

# Can post-Newtonian theory be tested using Advanced LIGO and Einstein Telescope?

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Raman Research Institute,  
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**IAP, 11th October 2010**



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With Chandra Kant Mishra, K G Arun, & B S Sathyaprakash

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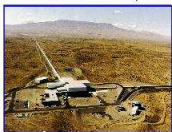
# Aside: What is IndIGO?

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## Current Global GW Network:

Initial LIGO and Virgo achieved Design sensitivity and Enhanced LIGO completed the final S6 run. Advanced LIGO and Virgo in 2015-2017

**LIGO-LHO: 2km, 4km**



**GEO: 0.6km**



**VIRGO: 3km**



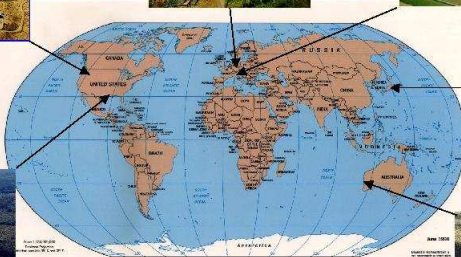
**LIGO-LLO: 4km**



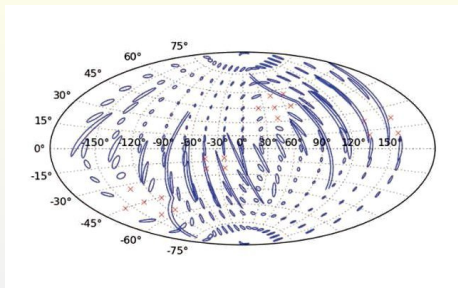
**TAMA: 0.3km**



**AIGO: (?)km**



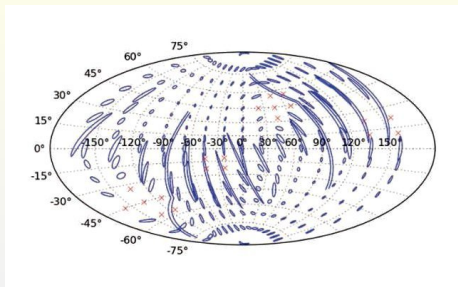
# Towards GW Astronomy - LIGO - Australia



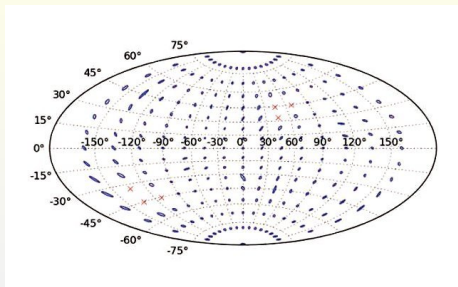
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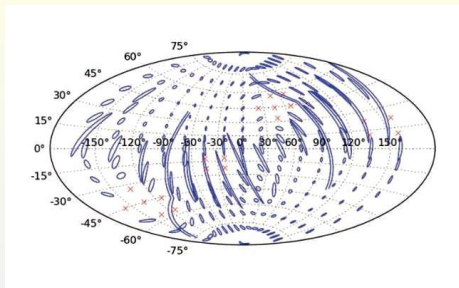


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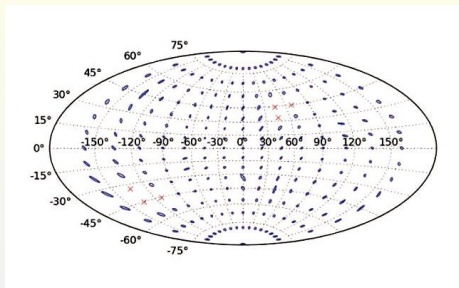
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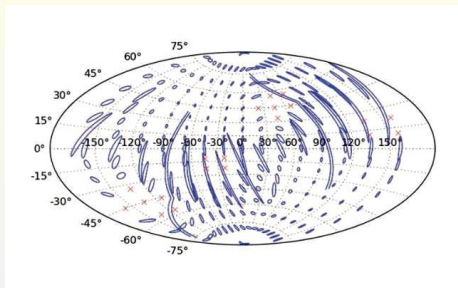


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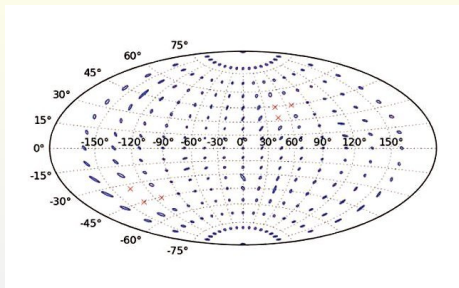
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IndIGO (Indian Initiative in GW Observations) Consortium will seek funds to collaborate with ACIGA to participate in LIGO-Australia.



