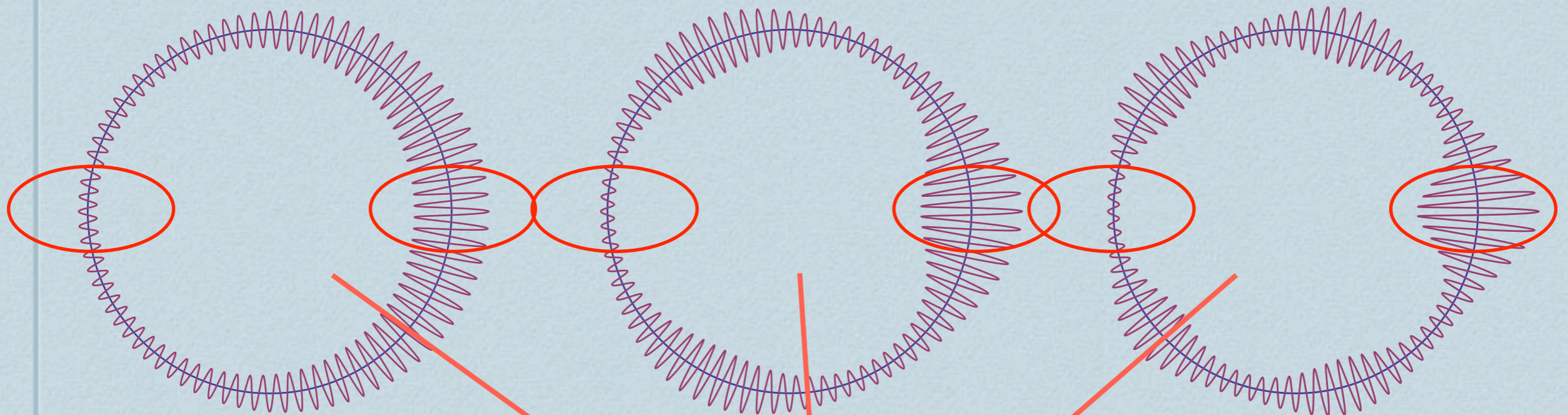
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Over estimate



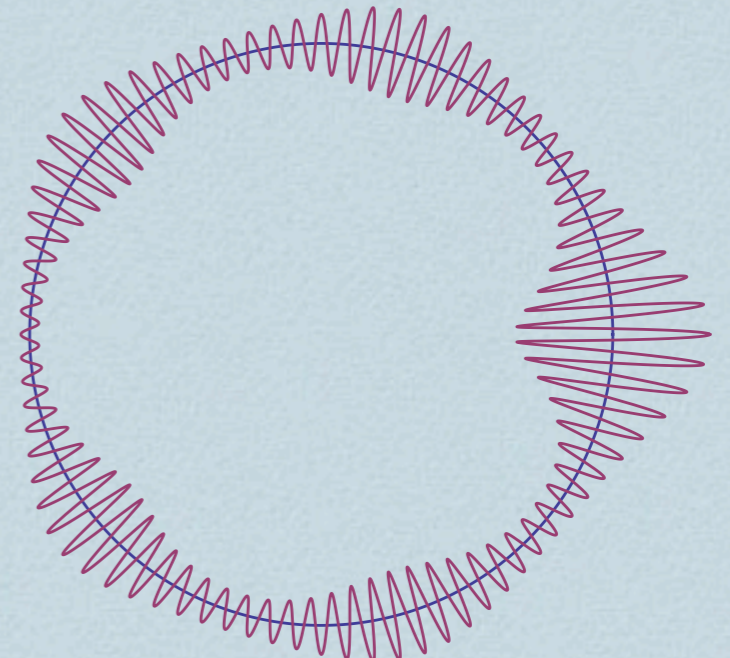
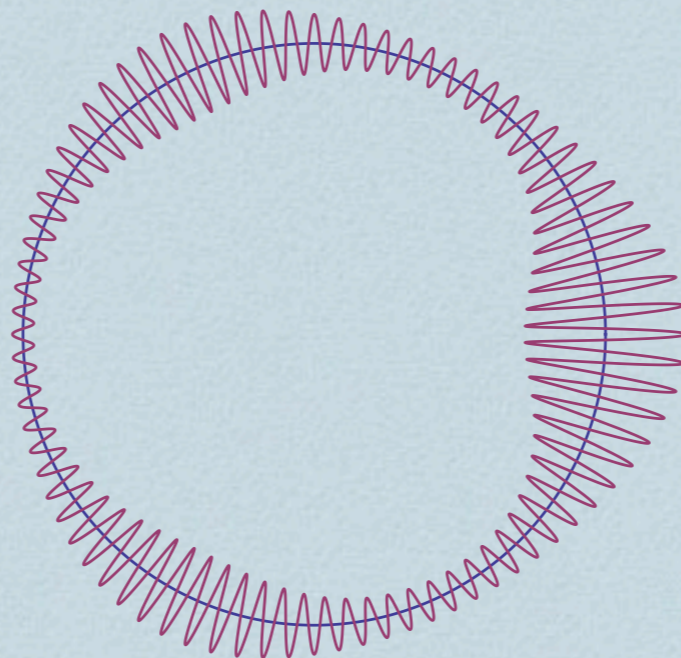
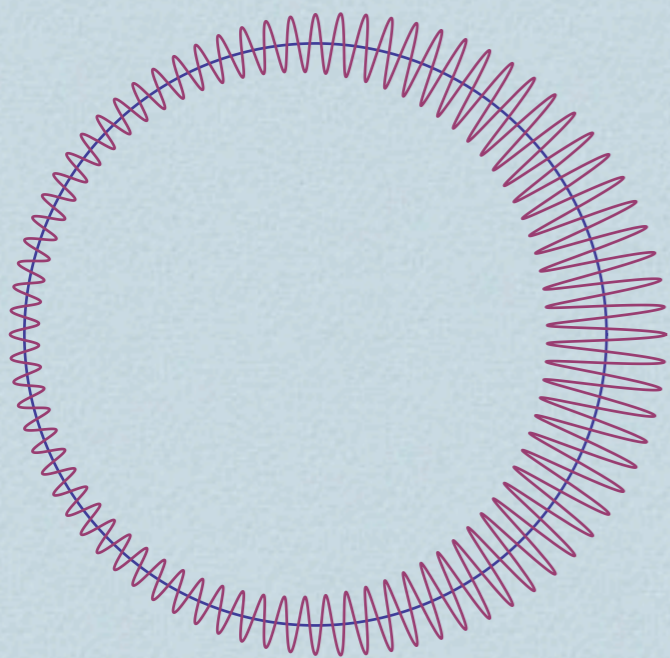
$$\Delta T(\hat{\mathbf{n}}) = (1 + A \hat{\mathbf{p}} \cdot \hat{\mathbf{n}}) \Delta T_{\text{iso}}(\hat{\mathbf{n}})$$

Over estimate

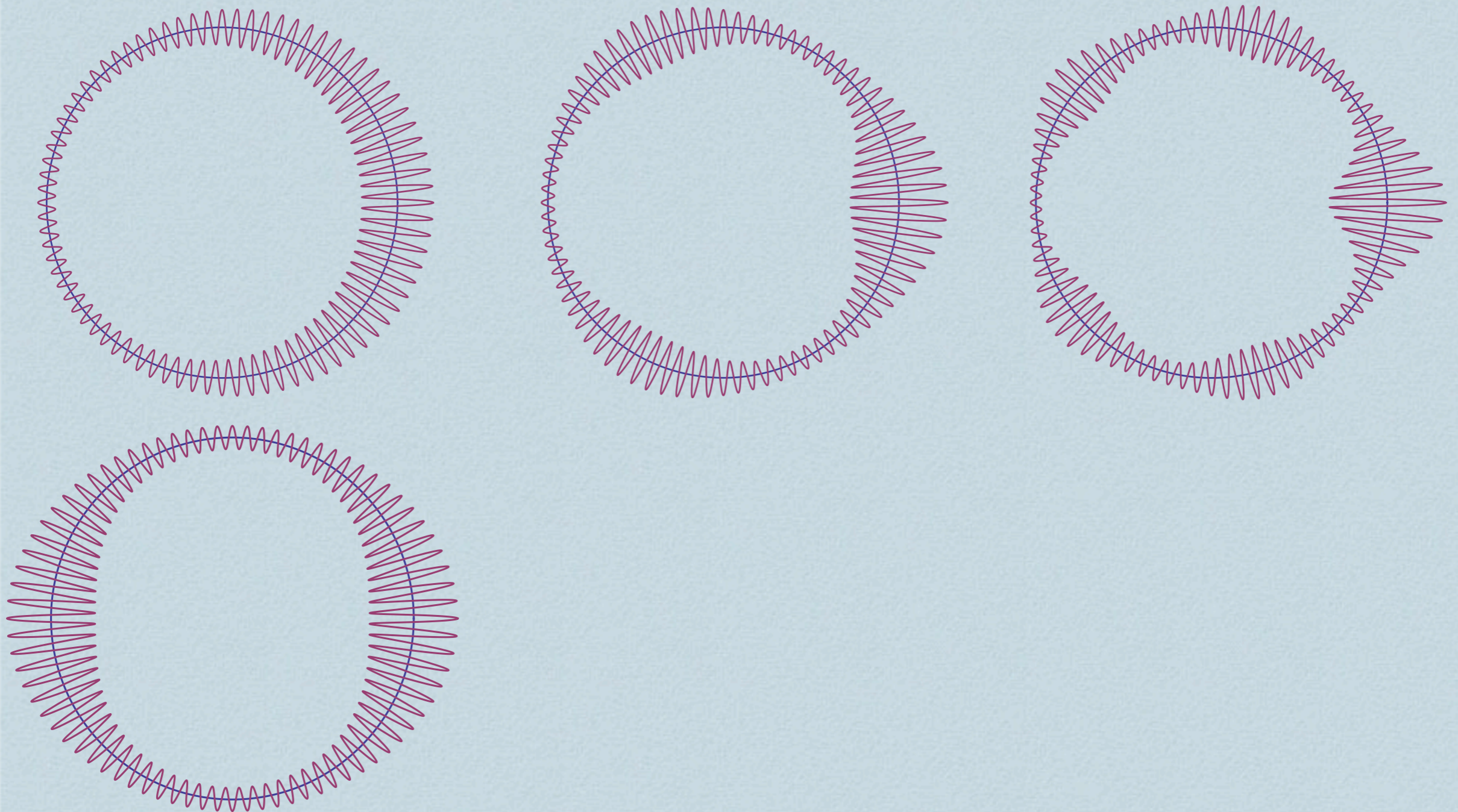


$$\Delta T(\hat{\mathbf{n}}) = (1 + 4\hat{\mathbf{p}} \cdot \hat{\mathbf{n}}) \Delta T_{\text{iso}}(\hat{\mathbf{n}})$$

