

Galaxy Formation, Dark Matter Substructure & Reionization

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IAP 2007

Galaxy Formation, Dark Matter Substructure & Reionization

- CDM substructure on small scales
- “Via Lactea” Nbody simulation
- Subhalo population of MW
- “Missing satellite problem”
- DM annihilation and GLAST

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Halo substructure

In the standard paradigm of cosmological structure formation (Λ CDM) galaxies form hierarchically, with low-mass objects ("**halos**") collapsing earlier and merging to form larger and larger systems over time. **Halos collapsing at high redshift**, when the universe is very dense, have central densities that are correspondingly high.

$z=49.000$



B. Moore

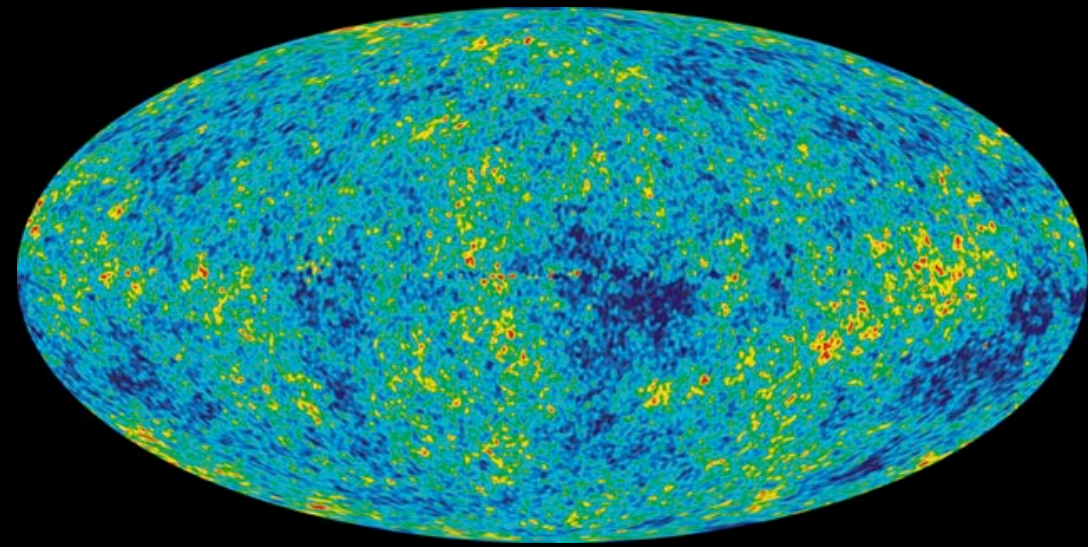
When these halos merge into larger hosts, their high densities allow them to resist the strong **tidal forces** that acts to destroy them.

Nbody simulations show that gravitational interactions unbind most of the mass associated with the merged progenitors, but it is expected a significant fraction of these small halos will **survive the hierarchical process as distinct substructure.**

B. Moore

It is therefore a clear, unique prediction of Λ CDM that galaxies are embedded in massive, extended dark matter halos teeming with self-bound substructure or "**subhalos**". High resolution Nbody simulations have confirmed that CDM halos both on cluster and galaxy scales are not smooth but are clumpy on all **resolved** mass scales.

What WIMP makes up the DM?



CMB, LSS, SN Ia, BBN \Rightarrow Λ CDM

WMAP-3yr (alone, flat prior): $\Omega_m=0.238$, $\Omega_b=0.042$

\Rightarrow 83% of the matter content of the universe is some non-baryonic, **very weakly interacting cold particle**

DM is “cold” or “not very warm”: Ly α forest, early reionization

We do not know what is, but we can still simulate its clustering properties under gravity...

Simulating CDM halos

collisionless (“pure N–body”, DM only) simulations

- assume all Ω_m is WIMP, and sample it with N particles
- bad approximation in the center of galaxies where baryons dominate
- simple physics: just gravity
- allows high resolution
- no free parameters (ICs known from CMB)

⇒ accurate solution to an idealized problem

hydrodynamical simulations

- computationally expensive, relatively low resolution (use AMR)
- hydro is complicated (SPH and grid codes often disagrees, see e.g. Agertz et al. 2006)
- important physical processes typically act on scales far below resolution (SF, SNe, etc) and are implemented through uncertain functions and free parameters

⇒ approximate solution to a more realistic problem

A brief history of Nbody simulations of CDM halos

log density

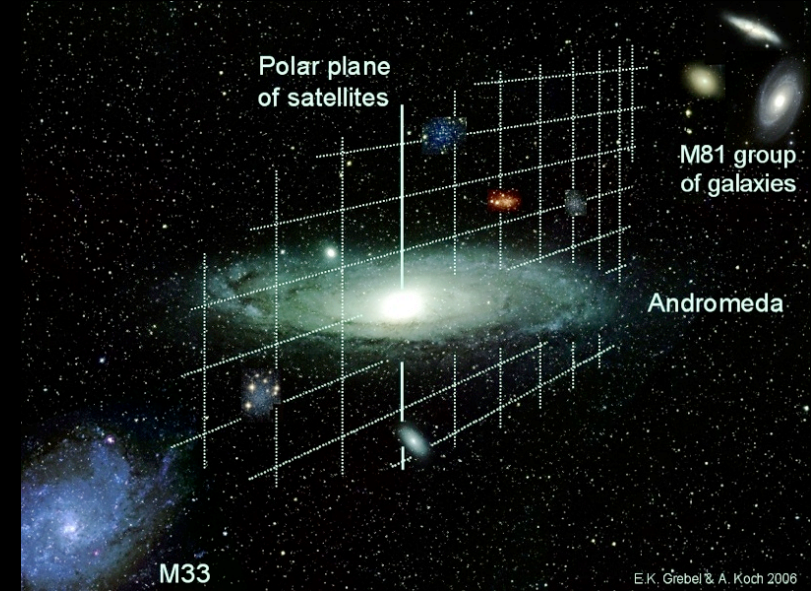
log phase space density

B. Moore

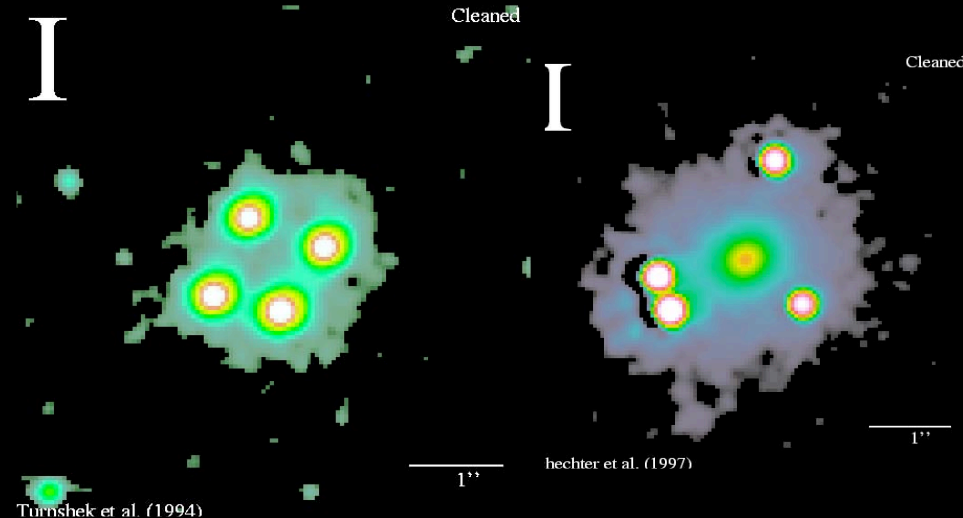
ability of subhalos to survive as substructure within the host is particularly sensitive to resolution issues

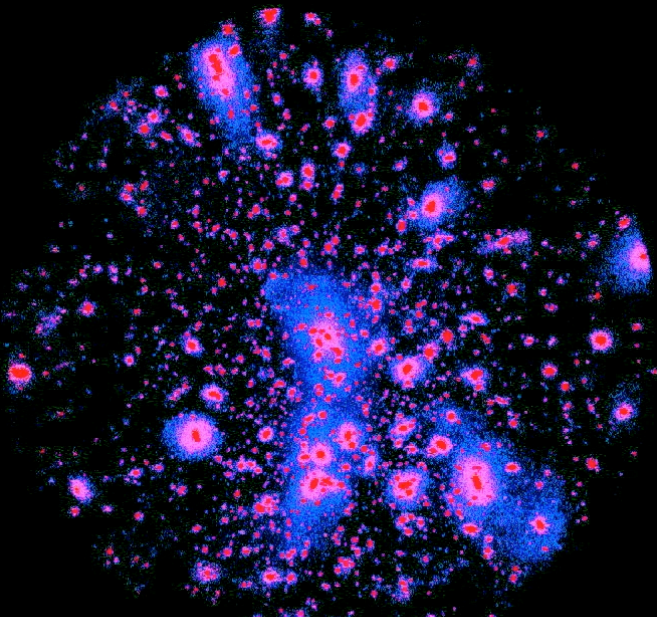
Observational probes of substructure

1. Satellite Galaxies of MW: the most massive DM subhalos are predicted to be associated with luminous dSph satellites. The amount and spatial distribution of satellites around the MW provide then unique information and clues on the galaxy assembly process. N.B. Most dark matter subhalos appear to have no optically luminous counterparts in the Local Group (“missing satellite problem” Moore +99; Klypin+99).



2. Gravitational Lensing: galaxy substructure may explain the flux ratio anomalies observed in multiply-imaged lensed QSOs (Metcalf & PM 01; Chiba 02; Dalal & Kochanek 02). Effect is sensitive to subhalo surface mass density in the inner 5–10 kpc.