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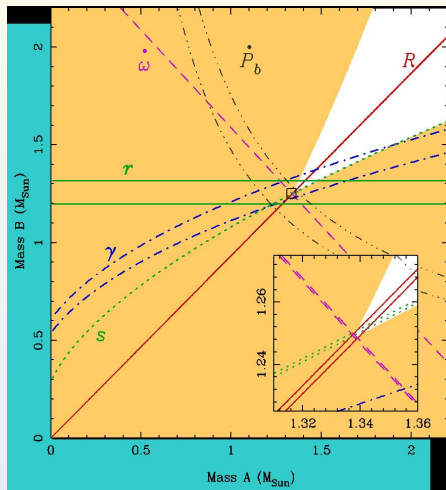
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- General relativity passes these tests in flying colours!

# Testing GR with Binary Pulsar - J0737-3039

Measurement of five PK parameters together with additional measurement of the mass ratio determine and check consistency of pulsar masses in the  $m_1$ - $m_2$  plane

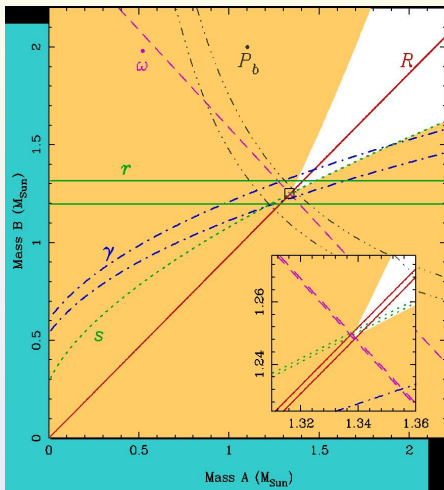
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Tests possible due to physically motivated but structurally simple parametrisations (PPN, PPK) of observable quantities that could have different values in different theories of gravity.

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## Gravitational Waves

- Gravitational Waves have direct imprints on all the strong field effects
- How well can GW observations constrain deviations from GR?

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  - ▶ Parametrizing the 1PN coefficient of the phasing formula in terms of the Compton wavelength of the massive graviton and bounding its value from GW observations [Will, 1998].

## The question

Can these tests be generalized, without having to know a priori the parameters of the underlying theory of gravity at least in theories that do not deviate from GR to prevent *detection* with GR templates?



# Parametrized test of PN theory

## Phasing formula in the restricted waveform approximation

$$\tilde{h}(f) = \frac{1}{\sqrt{30} \pi^{2/3}} \frac{\mathcal{M}^{5/6}}{D_L} f^{-7/6} e^{i\psi(f)},$$

and to 3.5PN order the phase of the Fourier domain waveform is given by

$$\psi(f) = 2\pi f t_c - \phi_c - \frac{\pi}{4} + \sum_{k=0}^7 (\psi_k + \psi_{kl} \ln f) f^{\frac{k-5}{3}}, \quad (1)$$

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- Independent determination of 3 or more of the phasing coefficients  $\Rightarrow$  Tests of PN theory [KGA, Iyer, Qusailah & Sathyaprakash, 2006].

## The $\alpha_l$ coefficients

$$\alpha_0 = 1, \quad \alpha_1 = 0, \quad \alpha_2 = \frac{3715}{756} + \frac{55}{9}\nu, \quad \alpha_3 = -16\pi,$$

$$\alpha_4 = \frac{15293365}{508032} + \frac{27145}{504}\nu + \frac{3085}{72}\nu^2;$$

$$\alpha_5 = \pi \left( \frac{38645}{756} - \frac{65}{9}\nu \right) \left[ 1 + \ln \left( 2 \cdot 6^{3/2} \pi M \right) \right],$$

$$\alpha_6 = \frac{11583231236531}{4694215680} - \frac{640}{3}\pi^2 - \frac{6848}{21}C$$
$$+ \left( -\frac{15737765635}{3048192} + \frac{2255}{12}\pi^2 \right) \nu + \frac{76055}{1728}\nu^2 - \frac{127825}{1296}\nu^3$$
$$- \frac{6848}{63} \ln(128 \pi M); \quad \alpha_7 = \pi \left( \frac{77096675}{254016} + \frac{378515}{1512}\nu - \frac{74045}{756}\nu^2 \right).$$

$$\alpha_{jl} = 0, \quad j = 0, 1, 2, 3, 4, 7;$$

$$\alpha_{5l} = \pi \left( \frac{38645}{756} - \frac{65}{9}\nu \right); \quad \alpha_{6l} = -\frac{6848}{63}$$

$C = 0.577 \dots$ , - Euler's constant.