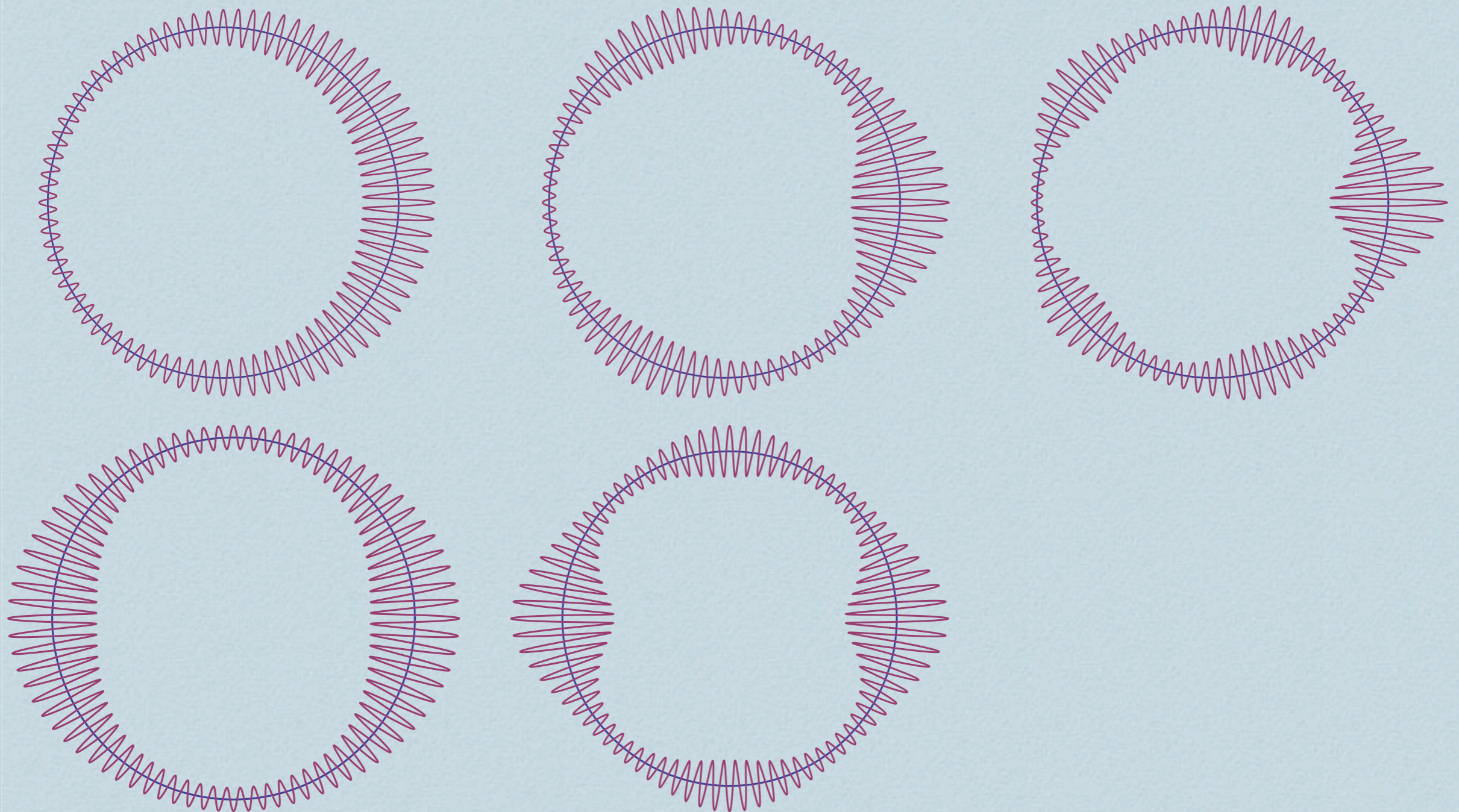
Other multipoles



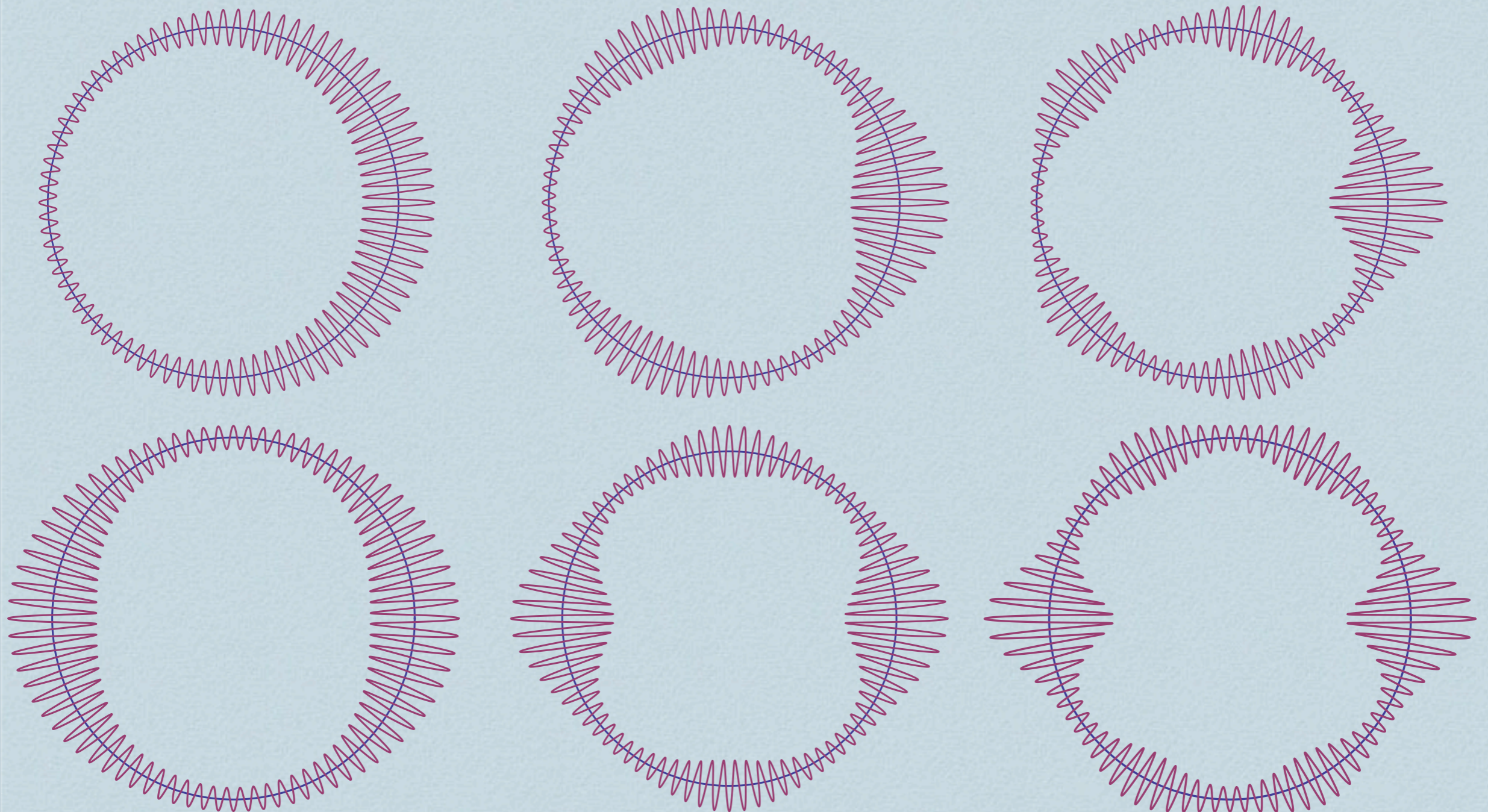
Other multipoles



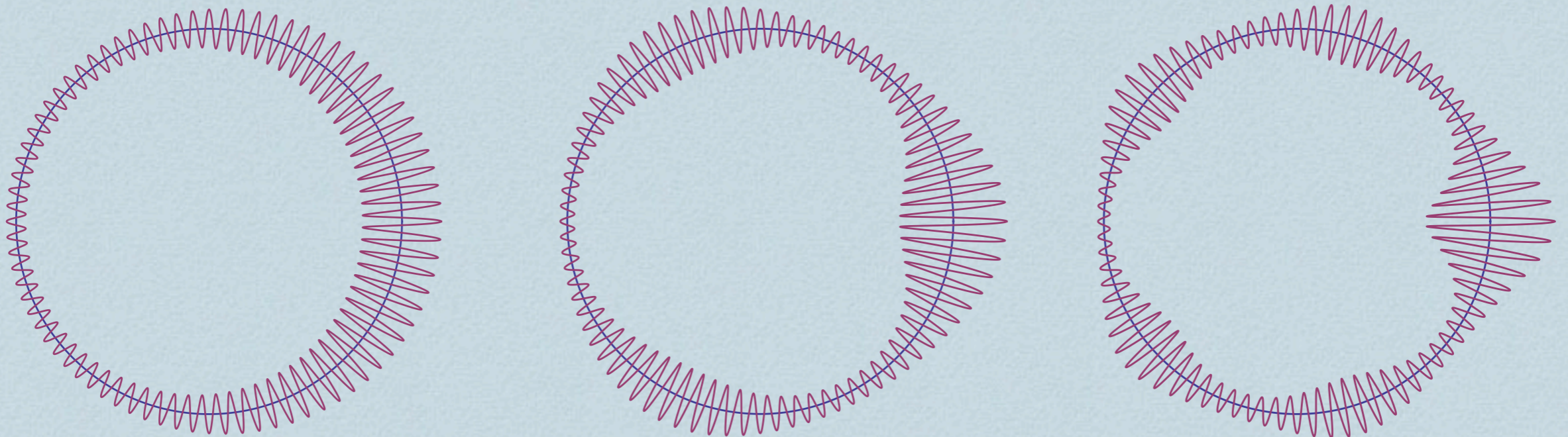
Other multipoles



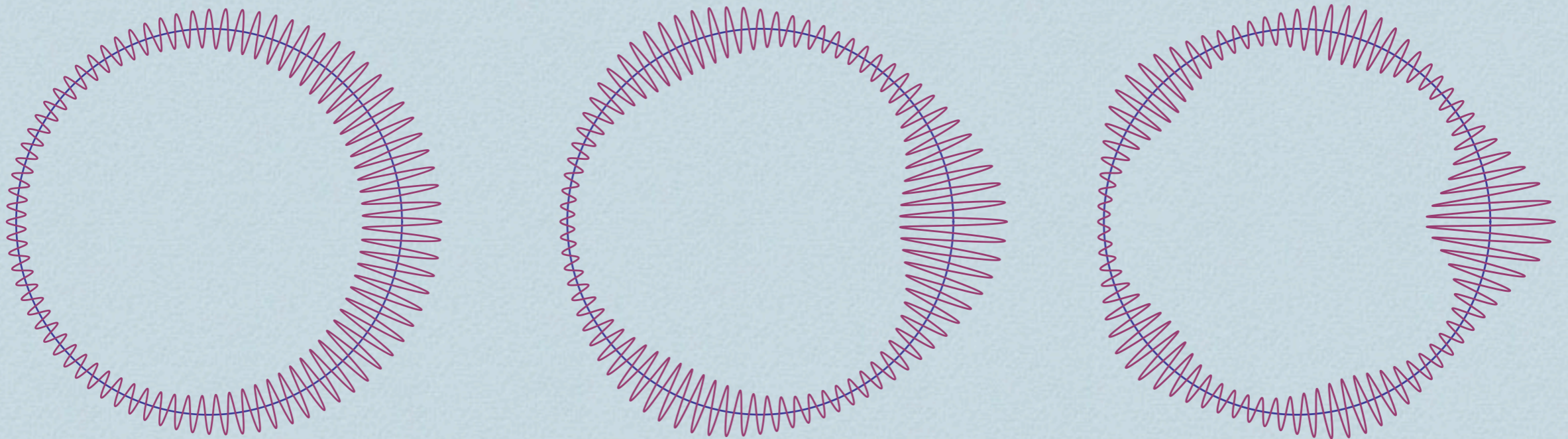
Other multipoles



CMB power multipole

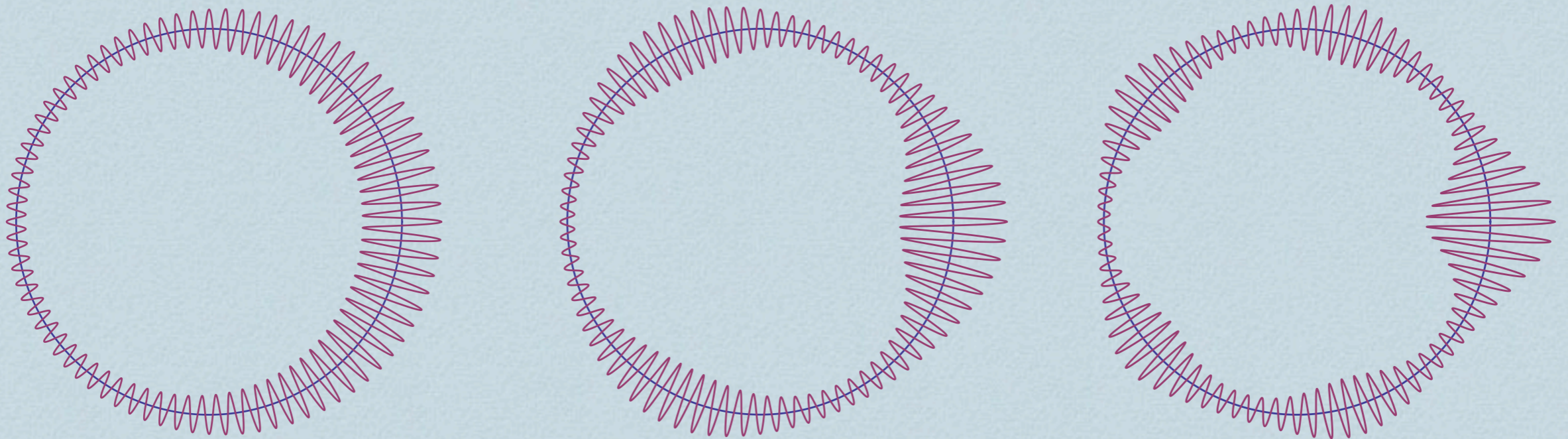


CMB power multipole



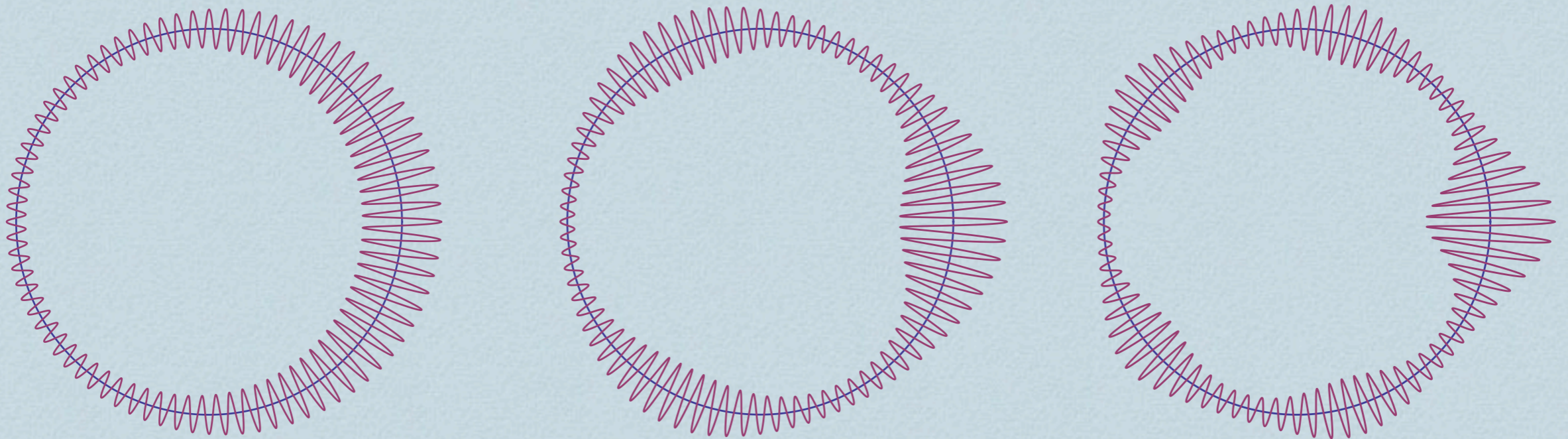
$$\Delta T(\hat{\mathbf{n}}) = \sum_{lm} a_{lm} Y_{lm}(\hat{\mathbf{n}})$$