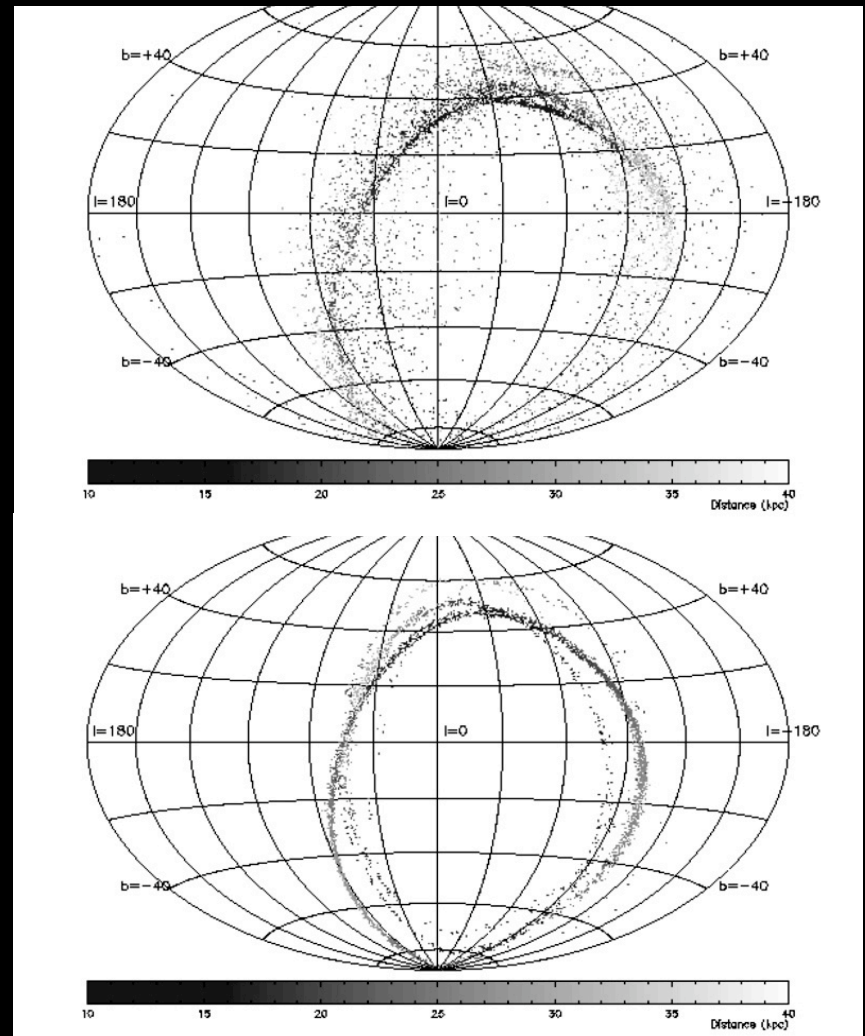




phase-space density ρ/σ^3 $z=0$ cluster

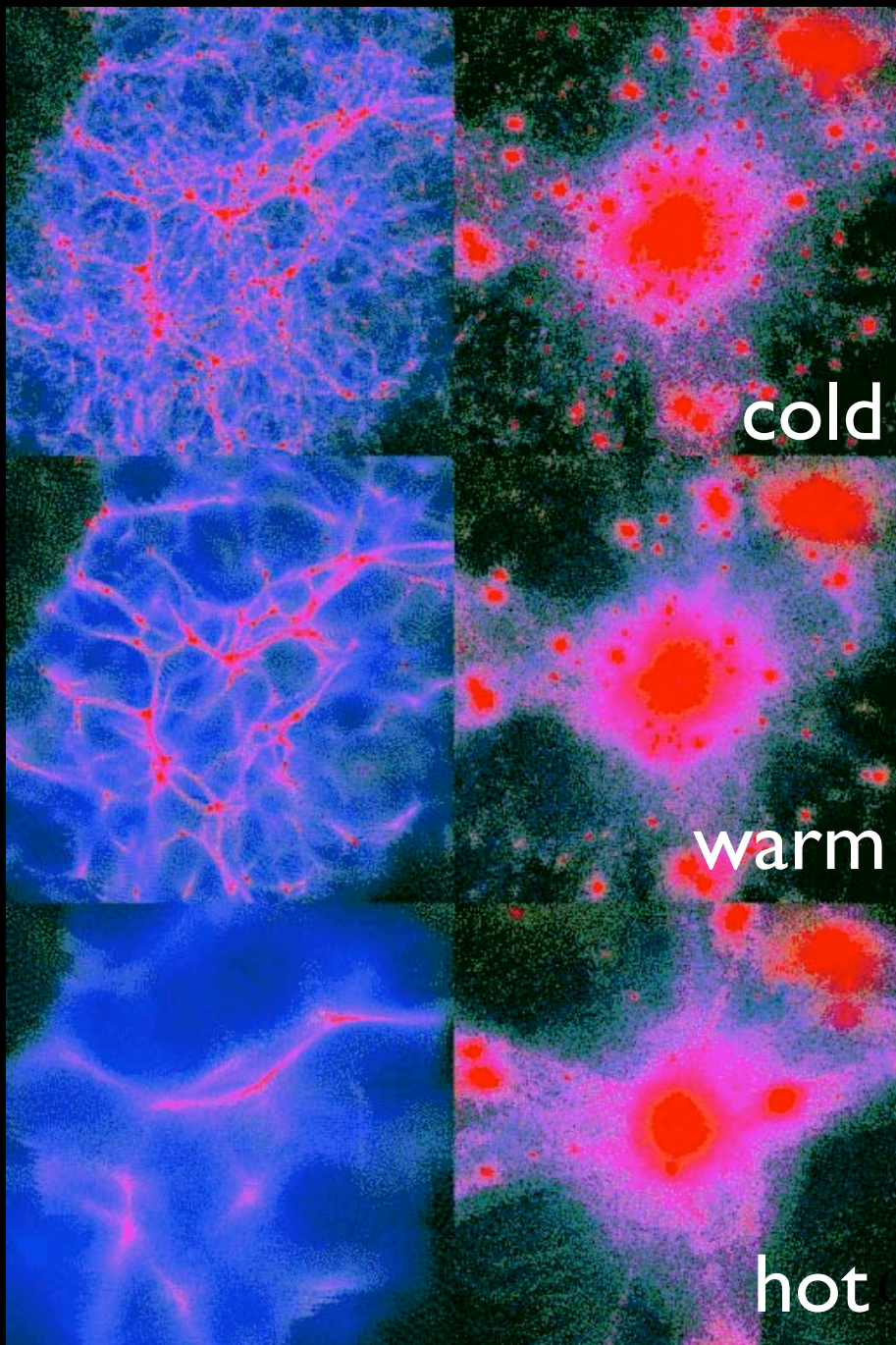
3. Dark Matter Annihilation: because of their high phase-space densities, subhalos may be detectable via γ -rays from DM particle annihilation in their cores (Bergstrom et al. 1999; Calcaneo-Roldan & Moore 2000; Stoehr et al. 2003; Colafrancesco, Profumo, & Ullio 2005; Diemand, Kuhlen, & Madau 2006): γ -ray luminosity $\propto \int \rho^2 dV$. (GLAST, VERITAS).

4. Tidal streams: presence of a population of CDM clumps alters the phase-space structure of a globular cluster tidal stream (Ibata+ 02). If the global Galactic potential is nearly spherical, this corresponds to a broadening of the stream from a thin great-circle stream into a wide band on the sky. (GC streams detectable by GAIA)