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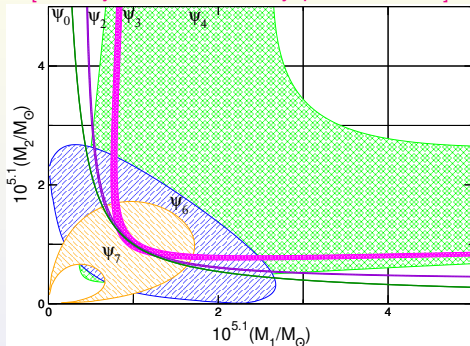
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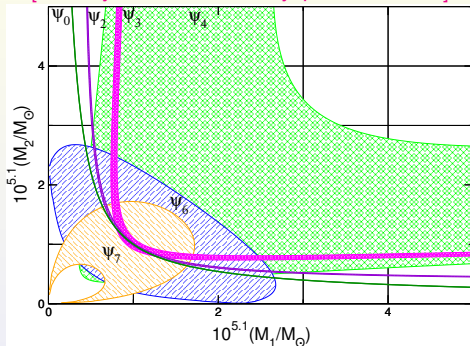


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## Issues

Highly correlated parameters & Ill-conditioned Fisher matrix for a large parameter space.

## Alternative Proposal [KGA, Iyer, Qusailah & Sathyaprakash, 2006b]

- Treat two parameters as basic variables in terms of which one can parametrize *all* other parameters in the *restricted* phasing formula *except* one which is the *test* parameter. Dimensionality of the parameter space is thus considerably reduced.

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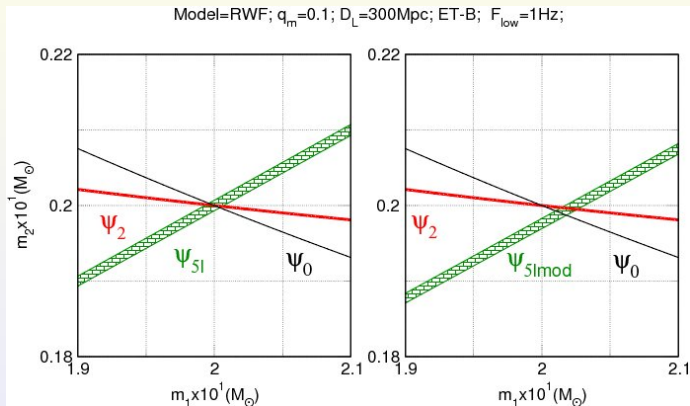
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- By expressing PN coefficients at order higher than the PN order of the test coefficient in terms of the basic variables one reduces the systematic effects in GR coming from higher order PN terms and focusses solely on the differences arising between GR and the *plausibly different correct* theory of gravity.

# What Difference we expect to see??

## GR vs Mock Alternative Gravity theory



Regions in the  $m_1$ - $m_2$  plane that corresponds to 1- $\sigma$  uncertainties in  $\psi_0$ ,  $\psi_2$  and  $\psi_{51}$ .  
Left panel for GR.

Right panel assumes correct theory of gravity is a hypothetical non-GR theory in which the phasing coefficient  $\psi_{51}$  and all higher PN coefficients, differ from the GR values by 1%



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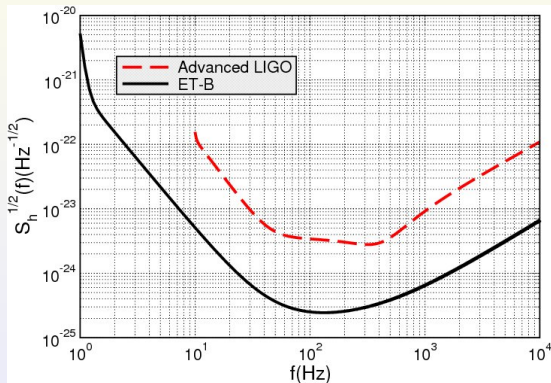
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## Present work - Use of Full Waveforms

- Revisit the earlier estimates using Advanced LIGO and the ET noise PSD. Critically examine & quantify underlying assumptions
- Effect of low frequency sensitivity of ET on our Test of GR.
- Use of 3PN accurate amplitude corrected waveforms ( $f_k = f/k$ )

$$\begin{aligned}\tilde{h}(f) &= \frac{2M\nu}{D_L} \sum_{k=1}^8 \sum_{n=0}^6 \frac{A_{(k,n/2)}(t(f_k)) x^{\frac{n}{2}+1}(t(f_k))}{2\sqrt{k\dot{F}}(t(f_k))} \\ &\times \exp[-i\phi_{(k,n/2)}(t(f_k)) + 2\pi if t_c - i\pi/4 + ik\Psi(f_k)] \\ \Psi(f) &= -\phi_c + \sum_{j=0}^7 [\psi_j + \psi_{jl} \ln f] f^{(j-5)/3} \\ \psi_j &= \frac{3}{256\nu} (2\pi M)^{(j-5)/3} \alpha_j, \quad \psi_{jl} = \frac{3}{256\nu} (2\pi M)^{(j-5)/3} \alpha_{jl}.\end{aligned}$$