CMB power multipole



$$\Delta T^2(\hat{\mathbf{n}}) = \sum_{lm} a_{lm}^{(2)} Y_{lm}(\hat{\mathbf{n}})$$

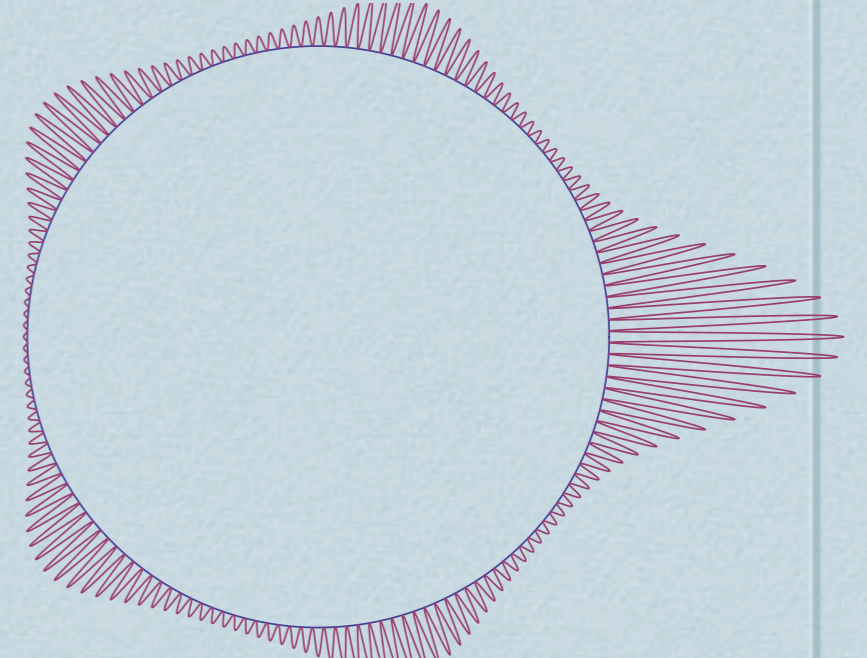
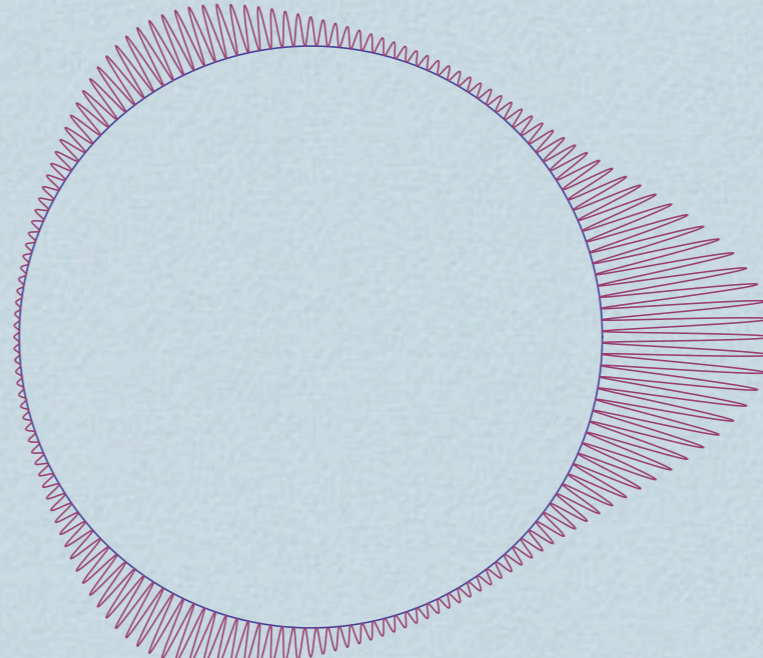
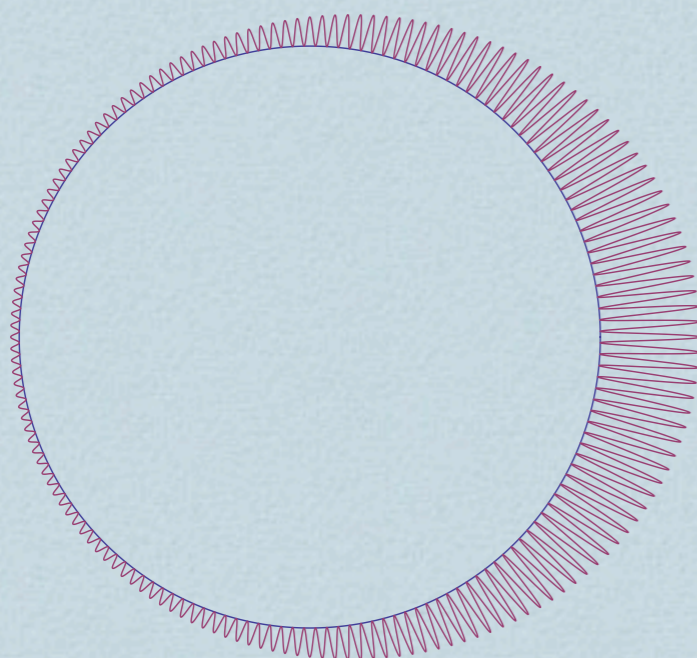
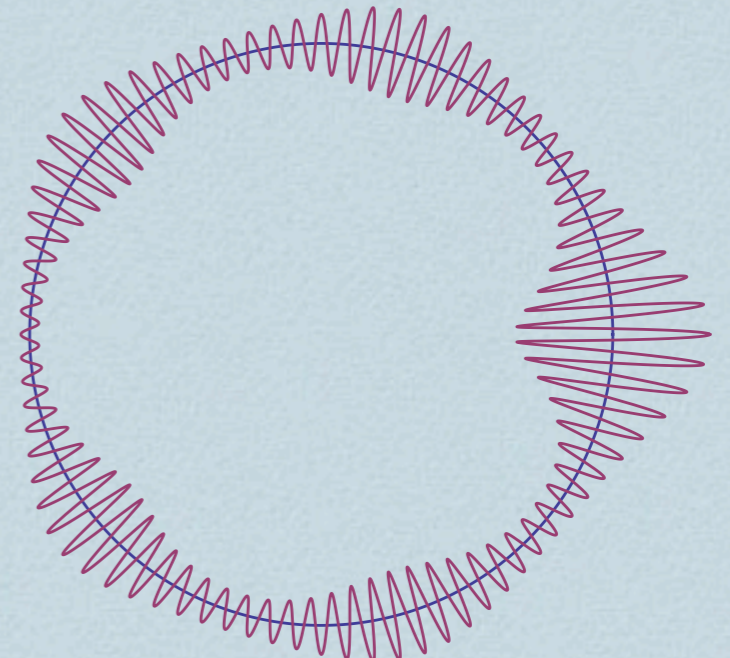
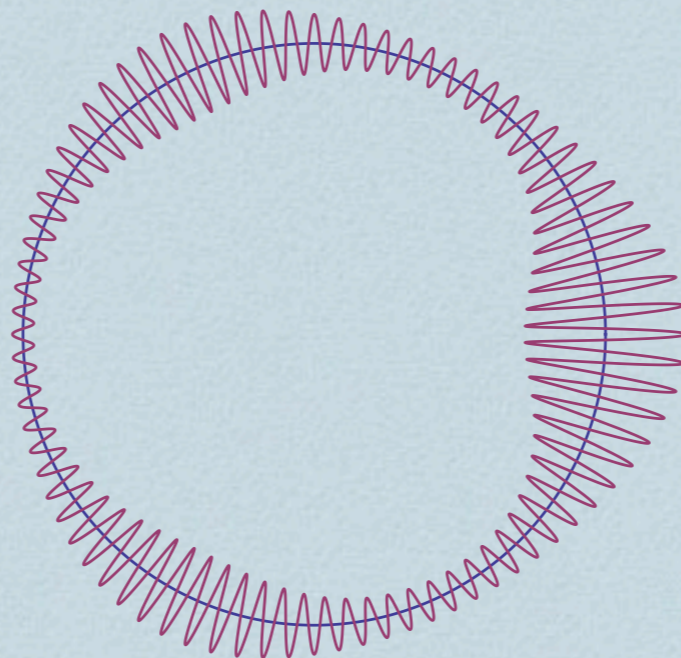
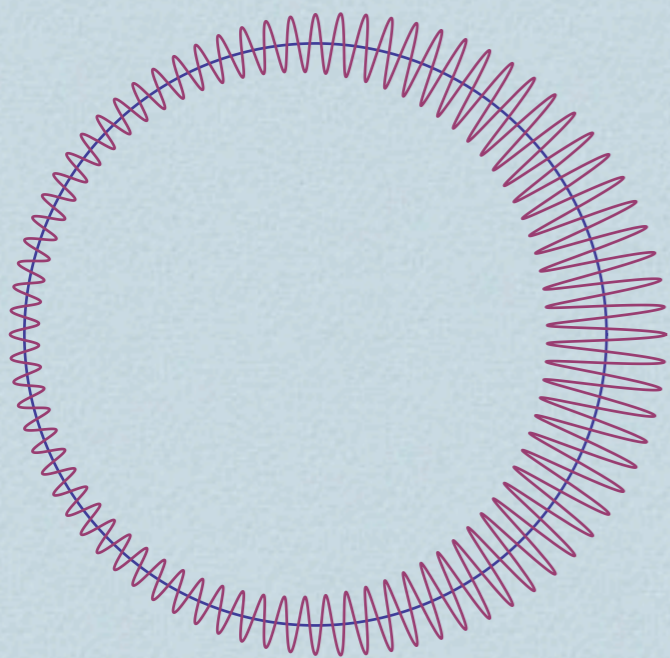
CMB power multipole