a galaxy cluster

Most like it cold

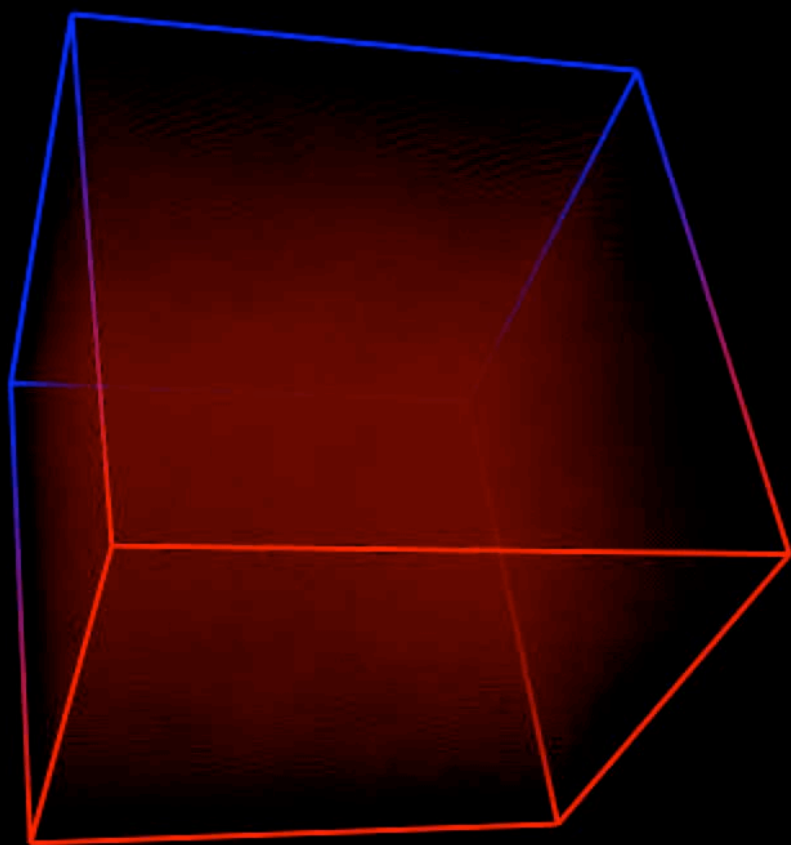


← 0.065 pc →

$z=86$ $M_{\text{vir}}=0.005 M_{\odot}$

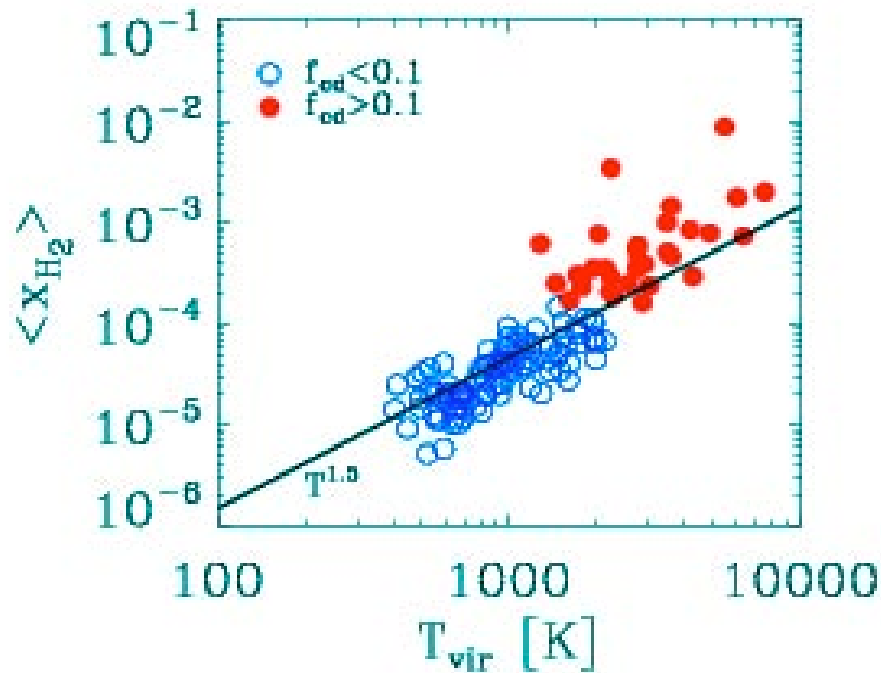
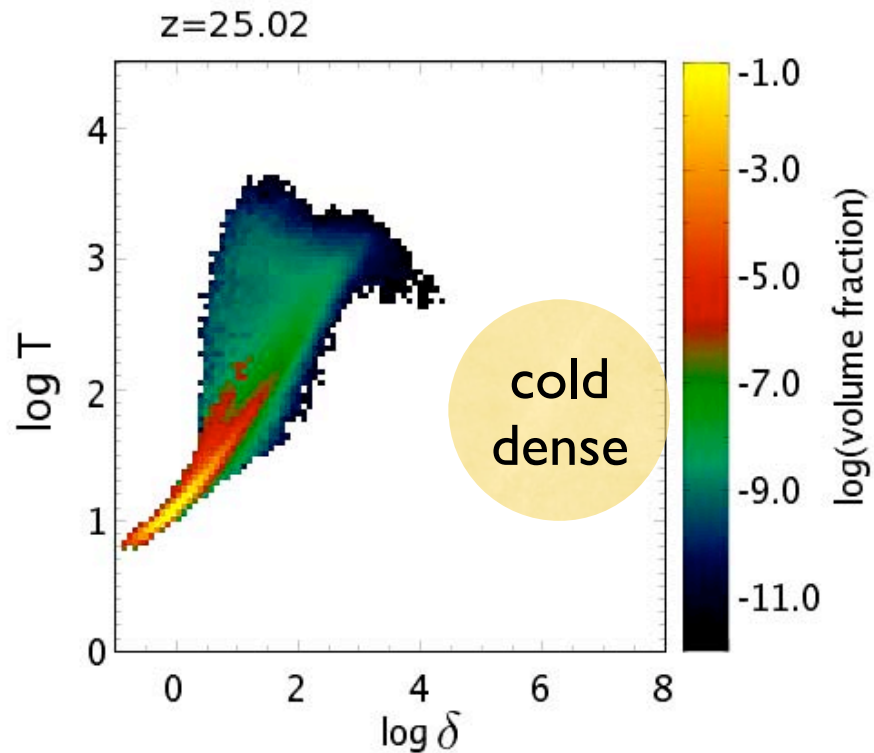
minimum scale for the gravitational aggregation of collisionless CDM $\sim M_{\oplus}$

From dark halos to first galaxies

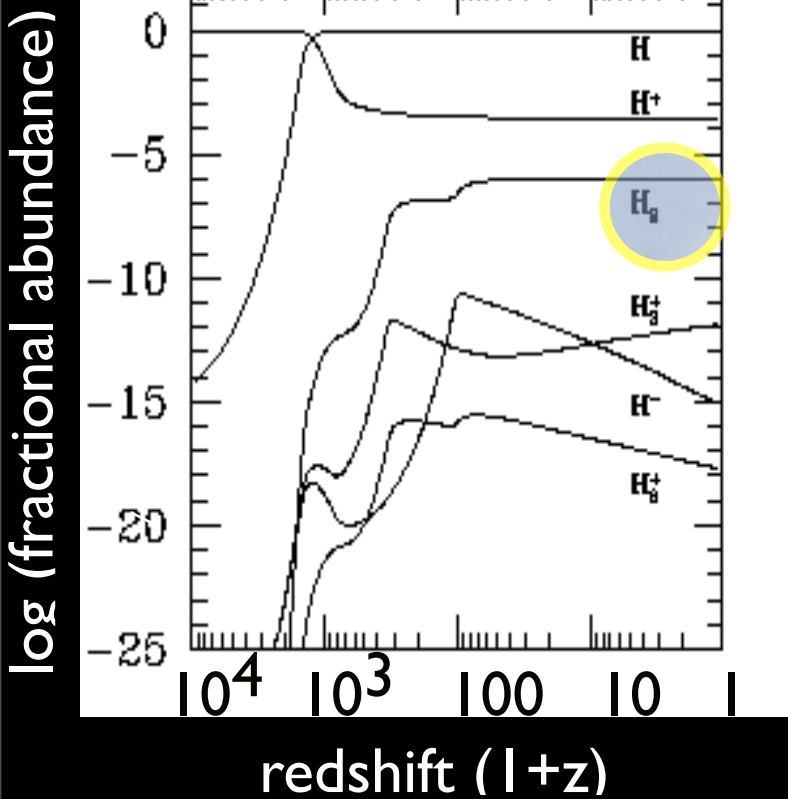


$z=98.01$

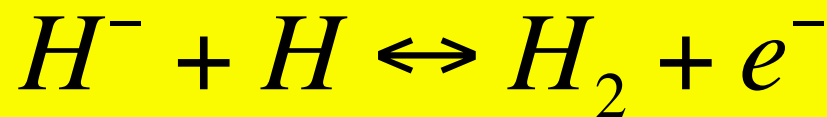
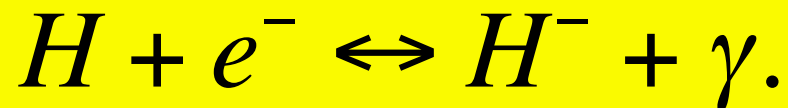
Kuhlen & PM 05



H₂ cooling and reionization

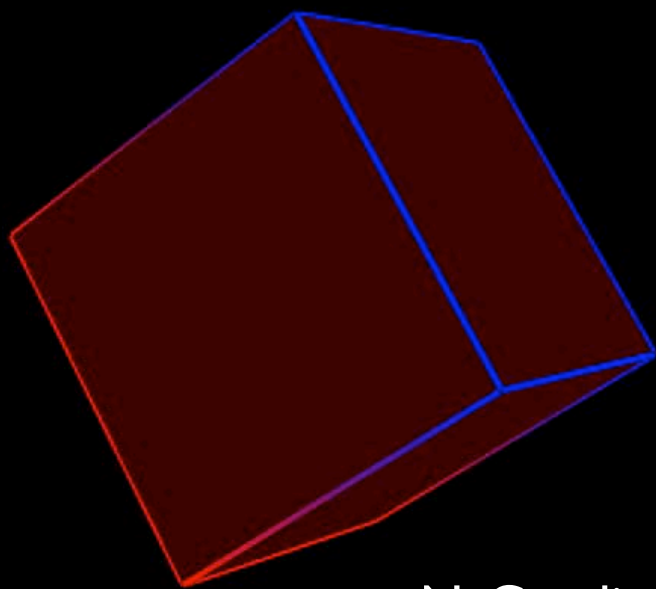


free electrons serve as catalysts for the formation of H₂ through the negative ion H⁻



H₂ is the main source of cooling in the first generation of gravitationally bound gas clouds

$$x_{H_2}(\text{IGM}) \sim 10^{-6} \Rightarrow t_{\text{cool}} \gg H^{-1}$$



N. Gnedin

Where are the hosts of the first stars today?

“VIA LACTEA”: the highest-resolution DM simulation of a Milky Way-sized halo

Largest DM simulation to date at these scales.
320,000 cpu hours
(36.5 cpu yrs)
213,217,920 high res particles embedded in a periodic 90 Mpc box sampled at lower resolution to account for tidal field.

$M_{\text{halo}} = 1.8e12 M_{\odot}$
 $r_{200} = 390 \text{ kpc}$
softening = 90 pc
 $m_p = 2e4 M_{\odot}$



**time resolution: adaptive
timesteps as short as
68,500yr=Hubble time/200,000**

**WMAP 3-year cosmology:
 $\Omega_M=0.238$, $\Omega_\Lambda=0.762$, $h=0.73$, $n=0.951$, $\sigma_8=0.74$**

**First simulation to resolve building blocks of galaxy formation
down to the present epoch**

by Juerg Diemand, Michael Kuhlen, and PM



a Milky Way dark matter halo simulated with 234 million particles on NASA's [Project Columbia](#) supercomputer

[main](#)

[movies](#)

[images](#)

[publications](#)

data (full snapshots, subhalo properties, histories etc. will become available in summer 2007)

movies

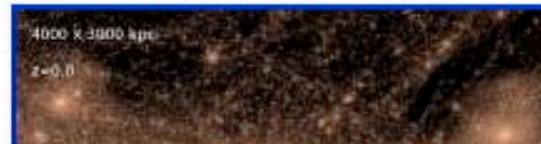
These animations show the projected dark matter density-square maps of the simulated Milky Way-size halo Via Lactea. The logarithmic color scale covers the same 20 decades in projected density-square in physical units in each frame. All movies are encoded in MPEG format and some are available in different quality versions.

the formation of the Via Lactea halo



- entire formation history ($z=12$ to 0): [high quality \(218MB\)](#)
smaller frames, quality: [high\(55MB\)](#) [medium\(11MB\)](#)
[low\(4.7MB\)](#)
- entire formation history, plus rotation and zoom at $z=0$:
quality: [high\(433MB\)](#) [medium\(72MB\)](#)
- early, active phase of merging and mass assembly ($z=12$ to 1.3):
[\(81MB\)](#)
- late, passive and stationary phase ($z=1.3$ to 0): [\(137MB\)](#)

rotation and zoom into the Via Lactea halo at $z=0$ (today)