# Amplitude spectrum of Advanced LIGO and ET



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- Amplitude corrections depend on masses, luminosity distance, source location  $\theta$  and  $\phi$ , polarization angle  $\psi$  and inclination angle  $\iota$ . Ten parameters  $\mathbf{p} \equiv (\ln D_L, \cos \theta, \phi, t_c, \phi_c, \psi_0, \psi_2, \psi_T, \cos \iota, \psi)$

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- Final parameter space is spanned by:  $\{t_c, \phi_c, \psi_0, \psi_2, \psi_T, (\cos \iota, \psi)\}$

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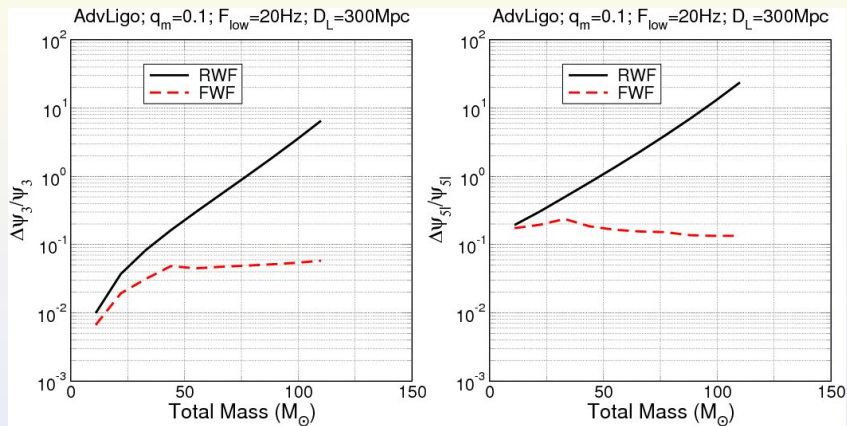
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- Few coalescence events of IMBBHs within  $z = 2$  or  $z = 1$  depending on what triggered seed galaxies.



# Advanced LIGO - Relative errors



Source orientations chosen arbitrarily to be  $\theta = \phi = \pi/6$ ,  $\psi = \pi/4$ ,  $\iota = \pi/3$ .

# Advanced LIGO - Results

- GW observations of BBHs (in the range  $11-110M_{\odot}$  and at a luminosity distance of 300 Mpc) by Advanced LIGO can be used to estimate *only* the 1.5PN coefficient  $\psi_3$  (leading tail) with fractional accuracy better than 6% when the FWF is used.

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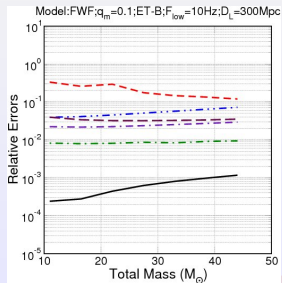
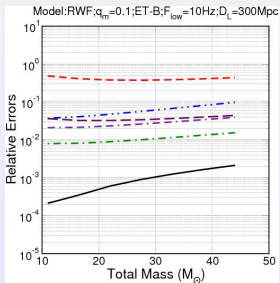
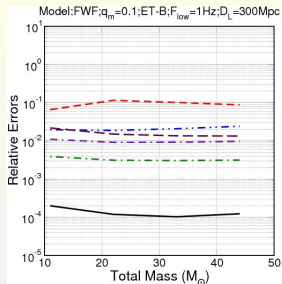
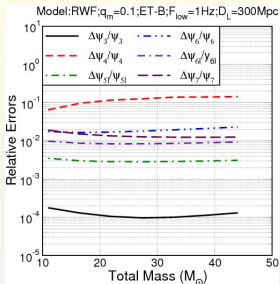
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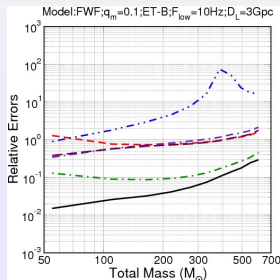
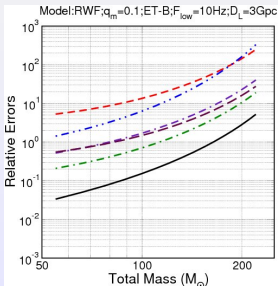
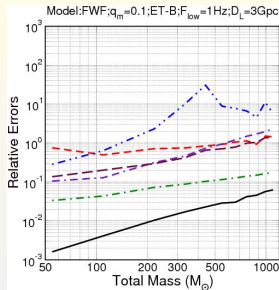
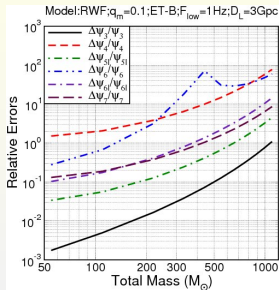
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# Einstein Telescope (ET)- Stellar mass BH