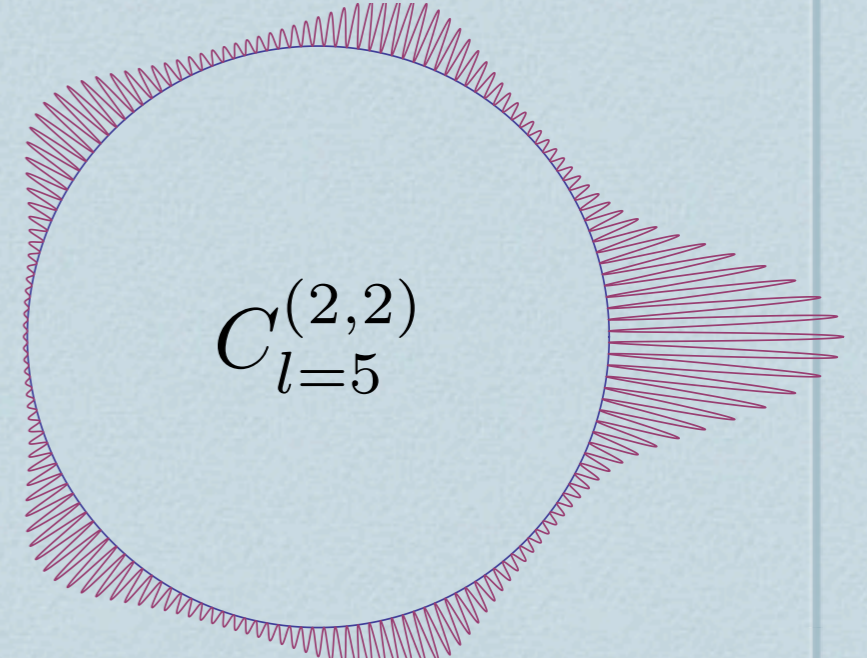
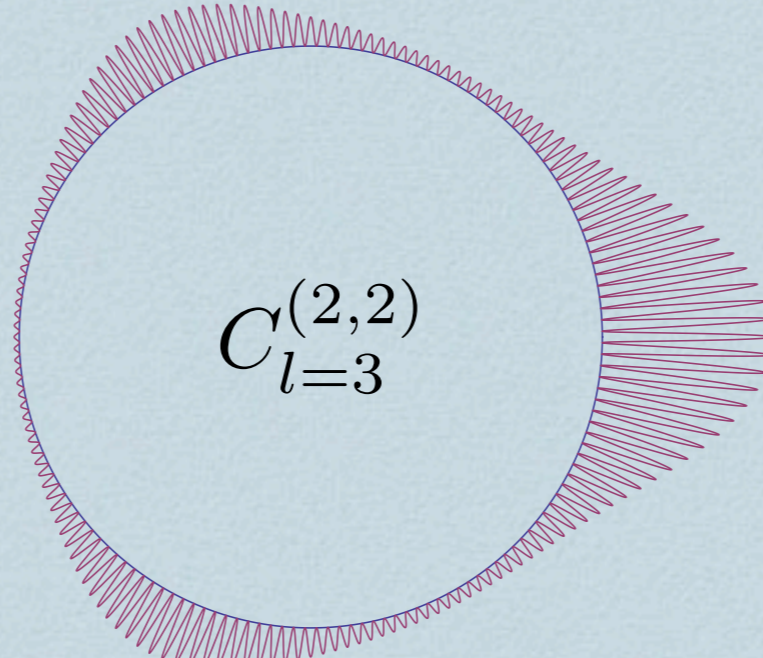
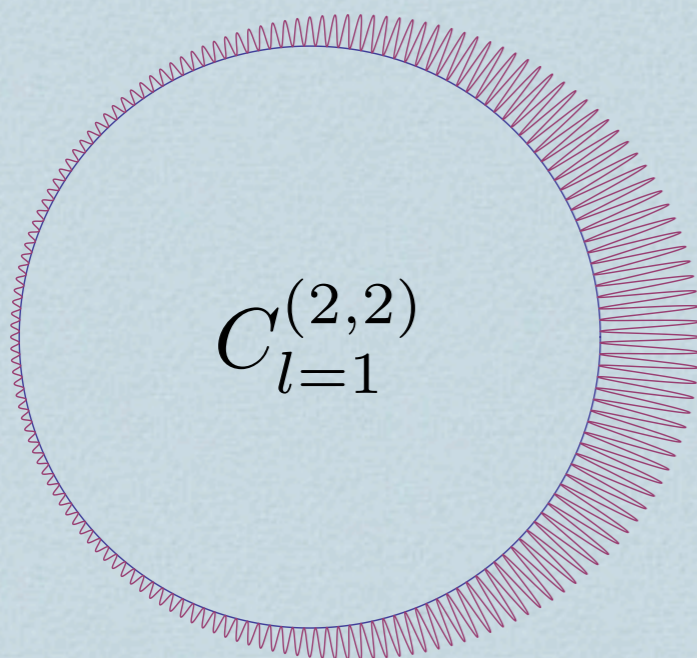
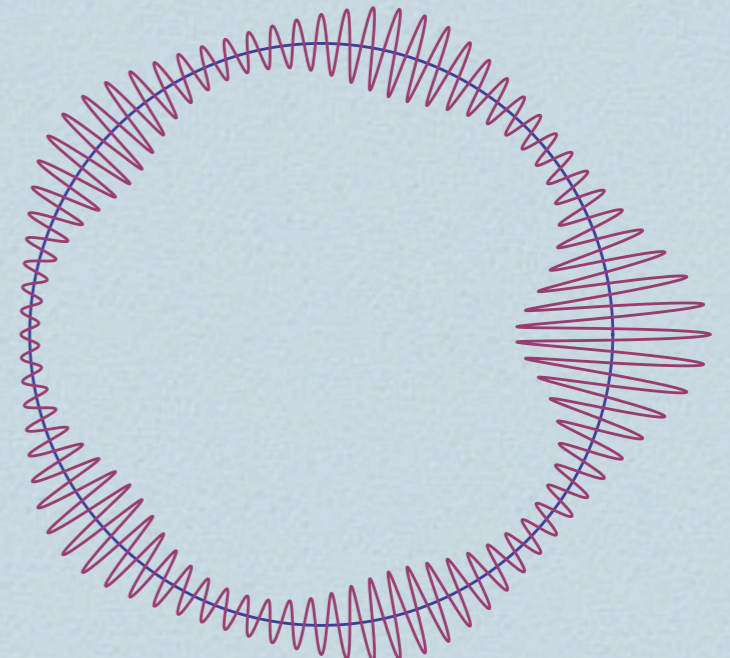
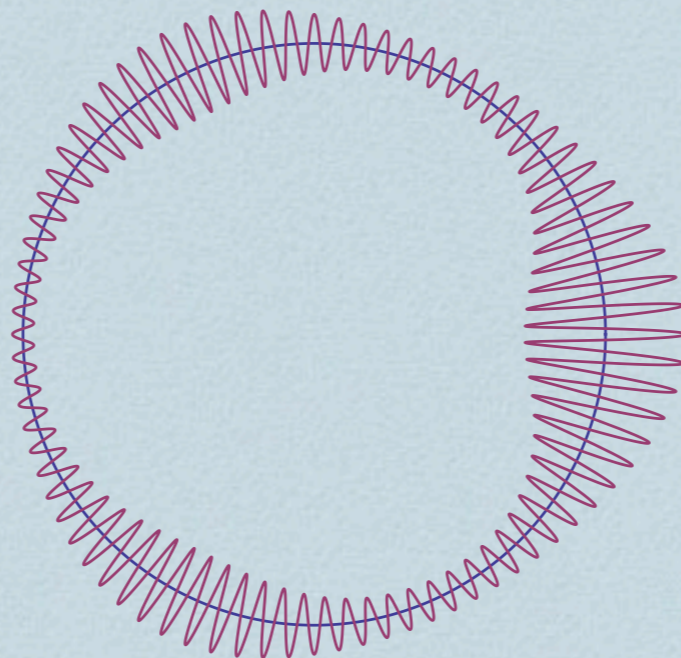
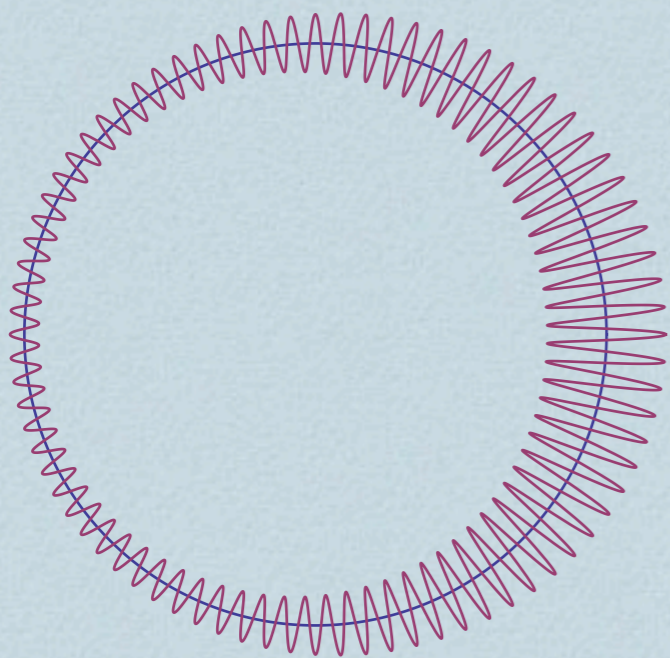
$$\Delta T^2(\hat{\mathbf{n}}) = \sum_{lm} a_{lm}^{(2)} Y_{lm}(\hat{\mathbf{n}})$$

$$\langle a_{lm}^{(2)*} a_{l'm'}^{(2)} \rangle = C_l^{(2,2)} \delta_{ll'} \delta_{mm'}$$

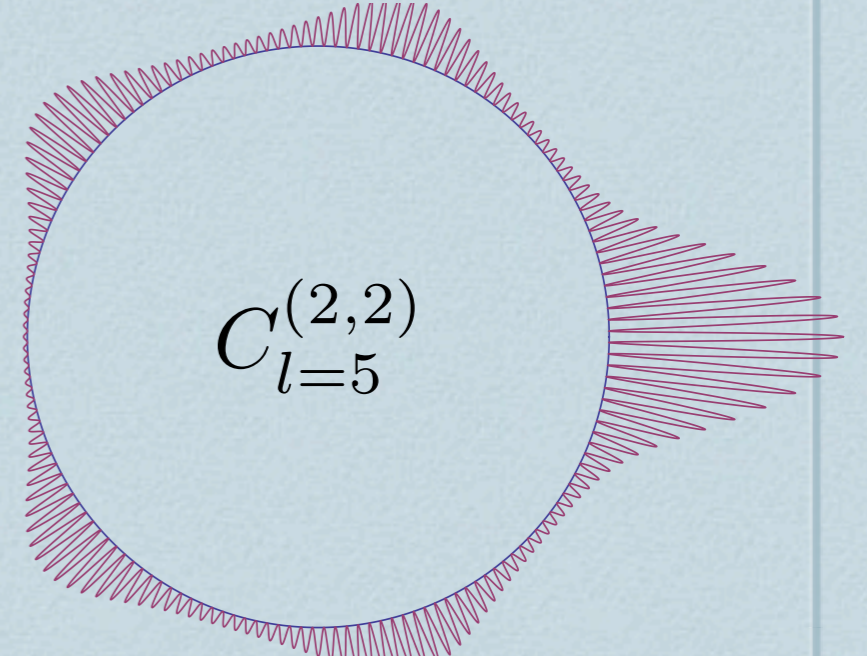
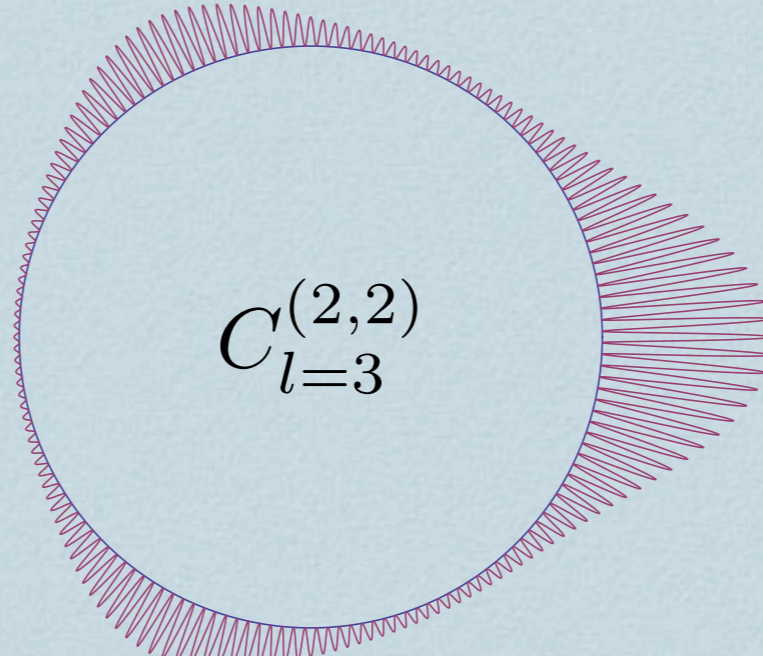
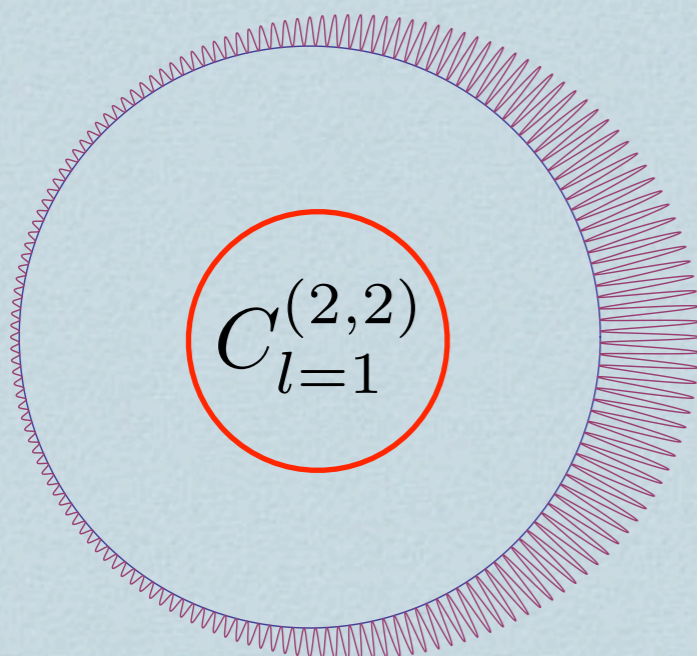
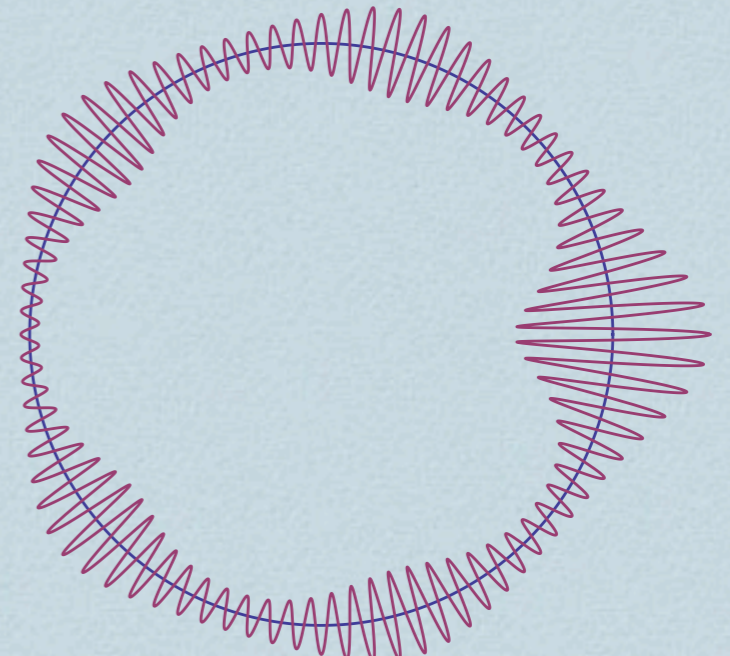
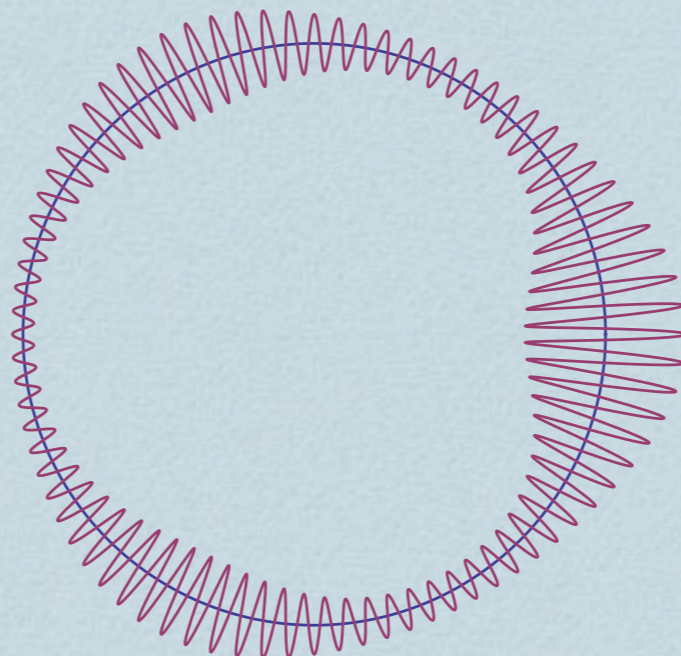
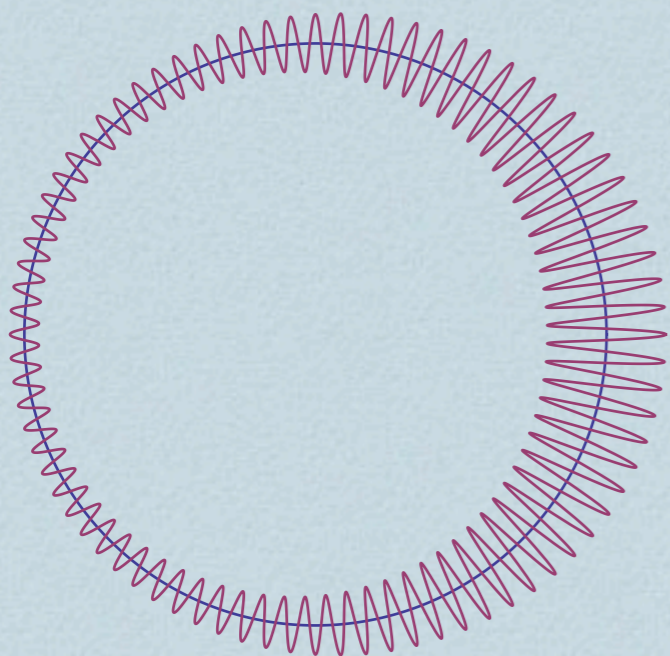
CMB power multipole