$z=11.9$

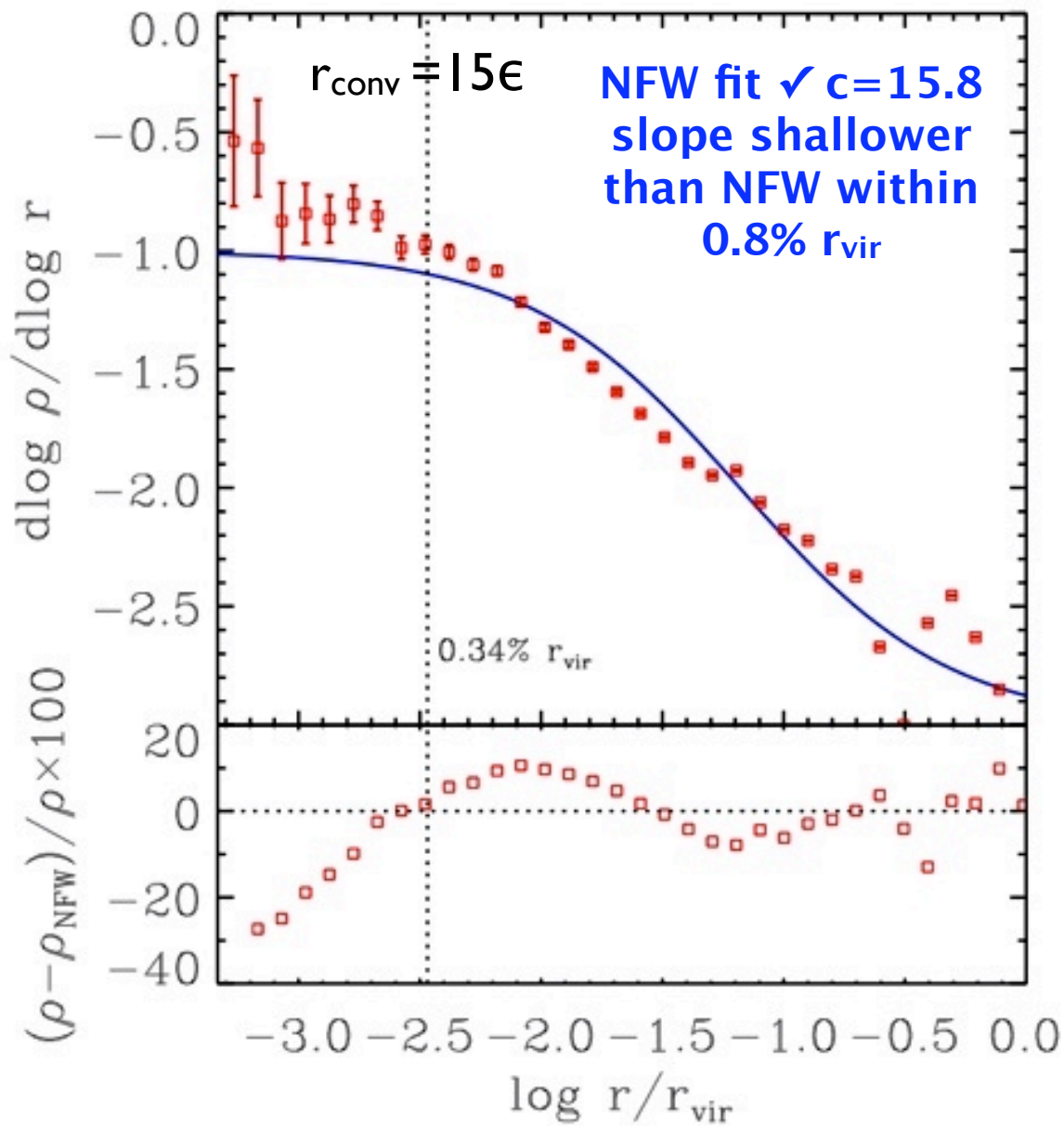
800 x 600 physical kpc

virial radius
@ $z=0$

Diemand, Kuhlen, Madau 2006

projected dark matter
density-square

Logarithmic slope of density profile



z=0.0 low resolution
3e6 vs 85e6 particles



80 kpc

$z=0.0$
3e6 vs 85e6 particles



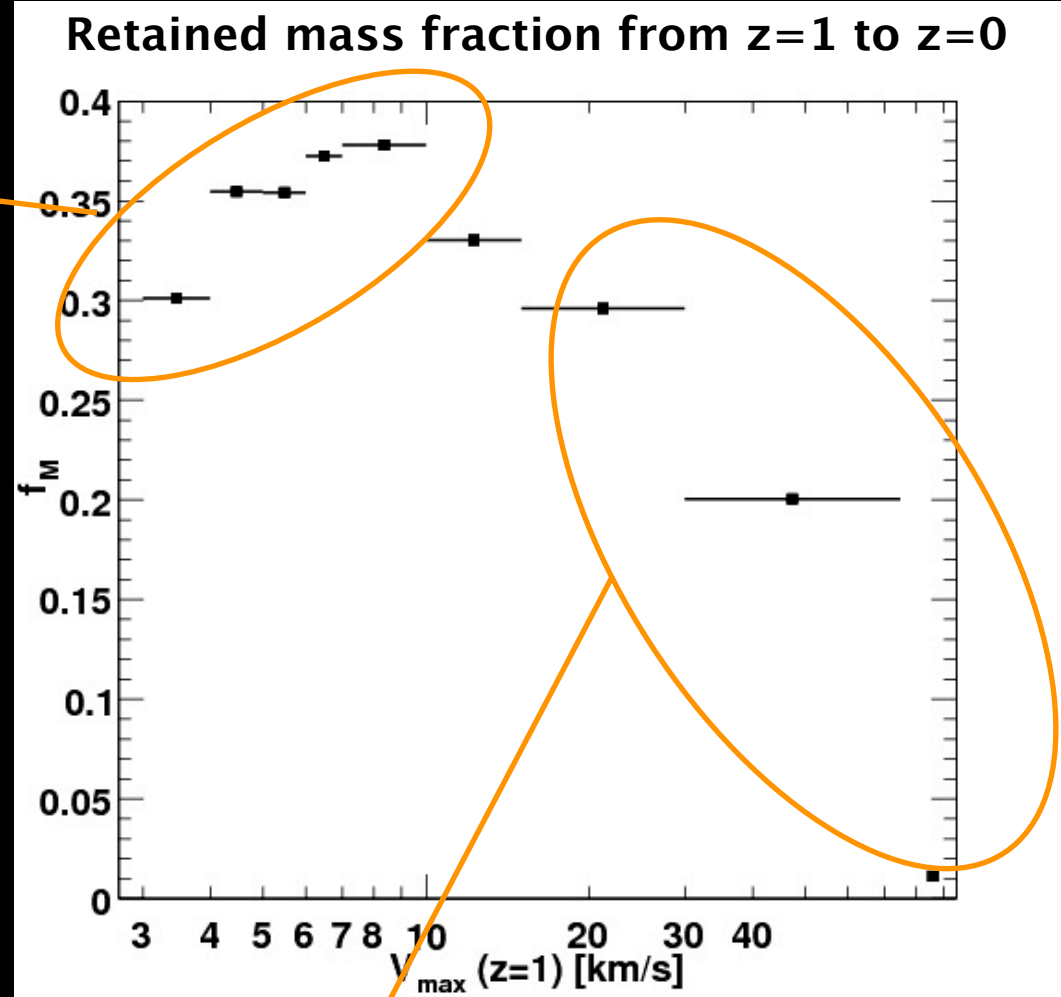
80 kpc

Tidal mass losses

smallest systems suffer from artificially large mass loss due to finite numerical resolutions

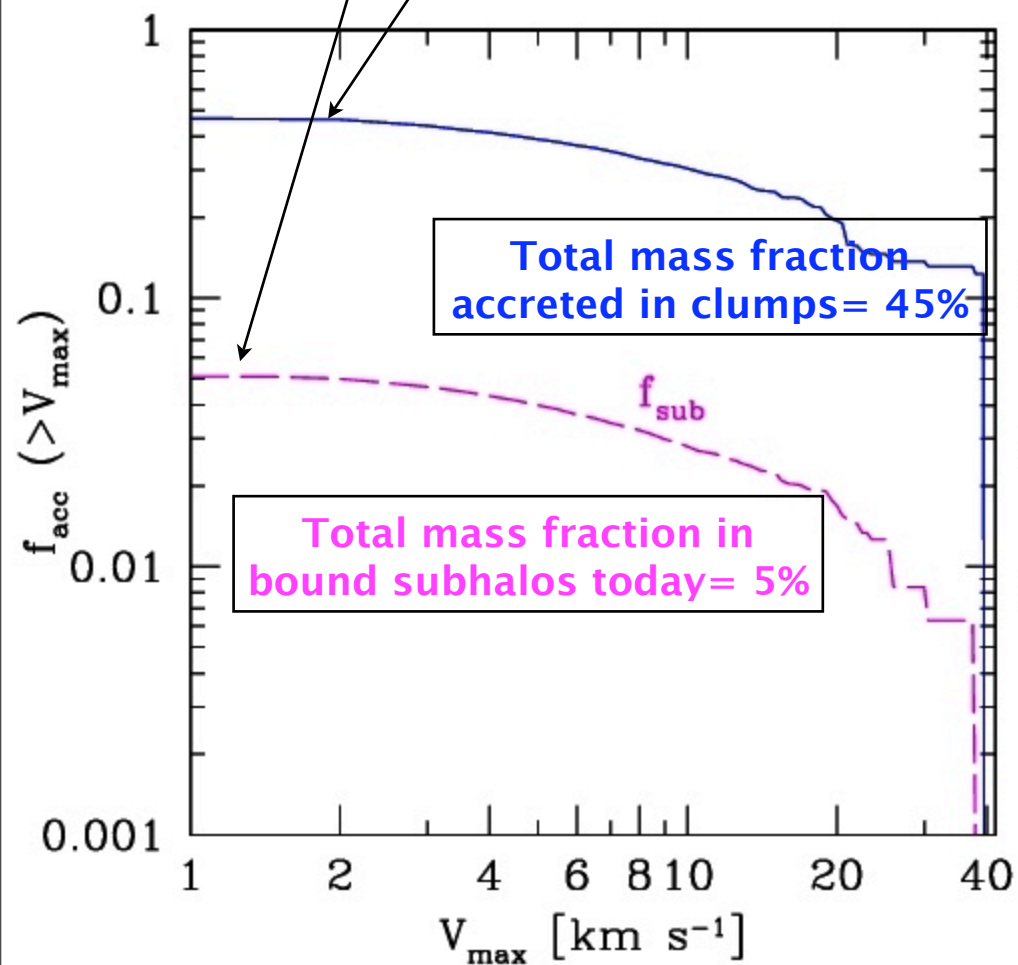
97% of the $z=1$ well resolved subhalos have a surviving bound remnant at $z=0$