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- When total mass is less than about  $100 M_{\odot}$ , all the  $\psi_k$ 's are measured with relative errors less than unity, the most accurately determined parameters being  $\psi_3$  and  $\psi_{51}$ ; which are determined with accuracies better than 10%. Most interesting mass range for the proposed test in the ET band.

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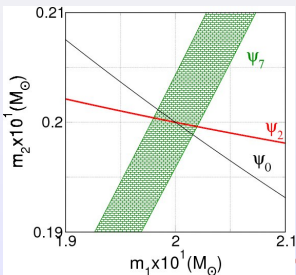
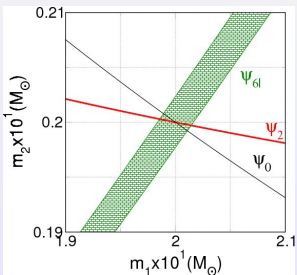
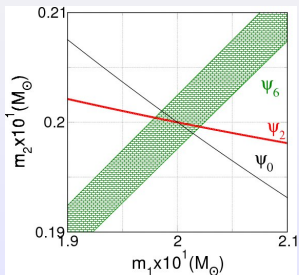
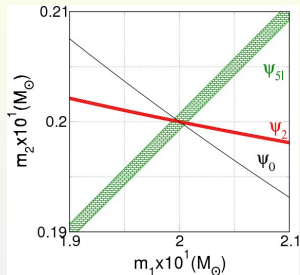
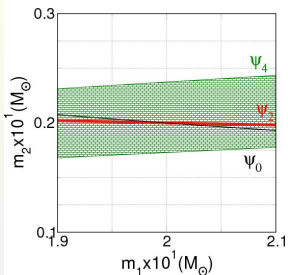
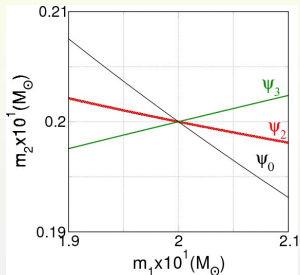
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- Choice of lower cutoff important for testing PN theory using ET

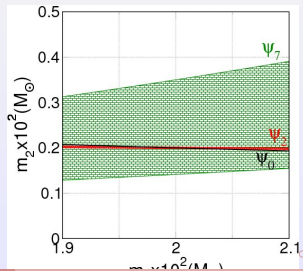
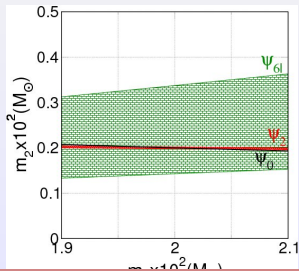
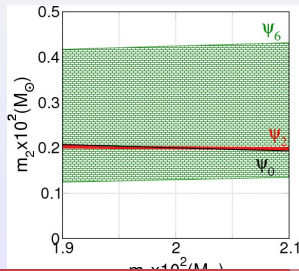
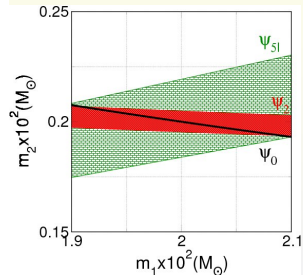
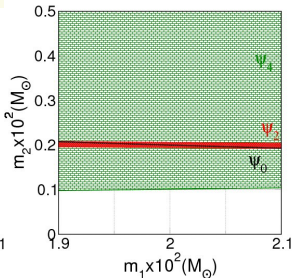
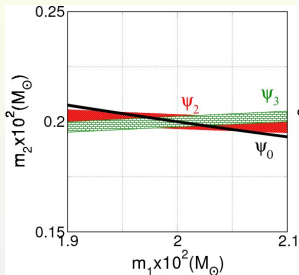
# Testing GR by GW phasing - Stellar mass BH

Model=FWF;  $q_m=0.1$ ;  $D_L=300\text{Mpc}$ ; ET-B;  $F_{\text{low}}=1\text{Hz}$