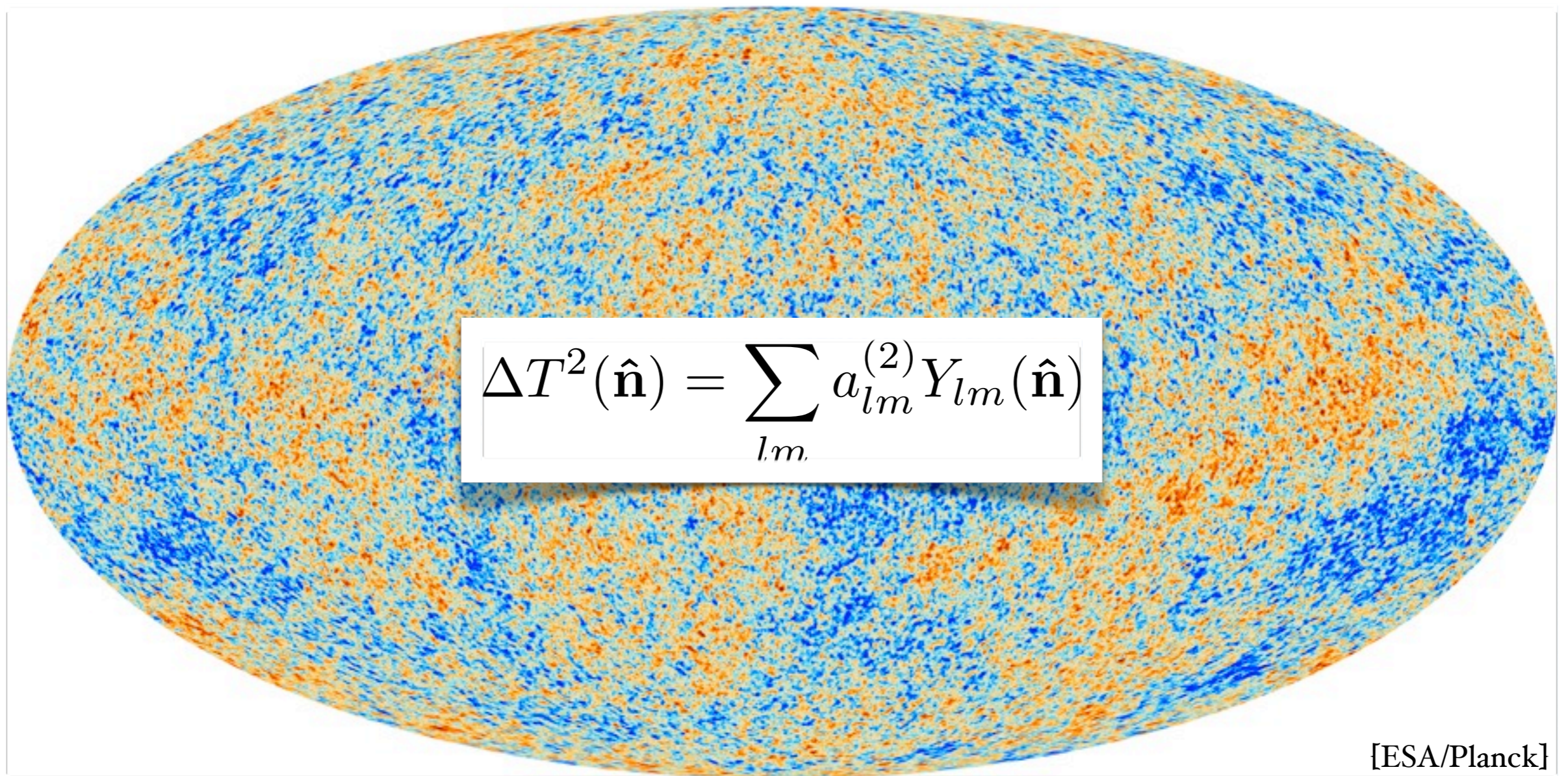
CMB power multipole



CMB power multipole

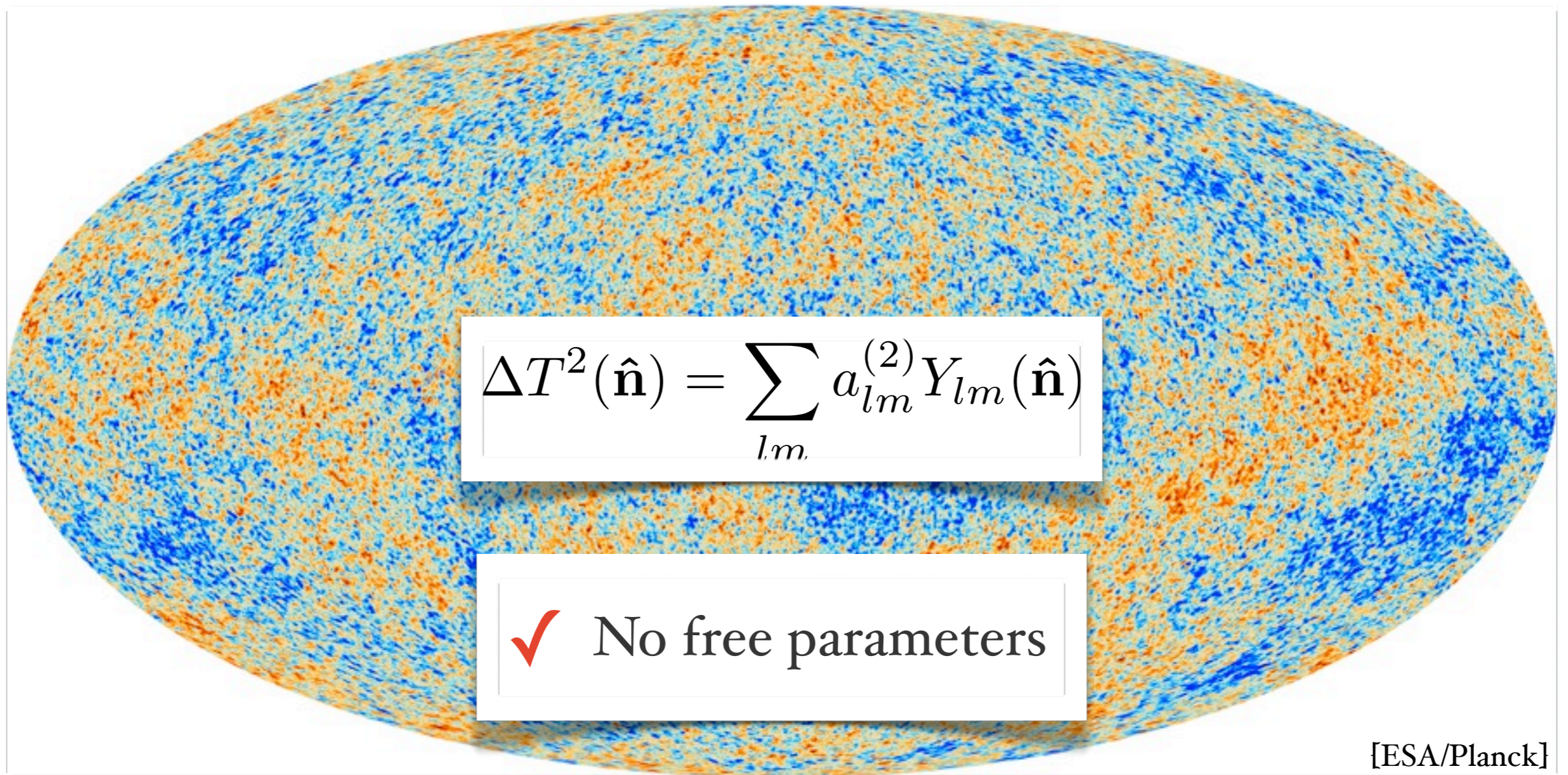


Measurable



[ESA/Planck]

Measurable



$$\Delta T^2(\hat{\mathbf{n}}) = \sum_{l,m} a_{lm}^{(2)} Y_{lm}(\hat{\mathbf{n}})$$

✓ No free parameters

Calculable

❖ For Gaussian perturbations

$$C_l^{(2,2)} = \sum_{l_1 l_2} \frac{(2l_1 + 1)(2l_2 + 1)}{4\pi} P_{l_1 l_2 l} C_{l_1} C_{l_2}$$

$$P_{l_1 l_2 l} \equiv (-1)^{l_1 + l_2 + l} \int_{-1}^1 P_{l_1}(x) P_{l_2}(x) P_l(x) dx$$

$P_l(x)$: Legendre polynomials

Calculable

- ❖ For Gaussian perturbations

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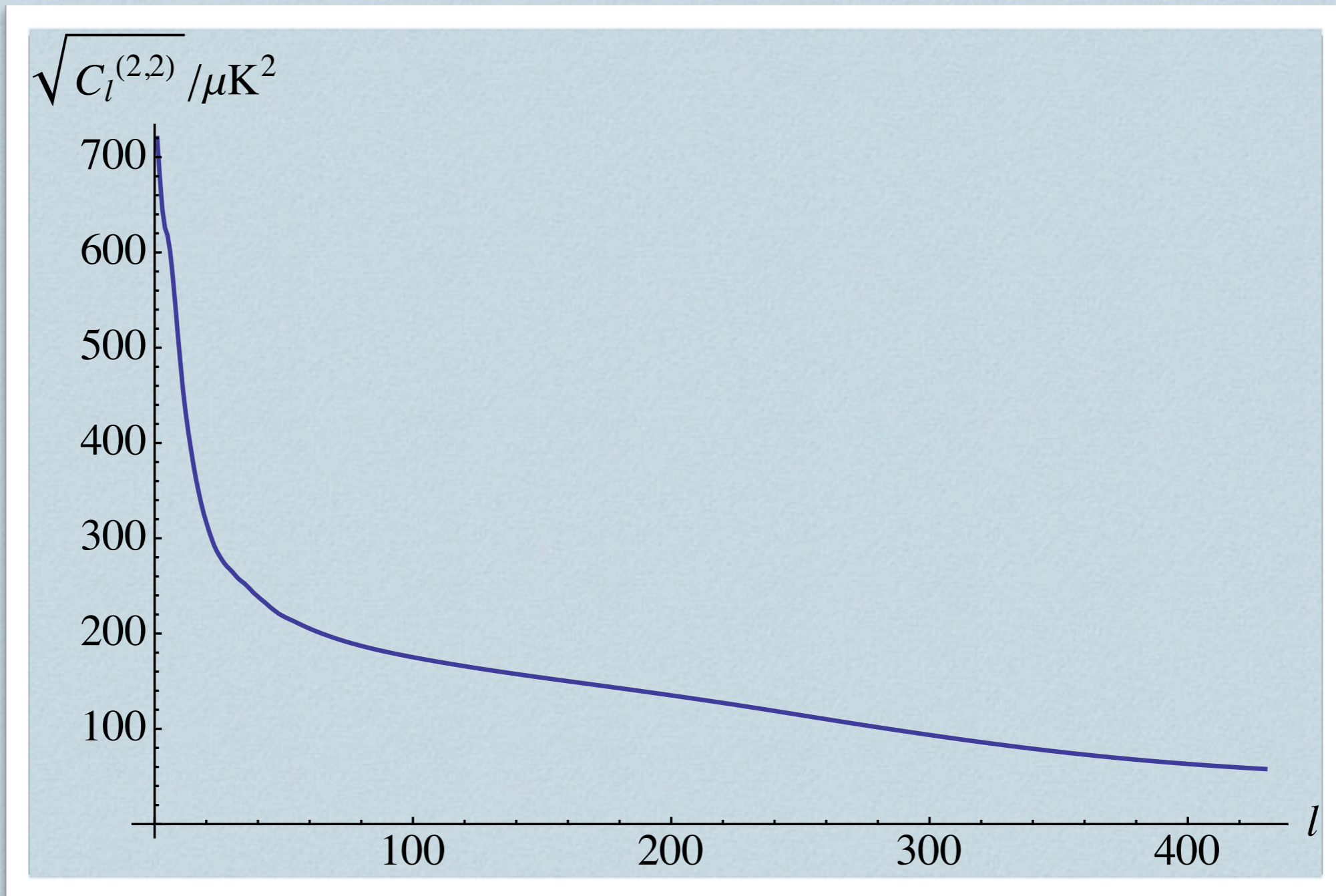
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$P_l(x)$: Legendre polynomials