the retained mass fraction is larger for initially lighter subhalos

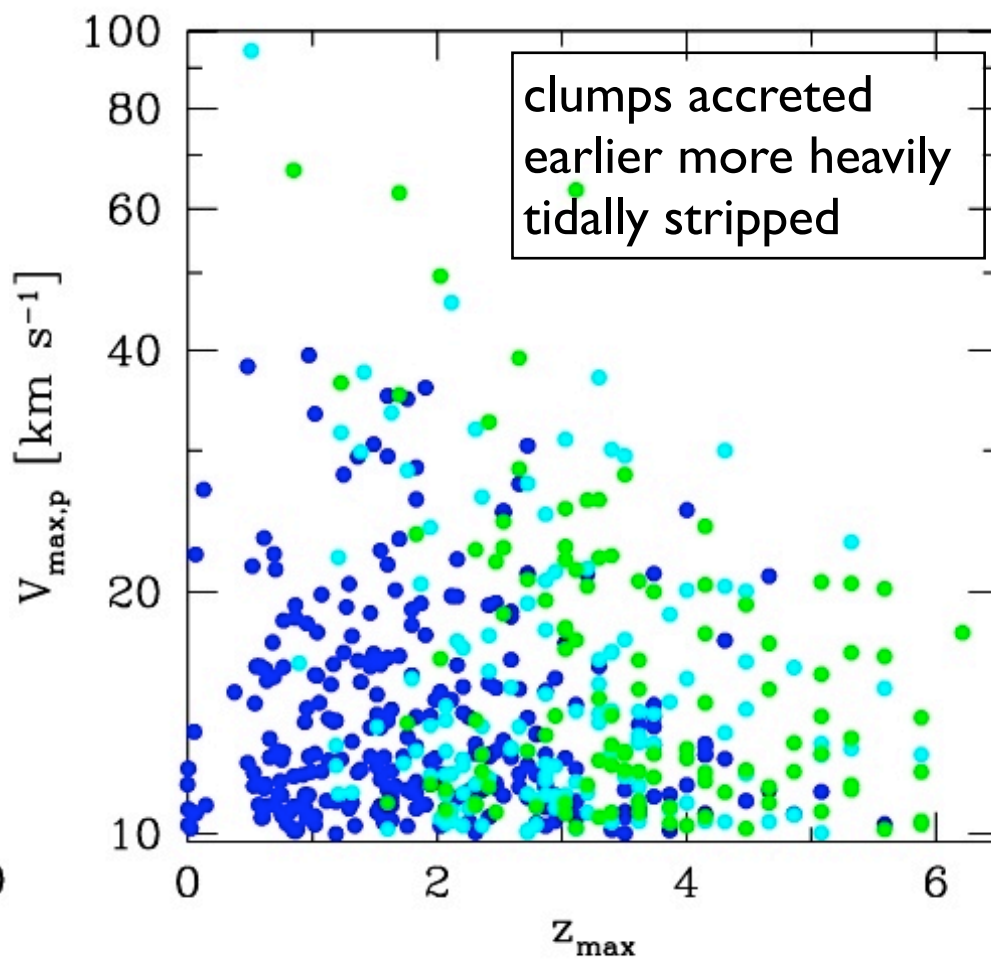


largest subhalos sink towards the center due to dynamical friction and retain a small fraction of their initial mass

numerical resolution



all 510 subhalos that reached $V_{\text{max,p}} > 10 \text{ km/s}$ at z_{max}

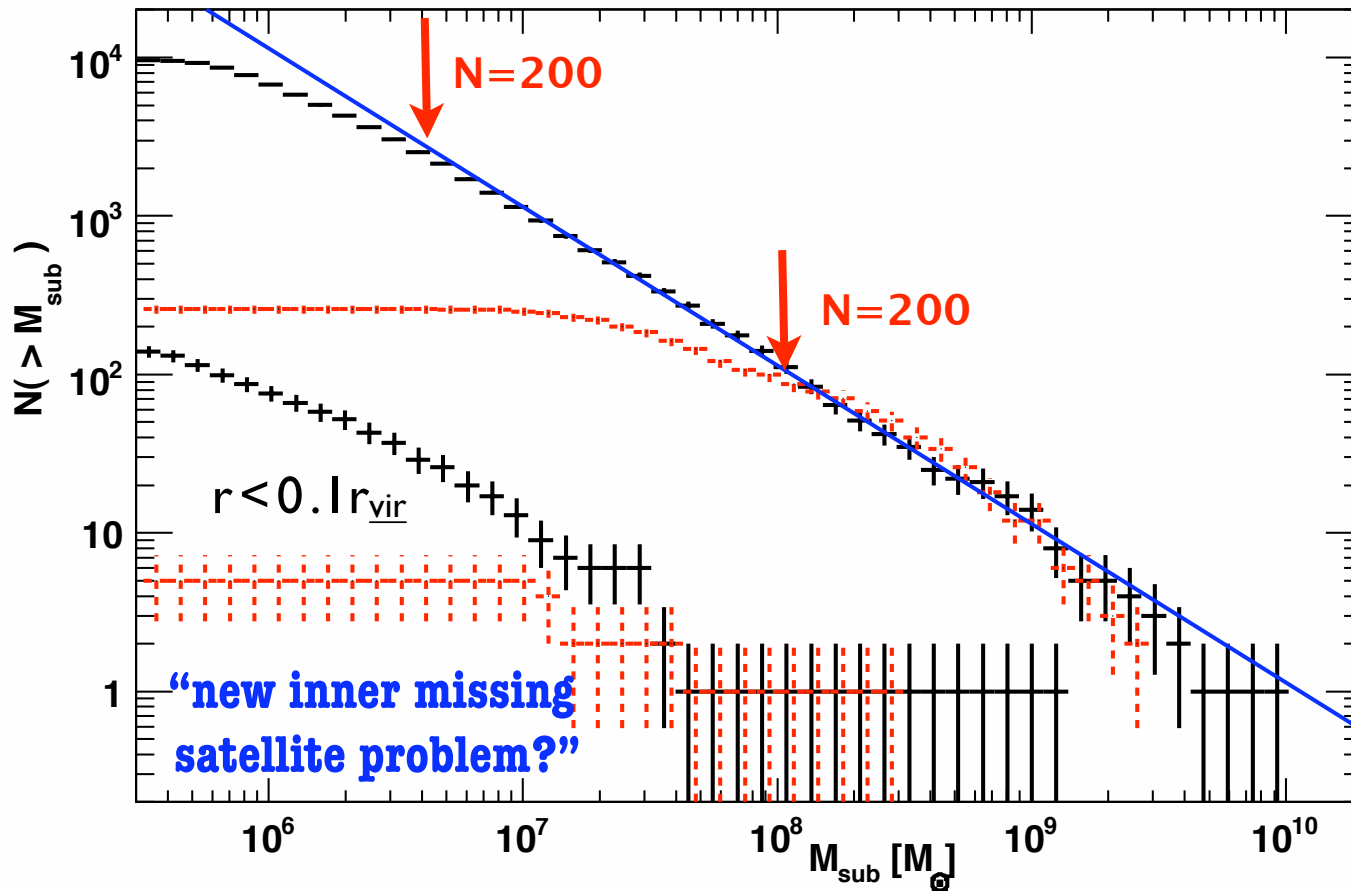


color coding: different ranges of V_{max} today

- $V_{\text{max}} < V_{\text{max,p}}/2$
- $V_{\text{max,p}}/3 < V_{\text{max}} < V_{\text{max,p}}/2$
- $V_{\text{max}} < V_{\text{max,p}}/3$

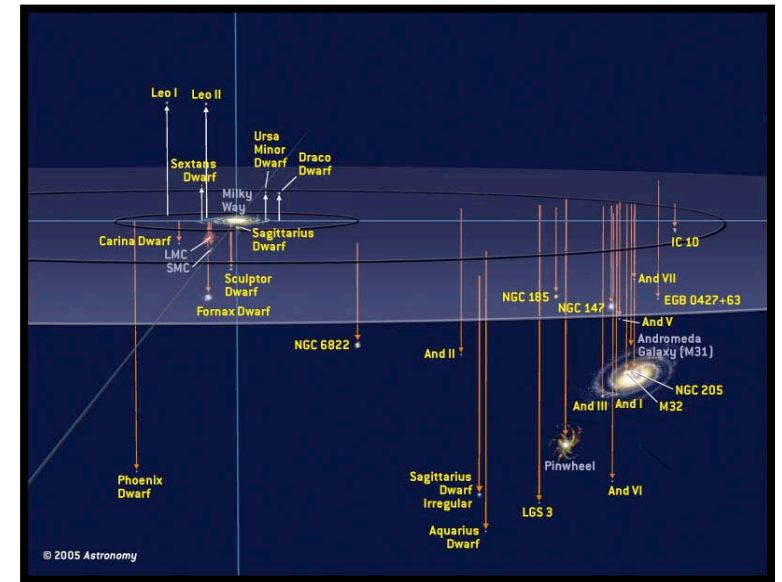
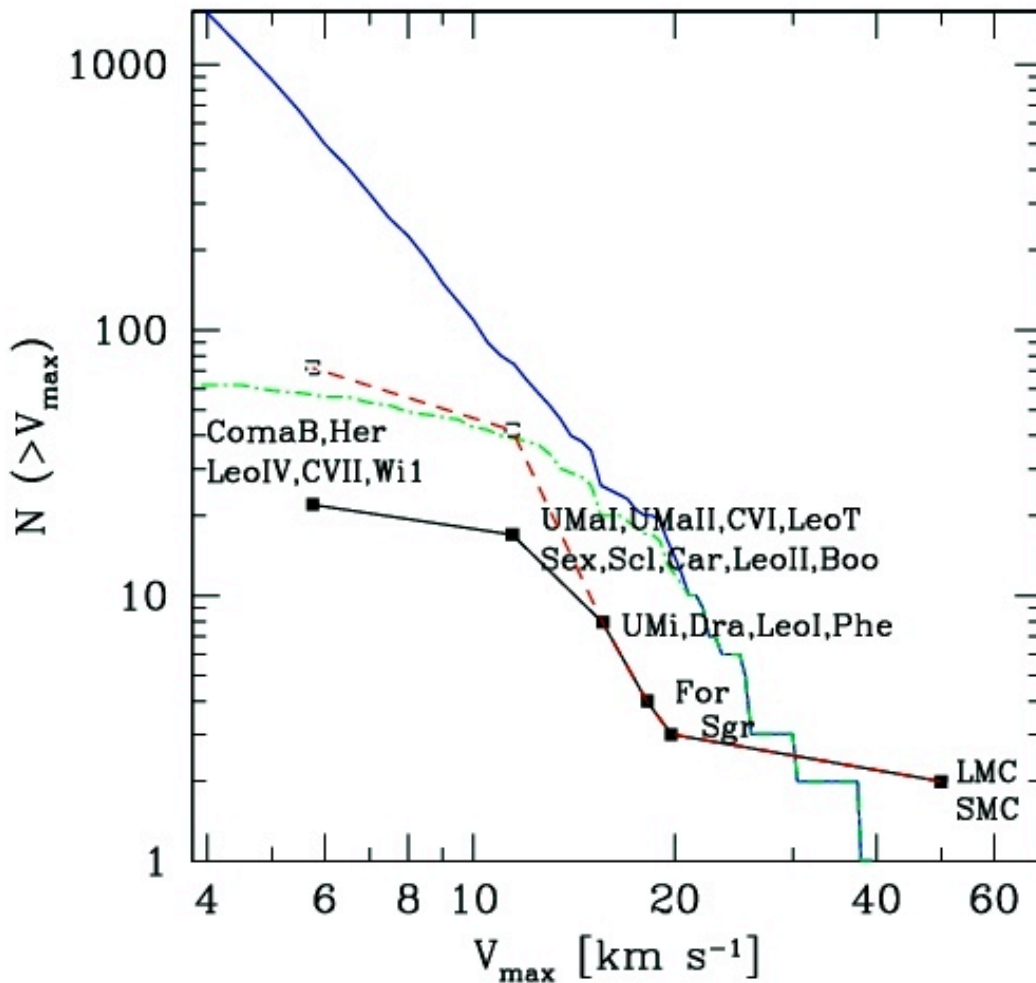
Subhalo mass function