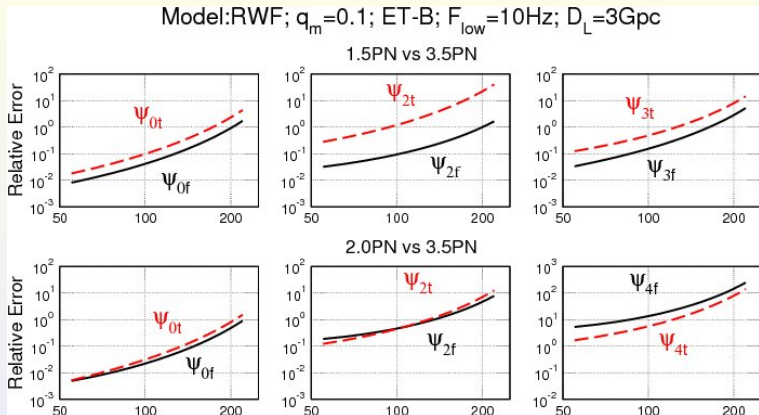
# Testing GR by GW phasing - IMBBH

Model= FWF;  $q_m=0.1$ ;  $D_L=3\text{Gpc}$ ; ET-B;  $F_{\text{low}}=1\text{Hz}$



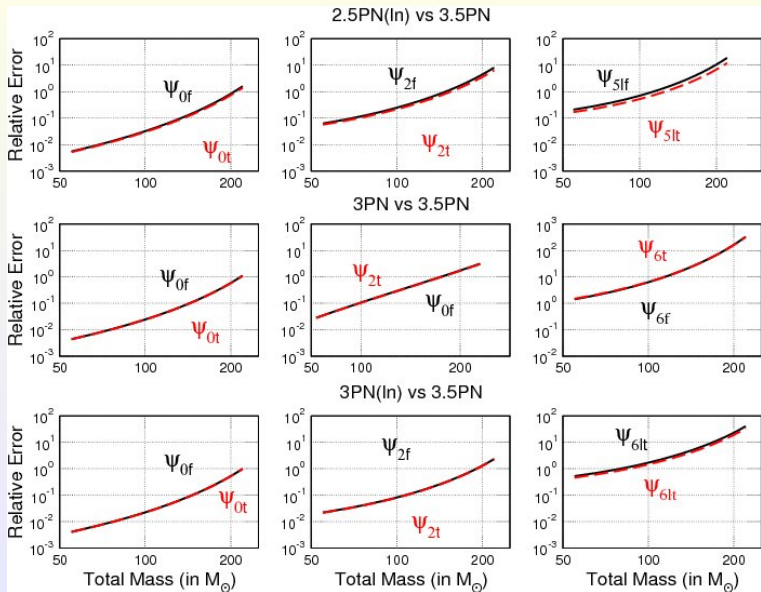


# Truncated phasing vs Full 3.5PN phasing



$\psi_0$  and  $\psi_2$  are basic parameters and all PN parameters up to 3.5PN (full phasing) except the test parameter are parametrized by  $\psi_0$  and  $\psi_2$ . The other similarly constructed but the phasing truncated at the PN order corresponding to the test parameter. The test parameter with truncated phasing is denoted by  $\psi_{it}$  while with full 3.5PN phasing it is denoted by  $\psi_{if}$ .

# Truncated phasing vs Full 3.5PN phasing



# What to choose as basic parameters??

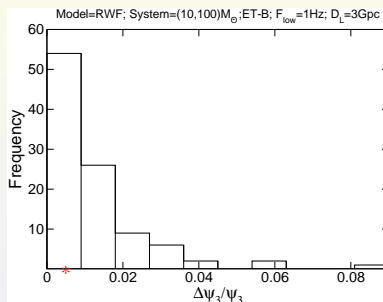
$(m_1, m_2) = (10, 100)M_\odot$ ;  $f_s = 1$  Hz;  $D_L = 3$  Gpc; Waveform Model: RWF