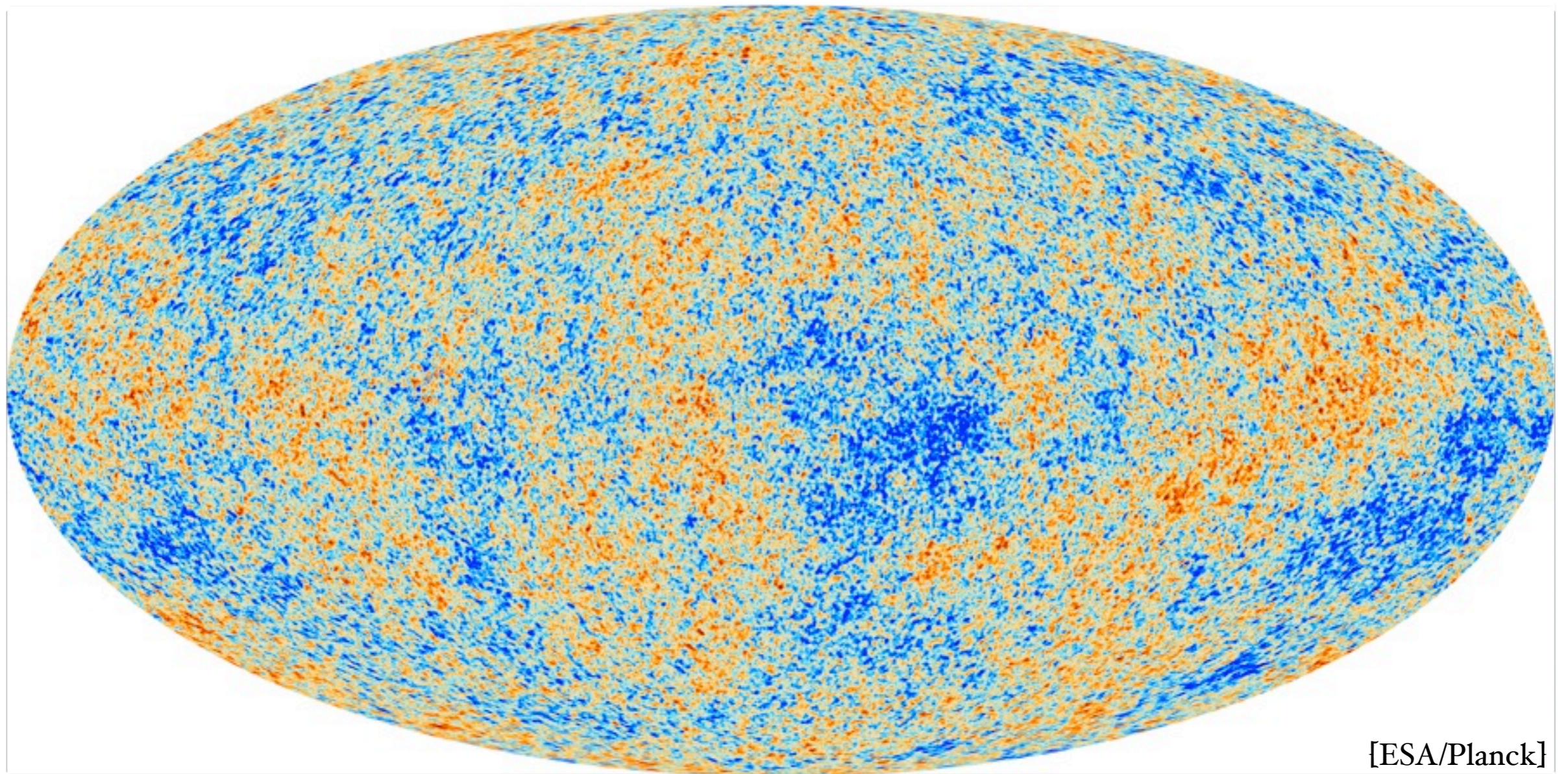
- ❖ Power dipole

$$C_1^{(2,2)} = \sum_l \frac{l+1}{\pi} C_l C_{l+1}$$

Gaussian perturbations

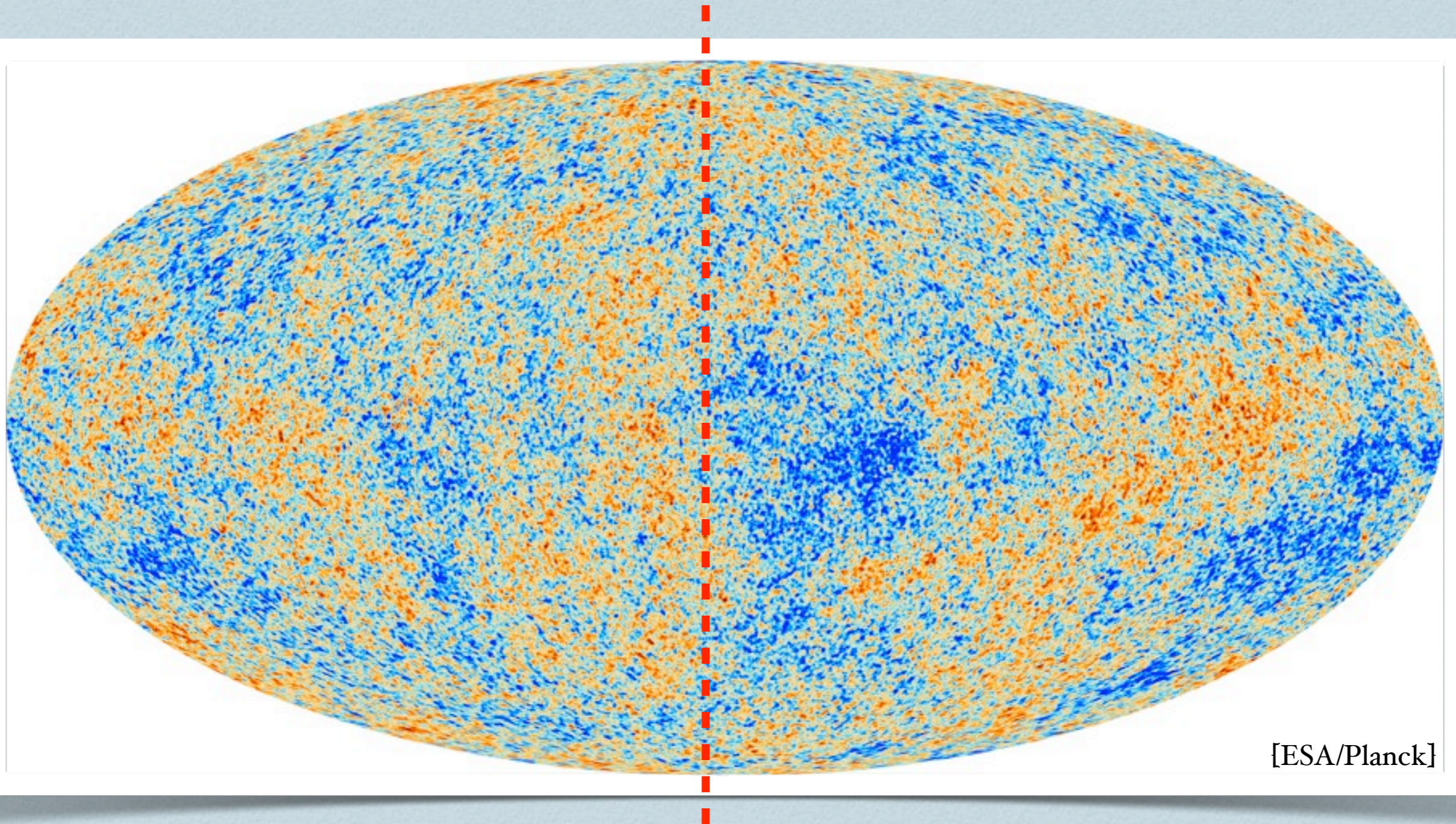


Natural modulation



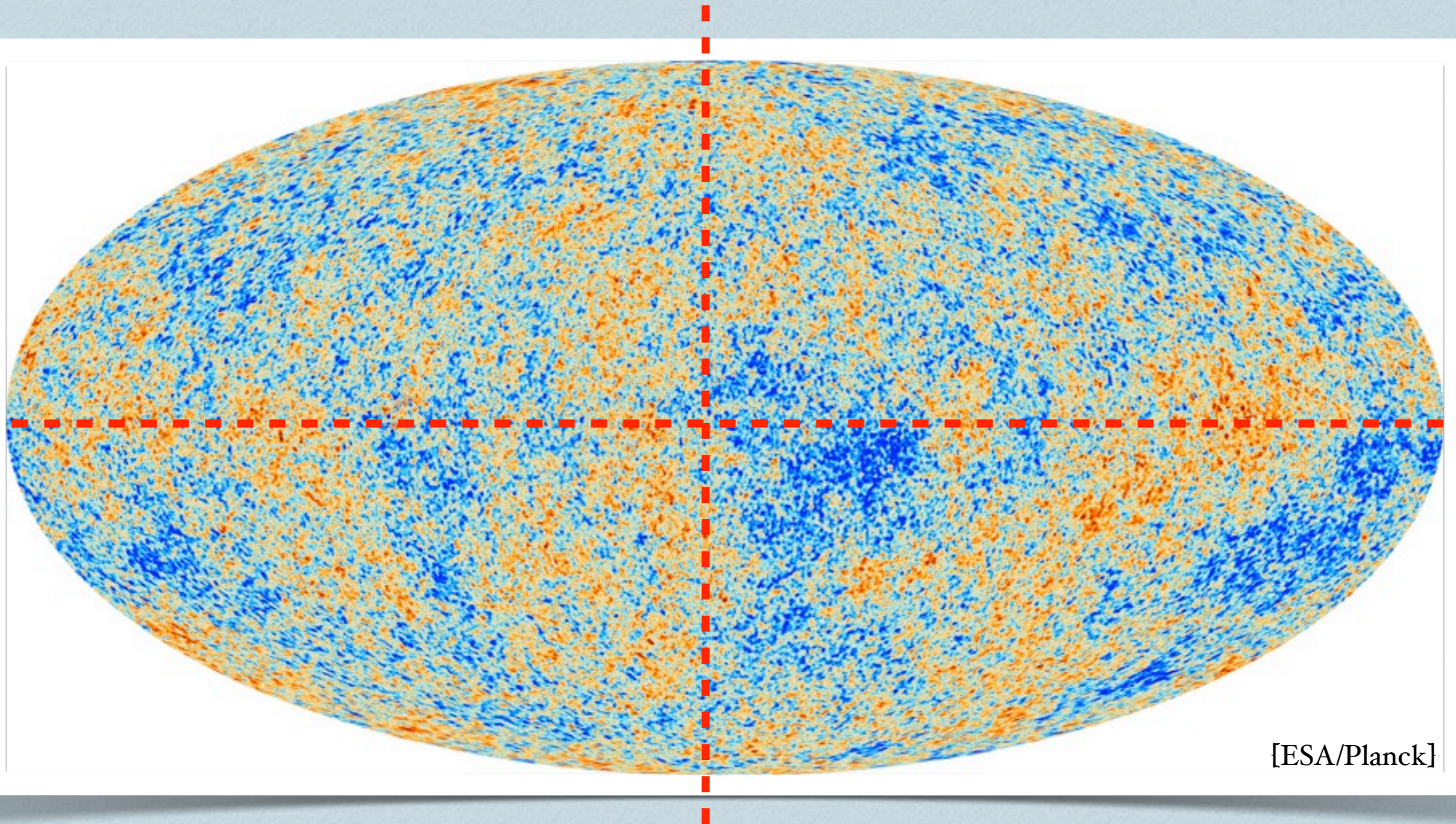
[ESA/Planck]