6100 subhalos within r_{200} above $10^6 M_{\odot}$



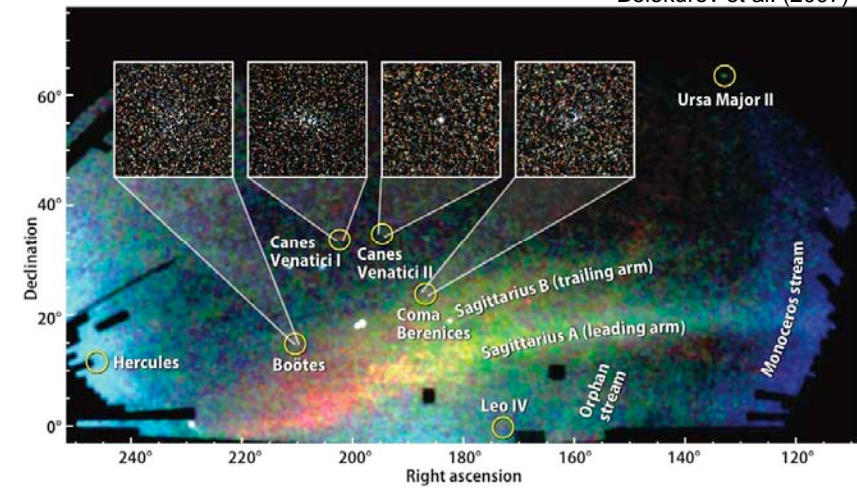
$N(> M_{\text{sub}}) \propto 1/M_{\text{sub}}$
mf steeper at high M
due to dynamical friction/tidal mass losses
shallower at low M due to numerical limitations

The substructure problem



SDSS is still discovering more dwarfs.

Belokurov et al. (2007)



NB comparison traditionally assumes $\sqrt{3}\sigma_* = V_{\max}$. Dark halos extend well beyond the stellar radius of a satellite \Rightarrow stellar kinematics alone provide only a lower limit on the halo V_{\max} value.

Are there many more ultra-faint Milky Way companions waiting to be discovered below $\mu_V=27-28$ mag arcsec⁻²?

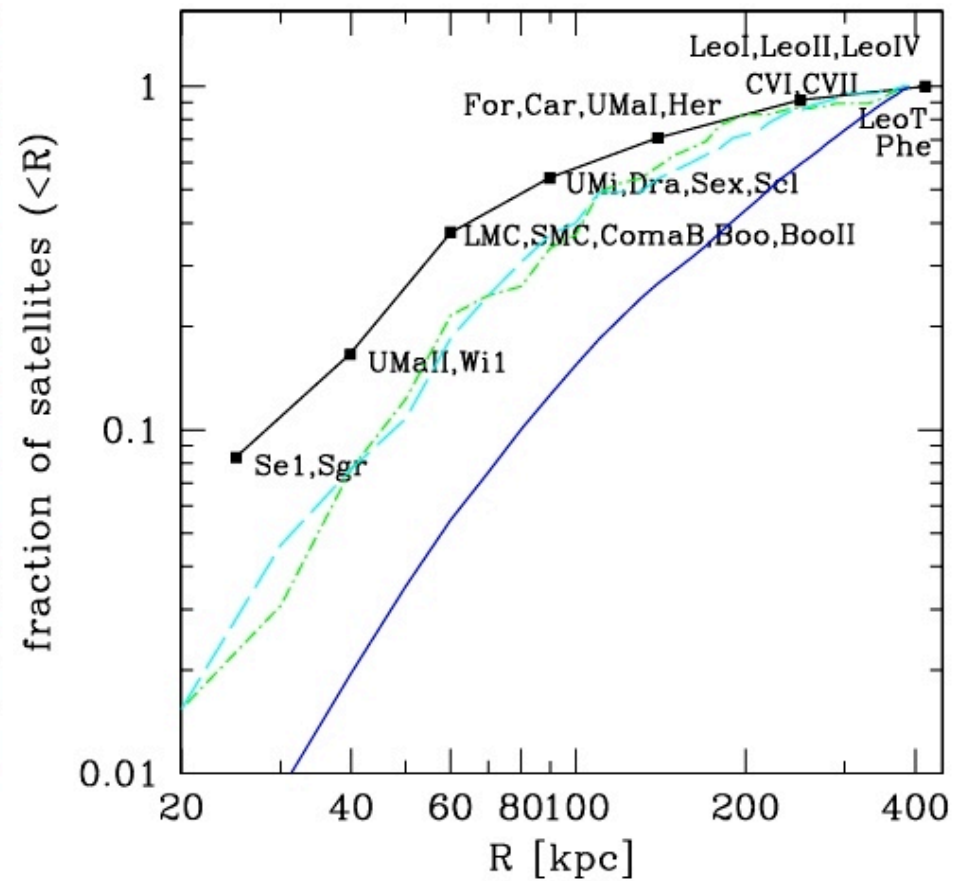
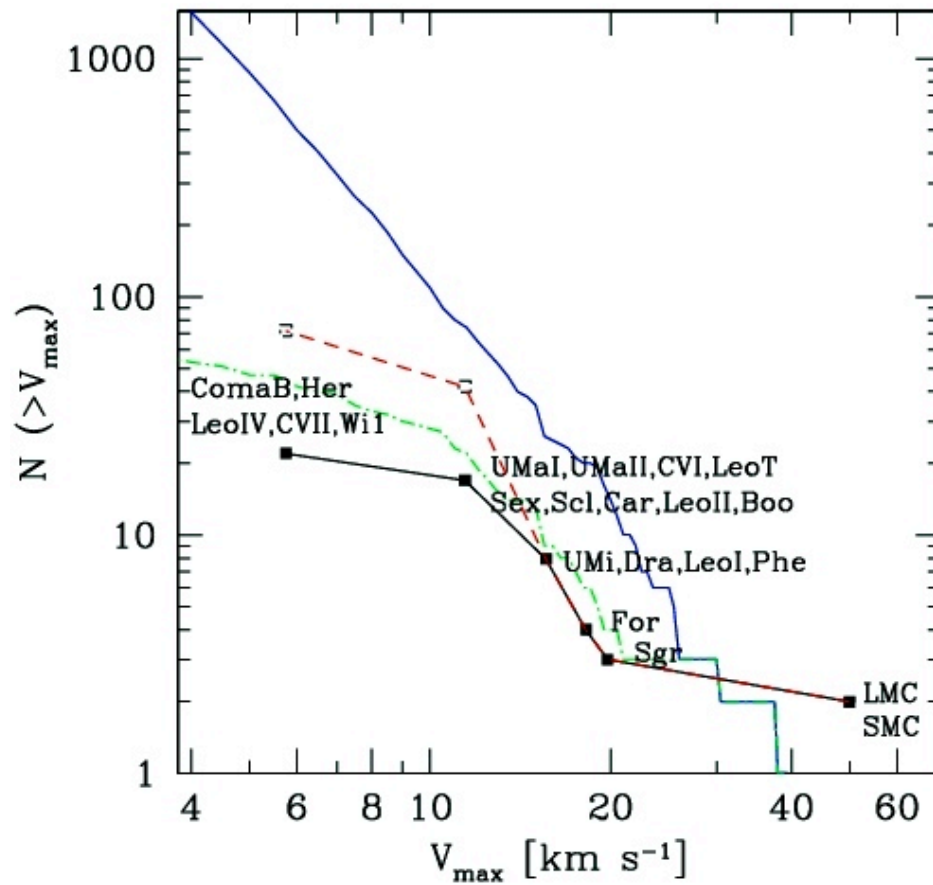
Via Lactea predicts 1000 satellites with $M_{\text{sub}} > 10^7 M_{\odot}$ ($>$ Leo T, Leo IV, Coma B, CVII)

Leo T (Irwin et al. 2007)