	$\psi_0$ - $\psi_2$	$\psi_0$ - $\psi_3$	$\psi_0$ - $\psi_4$	$\psi_0$ - $\psi_{5l}$	$\psi_0$ - $\psi_6$	$\psi_0$ - $\psi_{6l}$	$\psi_0$ - $\psi_7$
$\Delta\psi_0/\psi_0$	–	0.0015 (60)	0.0015 (60)	0.0015 (60)	0.0015 (60)	0.0015 (60)	0.0015 (60)
$\Delta\psi_f/\psi_f$	–	0.0092 (15)	0.010 (17)	0.017 (18)	0.043 (17)	0.020 (19)	0.022 (19)
$\Delta\psi_2/\psi_2$	–	0.027 (27)	0.027 (27)	0.027(27)	0.027(27)	0.027(27)	0.027(27)
$\Delta\psi_0/\psi_0$	0.0010 (55)	–	0.0010 (55)	0.0010(55)	0.0010(55)	0.0010(55)	0.0010(55)
$\Delta\psi_f/\psi_f$	0.0089 (13)	–	0.020 (16)	0.031(16)	0.082(16)	0.037(16)	0.042(16)
$\Delta\psi_3/\psi_3$	0.0050 (42)	–	0.0050 (42)	0.0050 (42)	0.0050(42)	0.0050(42)	0.0050 (42)
$\Delta\psi_0/\psi_0$	0.0011 (28)	0.0011(28)	–	0.0011 (28)	0.0011(28)	0.0011(28)	0.0011(28)
$\Delta\psi_f/\psi_f$	0.074(8)	0.15(8)	–	0.25(8)	0.65(8)	0.29(8)	0.33(8)
$\Delta\psi_4/\psi_4$	2.1 (8)	2.1(8)	–	2.1(8)	2.1(8)	2.1(8)	2.1(8)
$\Delta\psi_0/\psi_0$	0.00059 (77)	0.00059 (77)	0.00059(77)	–	0.00059(77)	0.00059(77)	0.00059(77)
$\Delta\psi_f/\psi_f$	0.014(24)	0.026(23)	0.029(23)	–	0.12(23)	0.052(23)	0.058(23)
$\Delta\psi_{5l}/\psi_{5l}$	0.056 (17)	0.056(17)	0.056(17)	–	0.056(17)	0.056(17)	0.056(17)
$\Delta\psi_0/\psi_0$	0.00054 (64)	0.00054 (64)	0.00054 (64)	0.00054(64)	–	0.00054 (64)	0.00054(64)
$\Delta\psi_f/\psi_f$	0.0067 (21)	0.013(20)	0.014(19)	0.021 (19)	–	0.025(19)	0.028(19)
$\Delta\psi_6/\psi_6$	0.67(13)	0.67 (13)	0.67(13)	0.67 (13)	–	0.67(13)	0.67(13)
$\Delta\psi_0/\psi_0$	0.00051(62)	0.00051 (62)	0.00051(62)	0.00051(62)	0.00051(62)	–	0.00051 (62)
$\Delta\psi_f/\psi_f$	0.0051(21)	0.0096 (19)	0.010 (19)	0.016(19)	0.042(19)	–	0.021(18)
$\Delta\psi_{6l}/\psi_{6l}$	0.17(13)	0.17 (13)	0.17 (13)	0.17(13)	0.17(13)	–	0.17(13)
$\Delta\psi_0/\psi_0$	0.00049 (59)	0.00049(59)	0.00049(59)	0.00049(59)	0.00049(59)	0.00049(59)	–
$\Delta\psi_f/\psi_f$	0.0046 (20)	0.0087(18)	0.0094(18)	0.014 (17)	0.038(18)	0.017(17)	–
$\Delta\psi_7/\psi_7$	0.19(10)	0.19(10)	0.19(10)	0.19(10)	0.19(10)	0.19(10)	–

Number in parentheses is factor by which accuracy will be reduced for lower cutoff of 10 Hz. Fundamental pair is chosen to be

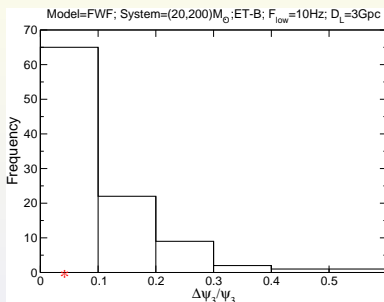
$(\psi_0, \psi_f)$  where  $f$  can be any of 2, 3, 4, 5l, 6, 6l, 7. Relative error in the test parameter is listed in the third row.

# Robustness of TOG wrt Angles - RWF



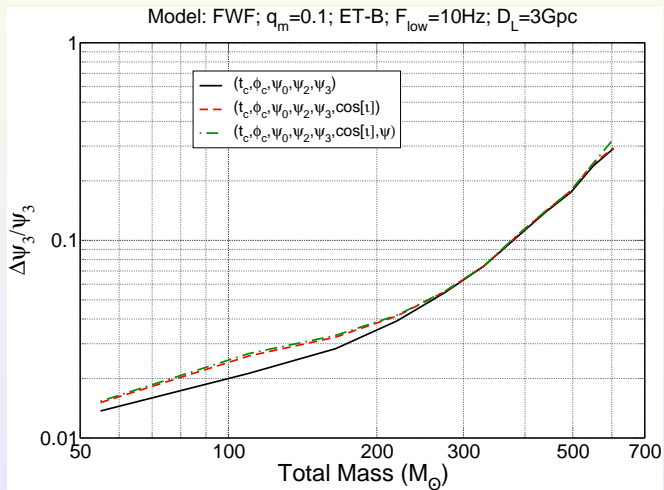
Histogram for the relative error in the estimation of the parameter  $\psi_3$  using hundred different realizations of angular parameters for a  $(10, 100)M_{\odot}$  binary located at the luminosity distance of 3 Gpc. The low frequency cutoff is 1 Hz and RWF has been used.  $\Delta\psi_3/\psi_3$  was 0.005 for the arbitrary choice of angles we made.