Natural modulation



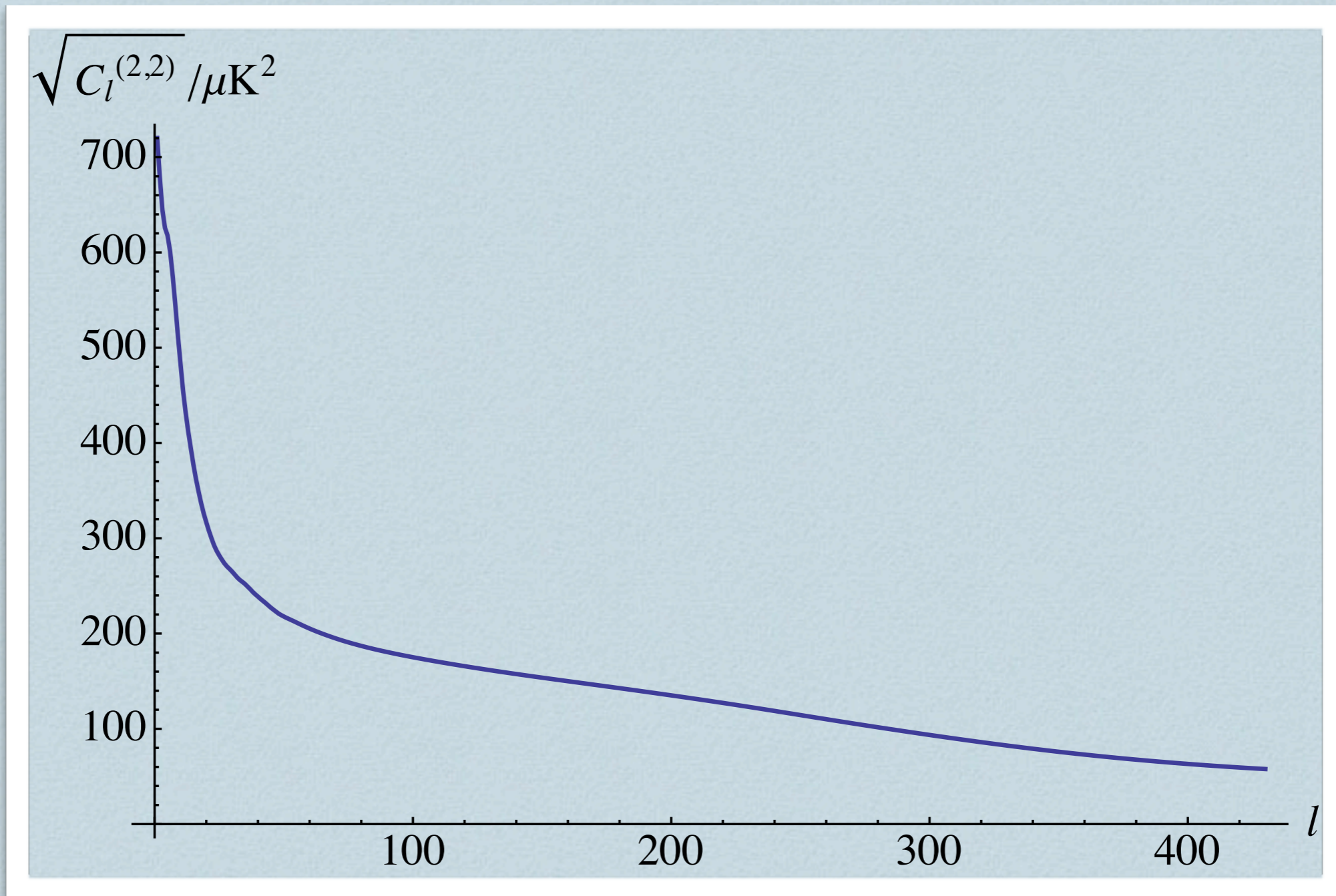
[ESA/Planck]

Natural modulation



[ESA/Planck]

Gaussian perturbations



Calculable

❖ For non-Gaussian perturbations

$$\Delta C_l^{(2,2)} = \sum_{l_1 \dots l_4} \frac{\sqrt{\prod_{n=1}^4 (-1)^{l_n} (2l_n + 1)}}{8\pi(2l + 1)} \sqrt{P_{l_1 l_2 l} P_{l_3 l_4 l}} T_{l_3 l_4}^{l_1 l_2}(l)$$

Calculable

- ❖ For non-Gaussian perturbations

$$\Delta C_l^{(2,2)} = \frac{1}{2l+1} \sum_{l_1 \dots l_4} F_{l_1 l_2 l_3 l_4} T_{l_3 l_4}^{l_1 l_2}(l)$$

Calculable

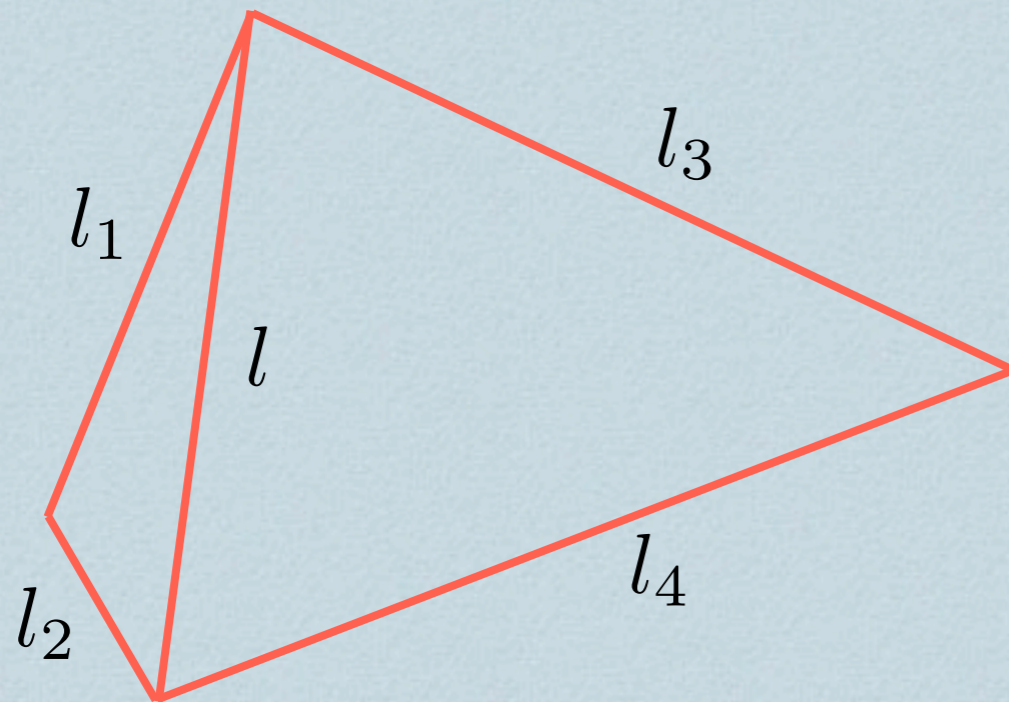
- ❖ For non-Gaussian perturbations

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Calculable

- ❖ For non-Gaussian perturbations

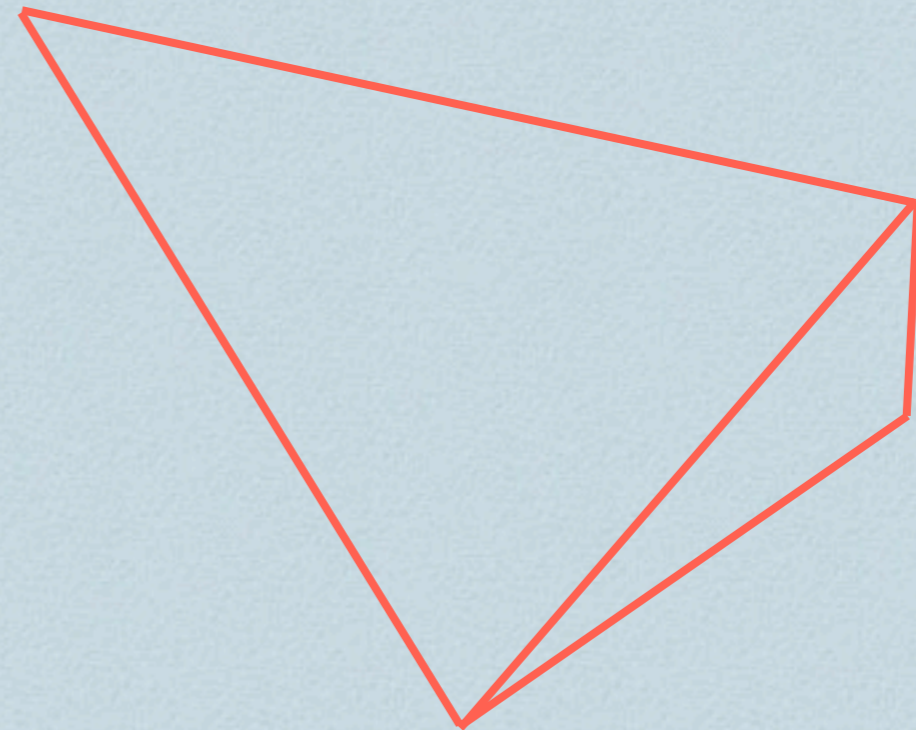
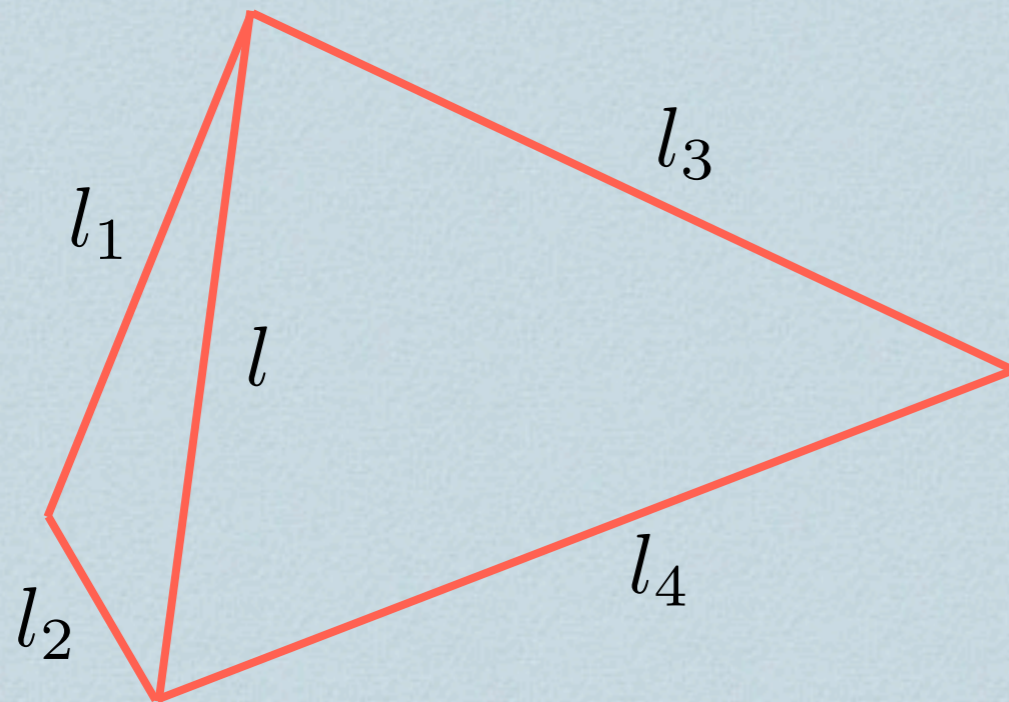
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Calculable

- ❖ For non-Gaussian perturbations

$$\Delta C_l^{(2,2)} = \frac{1}{2l+1} \sum_{l_1 \dots l_4} F_{l_1 l_2 l_3 l_4} T_{l_3 l_4}^{l_1 l_2}(l)$$



Calculable

- ❖ For non-Gaussian perturbations

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g_{NL}

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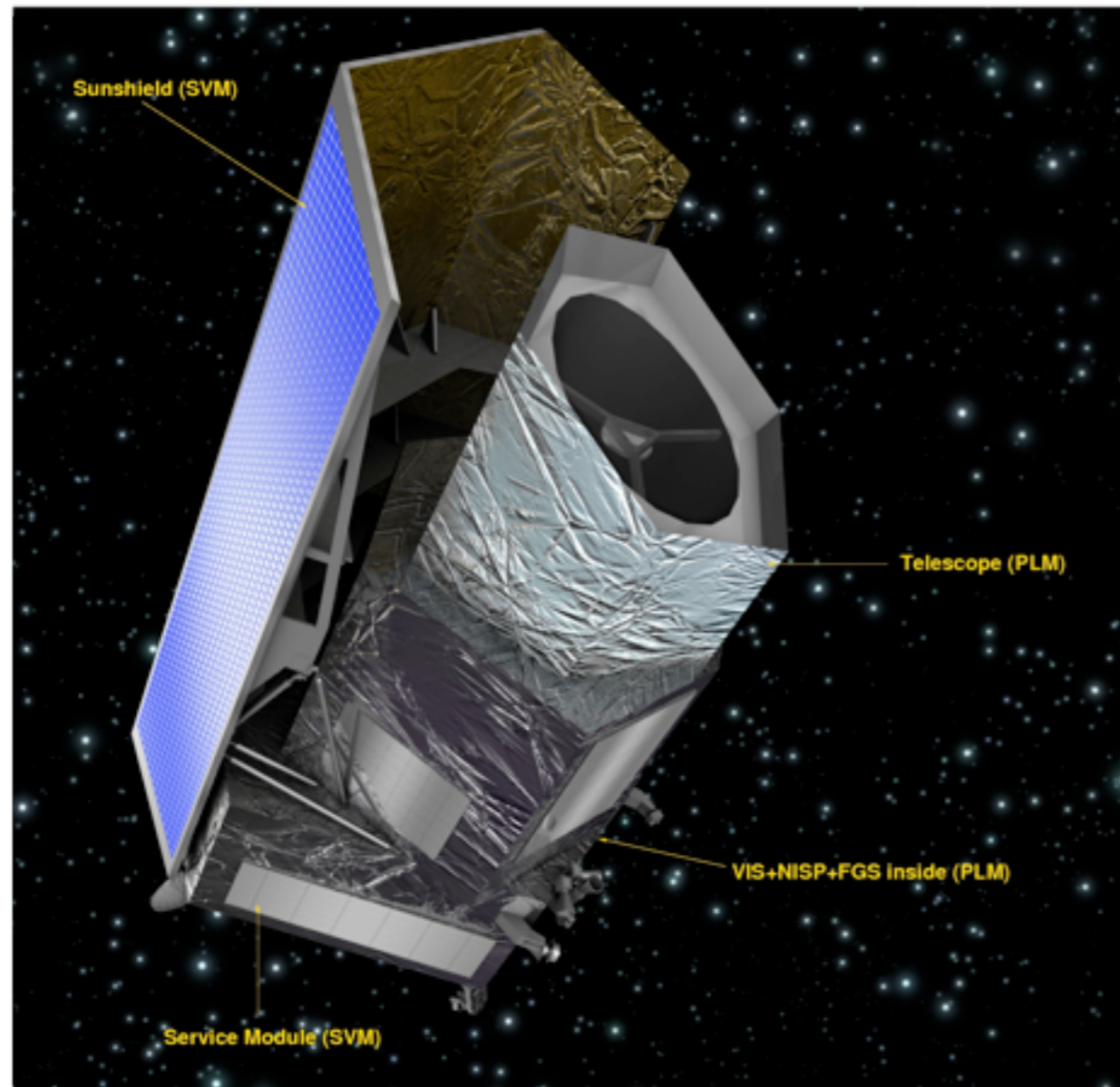
$$\langle \Phi(\mathbf{k}_1) \Phi(\mathbf{k}_2) \Phi(\mathbf{k}_3) \Phi(\mathbf{k}_4) \rangle$$