$M(\text{H I}) > 10^5 M_{\odot}$ and $L > 10^{3-4} L_{\odot}$

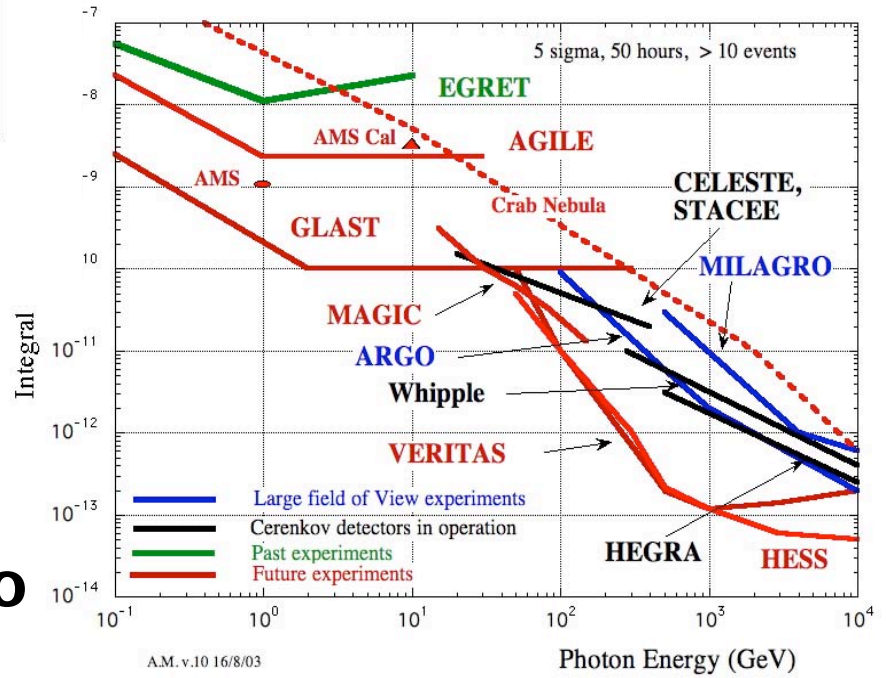
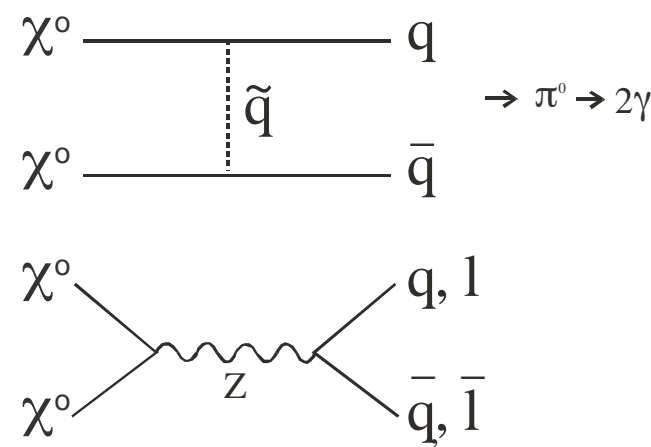
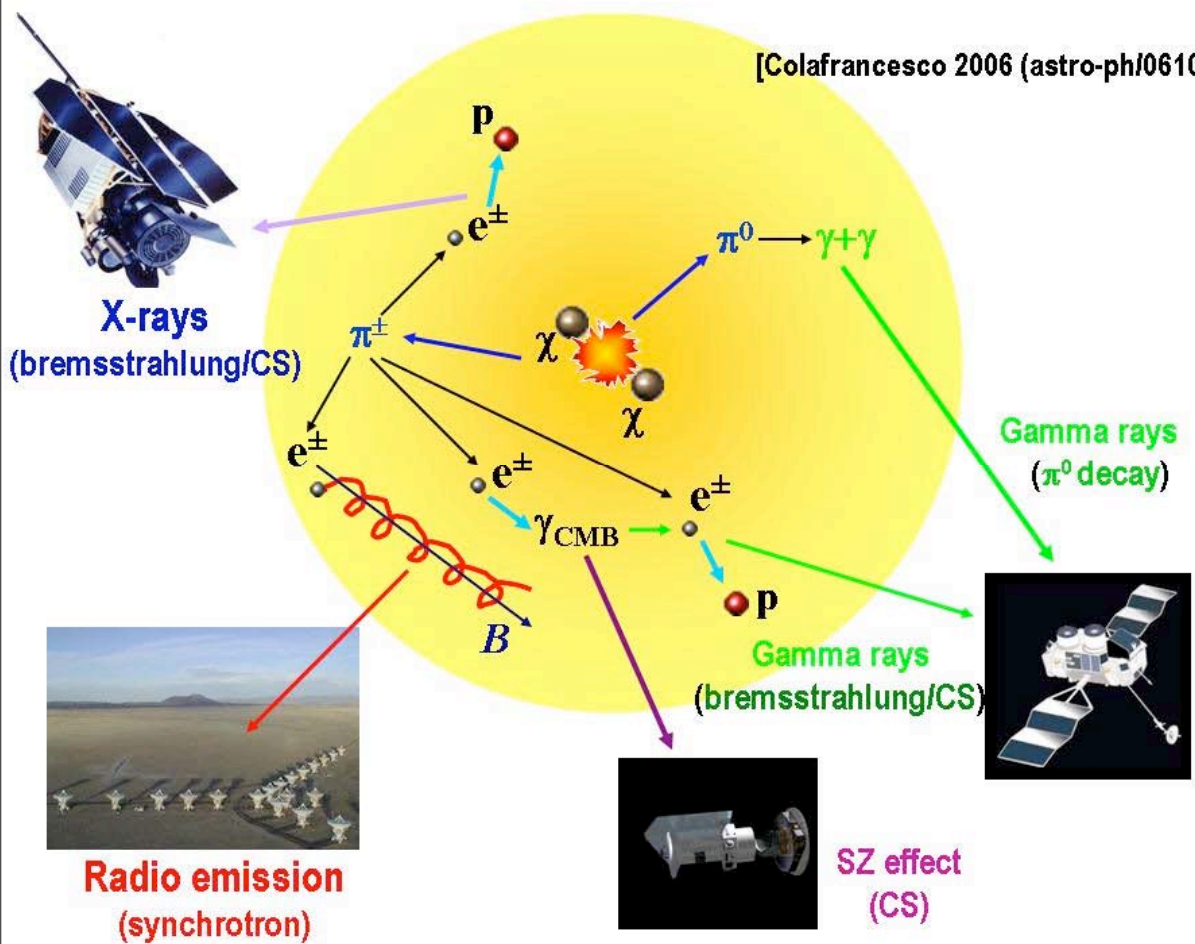
Need a very efficient feedback mechanism quenching SF for $V_{\text{max}} < 20$ km/s (today)
 $V_{\text{max,p}} < 35$ km/s (past)

Radial distribution of subhalos



DM not so dark?

[Colafrancesco 2006 (astro-ph/0610521)]



Minimal Supersymmetric Extension of Standard Model favors neutralino as main DM constituent

Annihilation flux for a distant spherically symmetric system of radius r_{vir} :

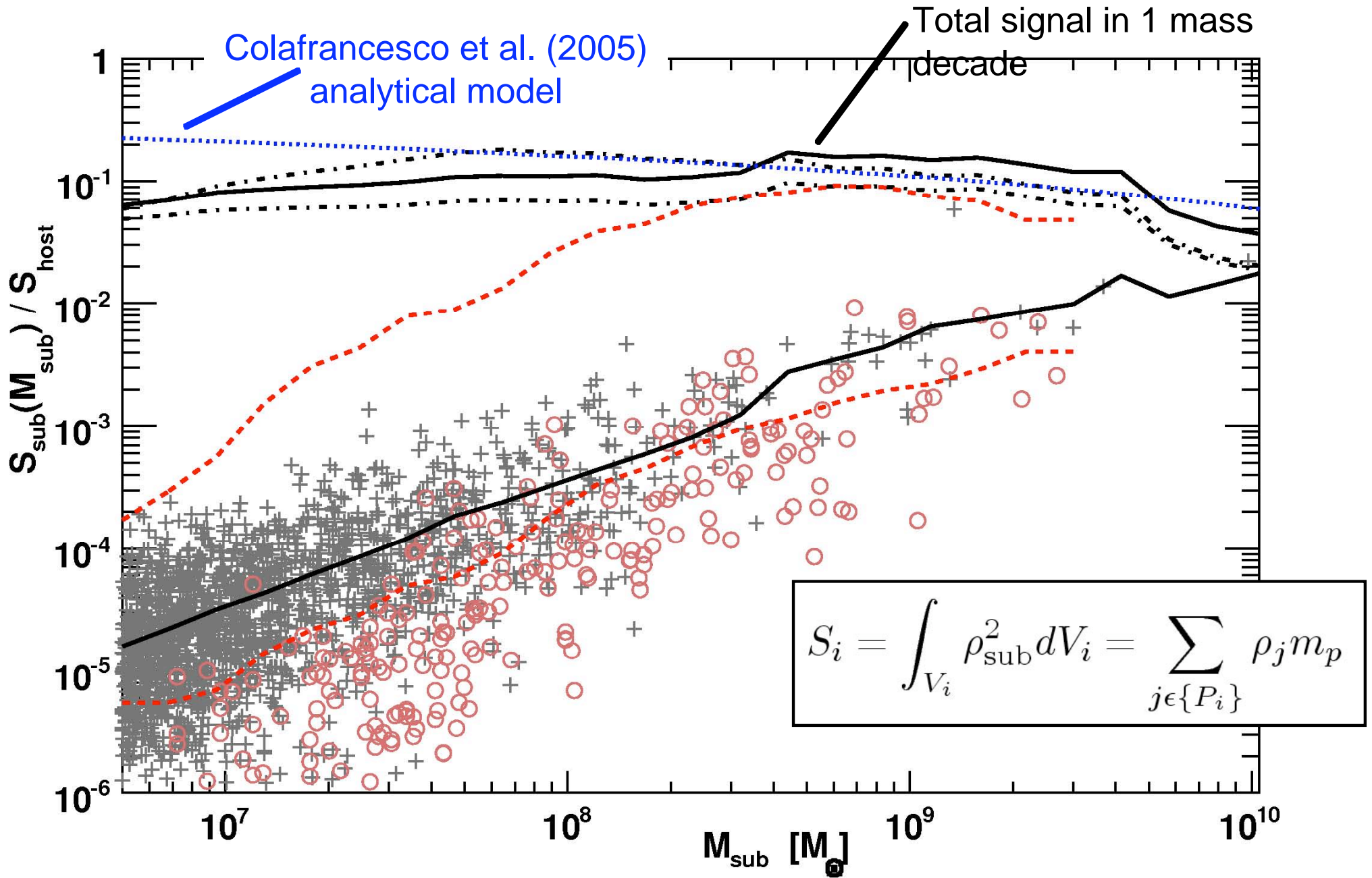
$$F = \frac{N_\gamma \langle \sigma v \rangle}{2 d^2 m_\chi^2} \int_0^{r_{\text{vir}}} \rho_{DM}^2(r) r^2 dr$$

Diagram illustrating the components of the annihilation flux equation:

- N_γ : γ -photons produced per annihilation
- $\langle \sigma v \rangle$: annihilation cross-section x thermal velocity
- m_χ^2 : mass of DM particle

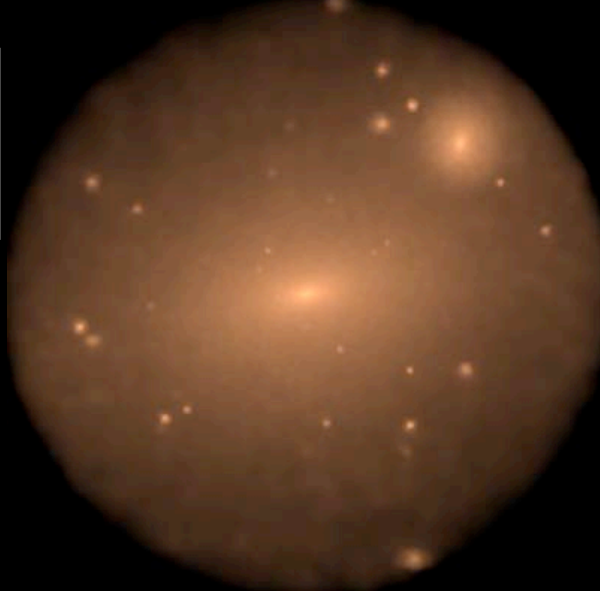
The density squared weighting of the integrand results in most of the flux in dark DM halos being produced by a small fraction of their mass in the densest regions: (1) galactic center and (2) halo substructure

subhalo annihilation luminosity vs. M_{sub}

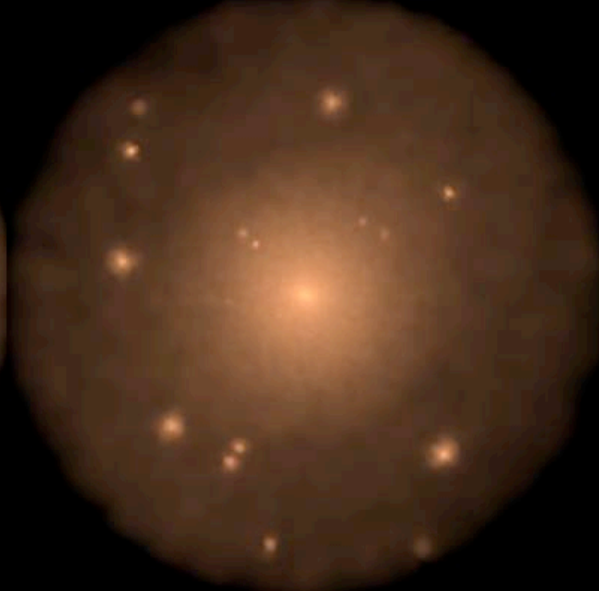


Sub-subhalos resolved in most massive satellites!