# Robustness of TOG wrt Angles - FWF



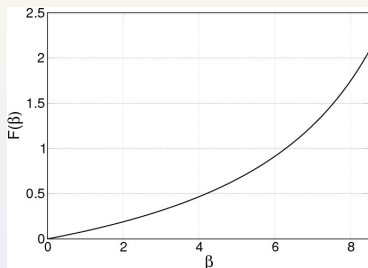
Histogram for the relative error in the estimation of the parameter  $\psi_3$  using hundred different realizations of angular parameters for a  $(20, 200)M_{\odot}$  binary located at the luminosity distance of 3 Gpc. The low frequency cutoff is 10 Hz and FWF has been used.  $\Delta\psi_3/\psi_3$  was 0.042 for the arbitrary choice of angles we made.

# Sensitivity of results to inclusion of $\iota$ and $\psi$ in the Fisher analysis



## Effect of spin on the test

- Effects of spin can offset estimation of the PN coefficients..e.g.  $\beta \geq 6$  can affect 1.5PN coeff by 100%.



Plot shows the variation of systematic bias due to spin  $F(\beta)$  with the spin parameter  $0 \leq \beta \leq 8.5$ , where  $F(\beta)$  is given by  $F(\beta) = 4\beta(16\pi - 4\beta)^{-1}$ .

## Summary and Conclusion

- Investigated possibility of testing the theory of gravity within a well-defined subclass of Parametrised Post Einstein (ppE) theories (Pretorius and Yunes) using GW observations of BBHs by a typical second generation GW interferometer (Advanced LIGO) and the plausible third generation GW interferometer (ET).



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- For IMBBH binaries, though a lower cutoff of 1 Hz and use of FWF improves the estimation of all PN parameters in the phasing formula, Only for an event very close by, can the test be performed very accurately.
- Choice of lower cutoff important for testing PN theory using ET

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  - ▶ Implies that implicit in our work is the assumption that we are dealing post detection with a known source and that  $\psi_0$  and  $\psi_2$  are as in GR. Much more work needed is needed to test the N and 1PN parameters..

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- If the PN expansion differs from GR slightly then the error in the estimation of parameters will not change to first order.

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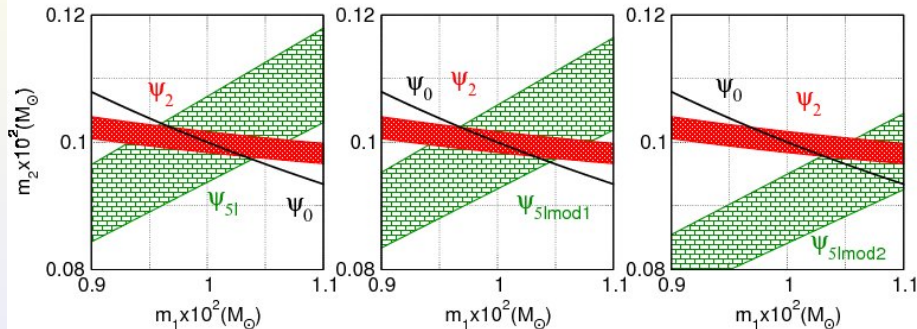
## Future directions

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- Effect of merger, ringdown, orbital eccentricity not estimated
- To test fully the proposal one must mimic the whole exercise by mock data. One has to inject a non-GR signal into Gaussian bgd with a signal that differs from GR at 1.5PN and higher orders by certain degree. One would then need to extract the first three parameters by a MCMC technique using GR templates and check if what we expect from our study holds good.

# What difference do we expect to see??

## GR vs Mock Alternative Gravity theory

Model=RWF;  $q_m=0.1$ ;  $D_L=3\text{Gpc}$ ; ET-B;  $F_{\text{low}}=1\text{Hz}$ ;



Regions in the  $m_1$ - $m_2$  plane that corresponds to  $1\text{-}\sigma$  uncertainties in Newtonian, 1PN and 2.5PN coefficients in the PN series.

Left panel: GR as the correct theory of gravity

Middle and Right Panel correspond to hypothetical non-GR theories of gravity which have phasing coefficients  $\psi_{5l}$  (2.5PN) and higher differing from the GR values by 1% and 10%