τ_{NL}

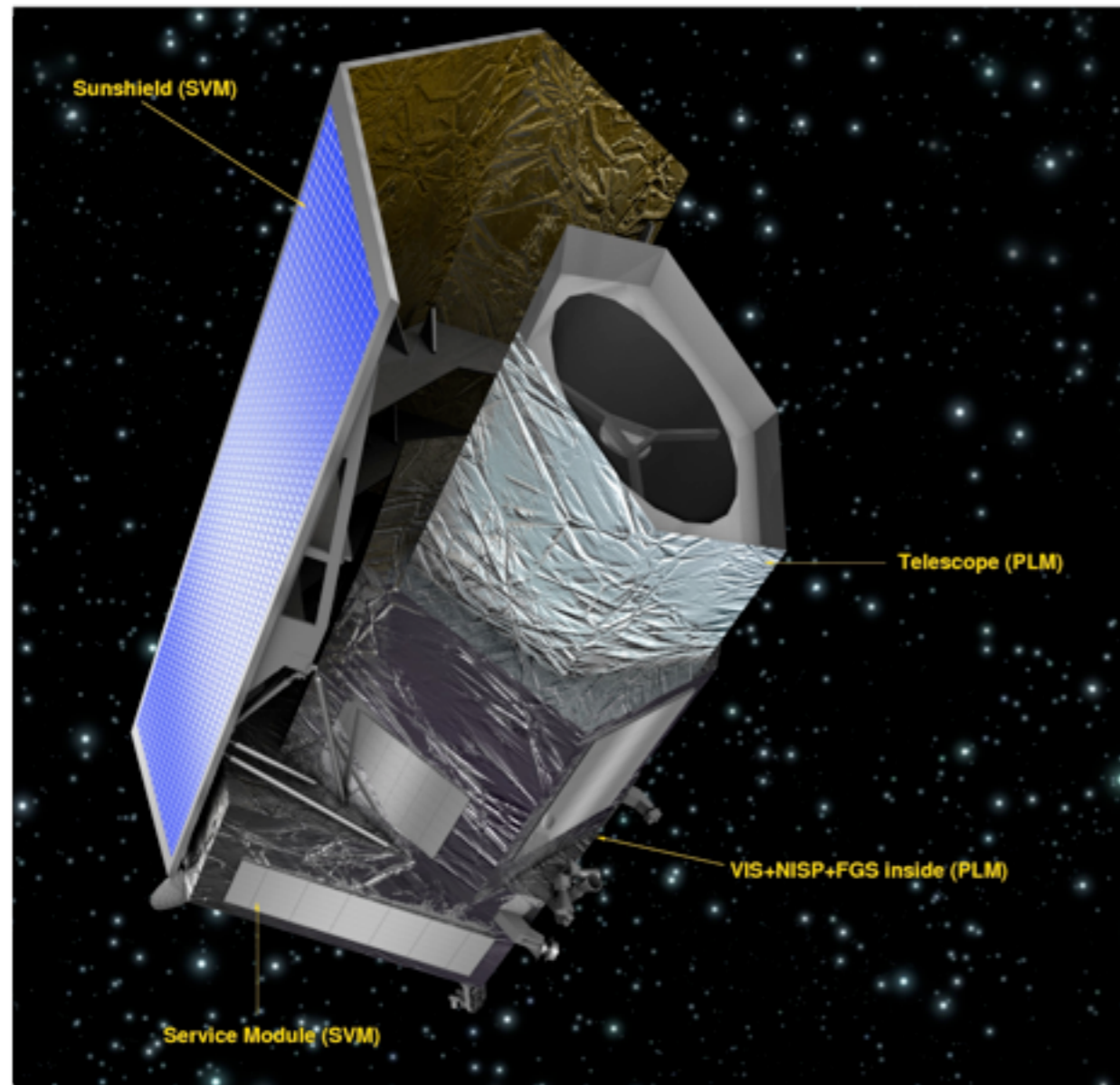
g_{NL}

- ❖ Fully determined by primordial cosmology

LSS power multipoles

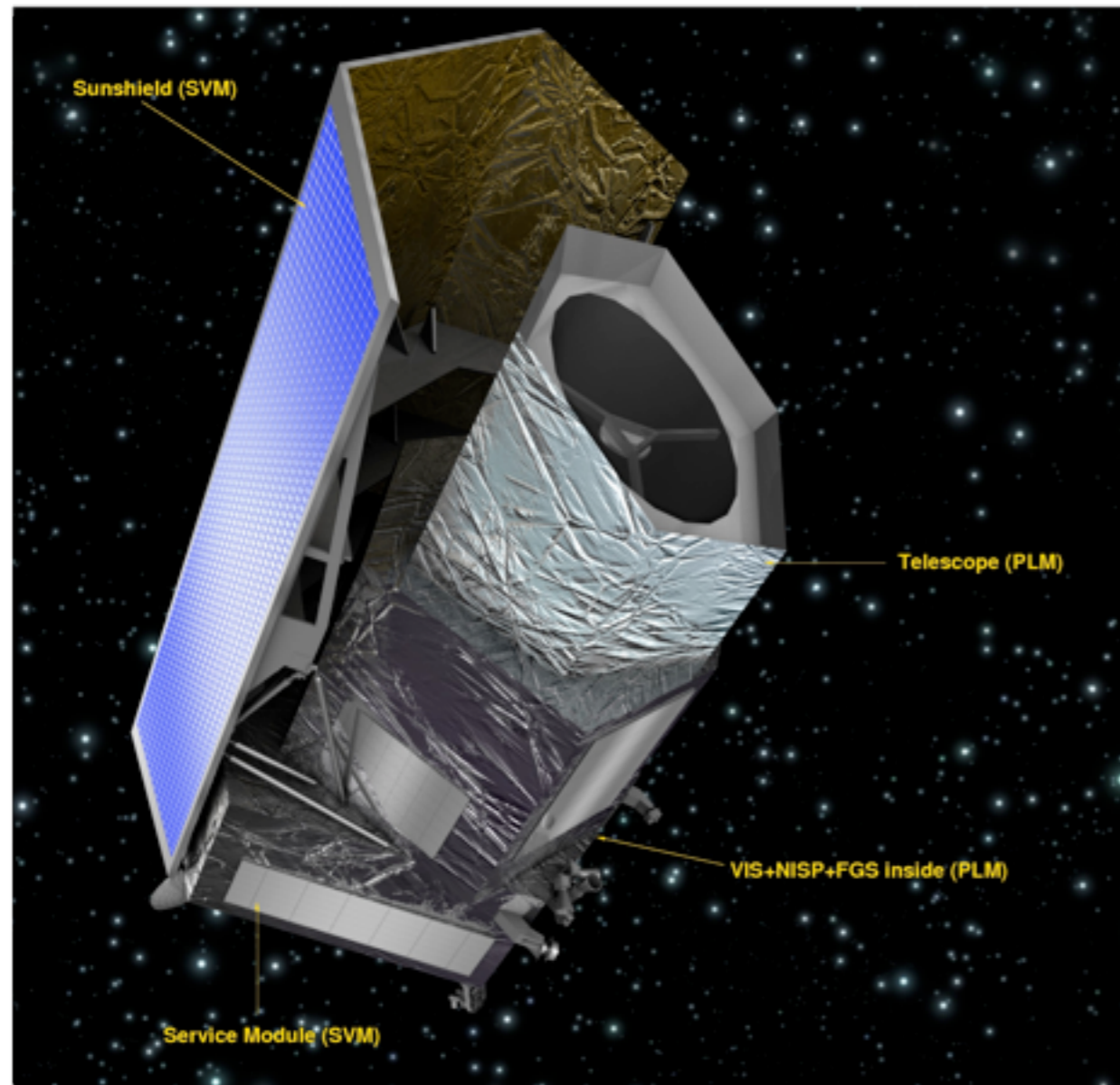


LSS power multipoles



$$\Delta T(\hat{\mathbf{n}}) = \sum_{lm} a_{lm} Y_{lm}(\hat{\mathbf{n}})$$

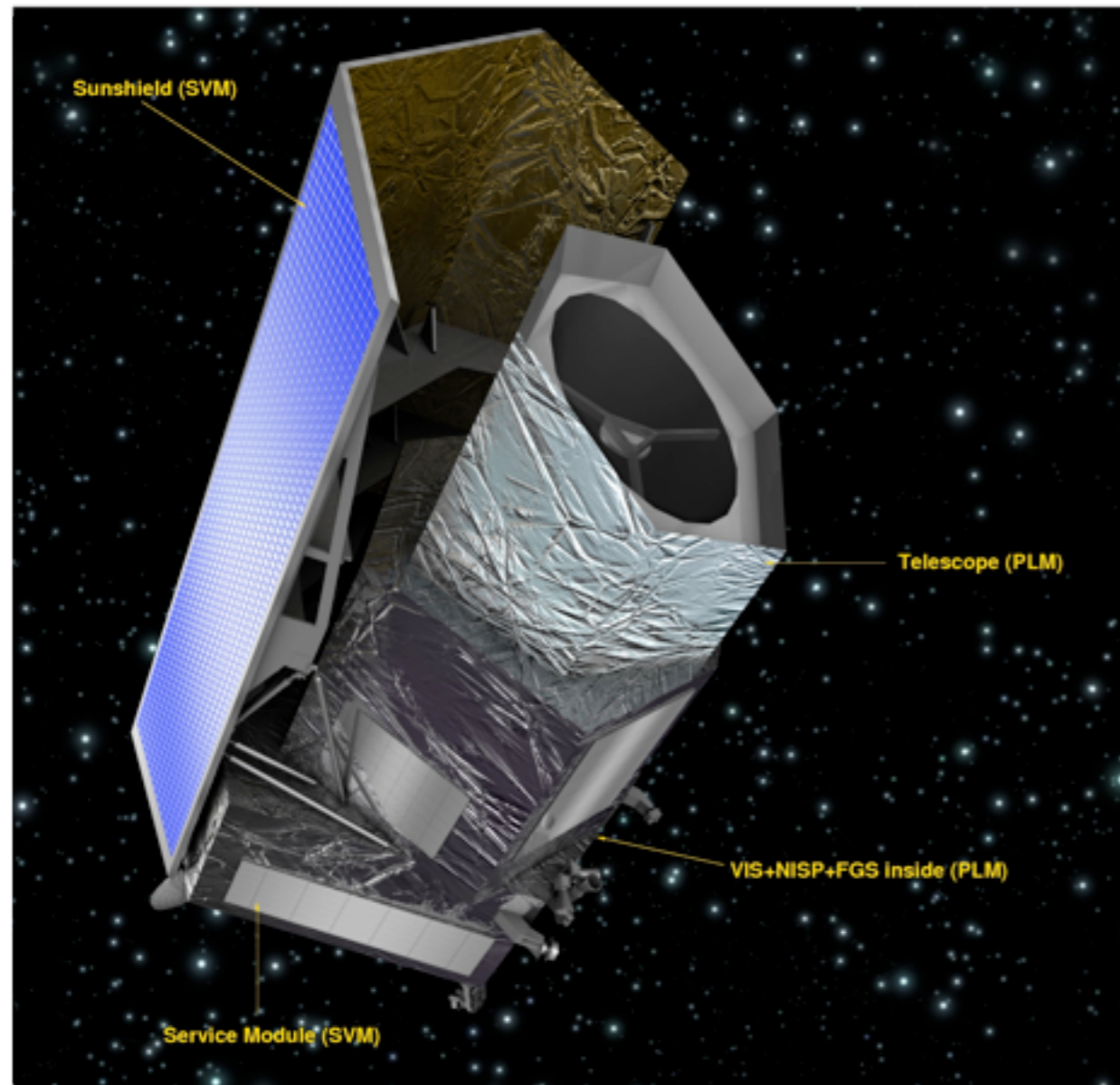
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- ❖ Possible measurement in the near future

Summary

- ❖ Spectator is an alternative to the curvaton scenario
- ❖ It generates smaller non-Gaussianity, negligible isocurvature perturbations, and less tuning
- ❖ Example model shows good agreement with Planck
- ❖ CMB asymmetry is explained with a fast roll spectator
- ❖ Power multipoles is an alternative approach to dipole asymmetry
- ❖ It has no free parameter and is determined by primordial cosmology

Based on [1306.5736], PRD 88 023512,
JCAP 1307 019, JCAP 1305 012, PRD 87 083501