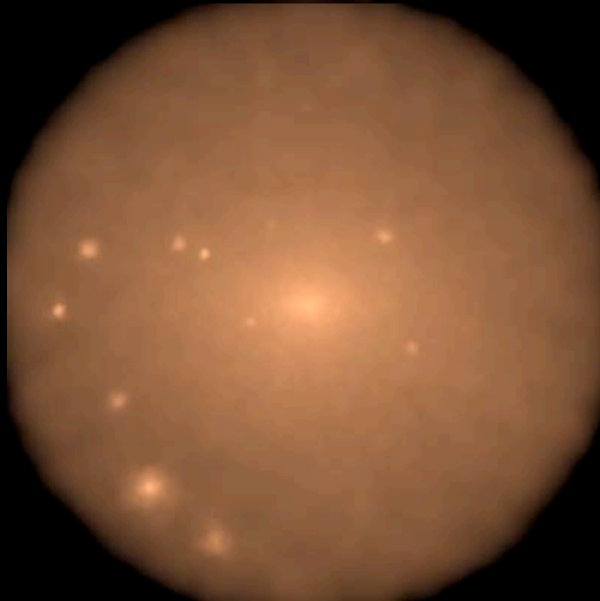
$M_{\text{sub}} = 9.8e9 M_{\odot}$
 $r_t = 40.1 \text{ kpc}$
 $D = 345 \text{ kpc}$



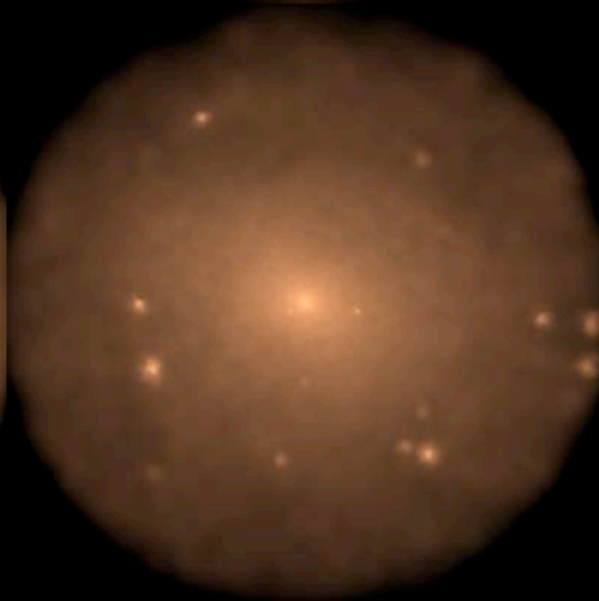
$M_{\text{sub}} = 3.7e9 M_{\odot}$
 $r_t = 33.4 \text{ kpc}$
 $D = 374 \text{ kpc}$



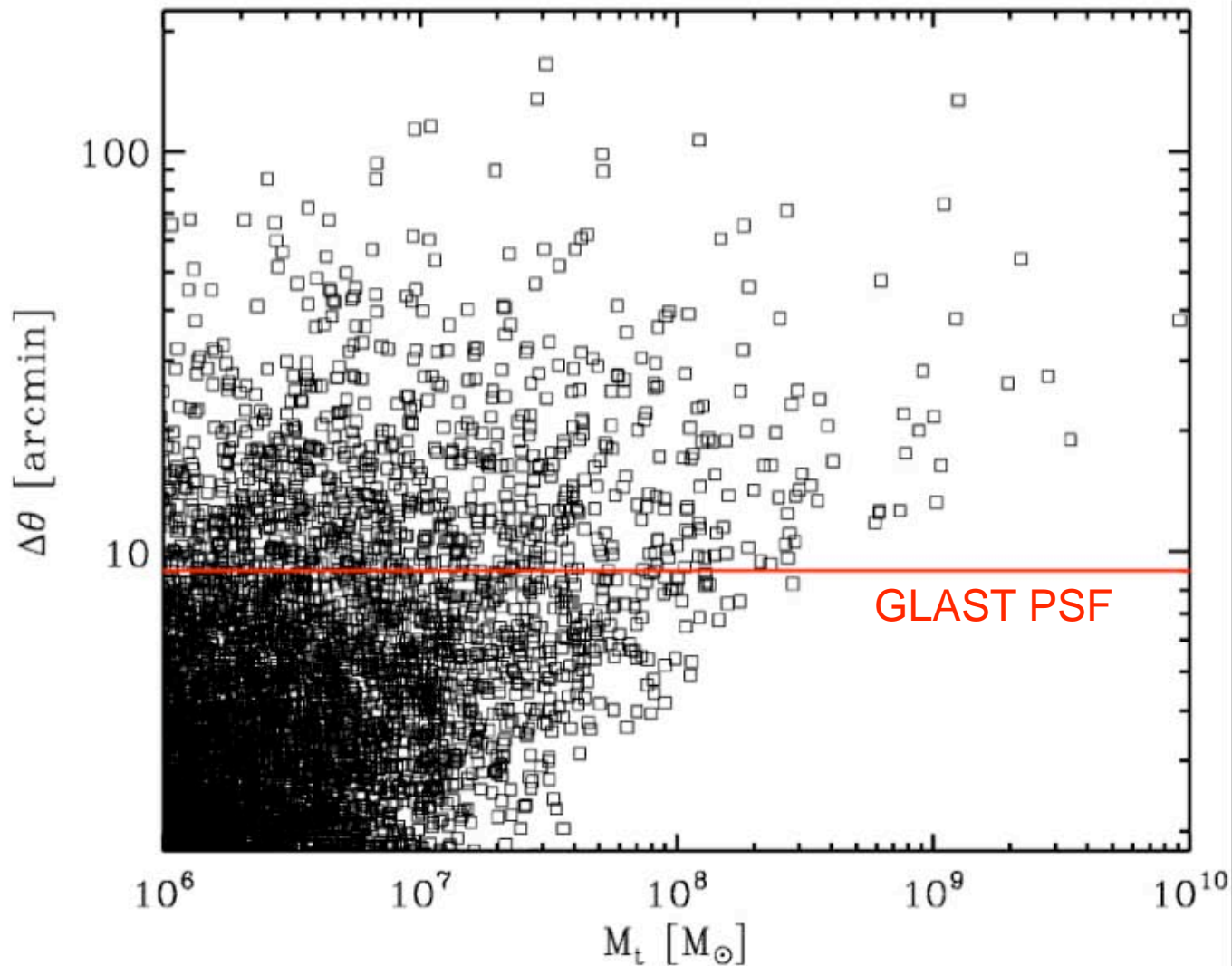
$M_{\text{sub}} = 3.0e9 M_{\odot}$
 $r_t = 28 \text{ kpc}$
 $D = 280 \text{ kpc}$



$M_{\text{sub}} = 2.4e9 M_{\odot}$
 $r_t = 14.7 \text{ kpc}$
 $D = 185 \text{ kpc}$



subhalo density (tidal radius) = 2 background density
subhalo tidal mass = total mass (< tidal radius) \leq bound mass



$\Delta\theta$ = angle subtended
by twice the subhalo's
scale radius r_s .

For an NFW profile 90%
of the flux originates
from within r_s .

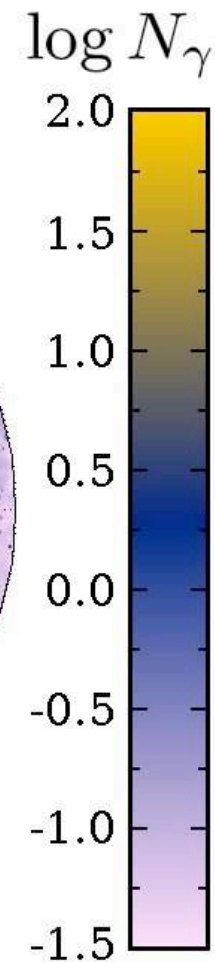
the brightest subhalos would be extended sources for **GLAST**
(PSF 9 arcmin at 10 GeV)

GLAST allsky map of neutralino DM annihilation



$$\langle\sigma v\rangle = 5 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$
$$M_\chi = 46 \text{ GeV}$$

2-year exposure
9 arcmin pixel



observer @ 8 kpc from GC
subhalo boost factor=10

Conclusions

- The highest-resolution simulation to date of the CDM halo of the Milky Way predicts the existence of more than **2,000 bound subhalos with $M_{\text{sub}} > 4 \times 10^6 M_{\odot}$** , distributed approximately with equal mass per decade of mass (a similar steeply rising subhalo mass function is also present at redshift $z=0.5$ in an elliptical-sized halo simulated with comparable resolution).
- the fraction of Via Lactea mass brought in by subhalos that have a surviving bound remnant today within r_{200} is 45%. About 10% of the material they brought in remains in self-bound identifiable substructure at the present-epoch.
- because of tidal mass loss, the number of massive Galactic subhalos that reached a peak circular velocity of **$V_{\text{max}} > 10$ km/s** throughout their lifetime exceeds 500, **5 times larger than their present-day abundance** and more than **twenty times** larger than the current (incomplete) tally of observed dwarf satellites of the Milky. **Any mechanism that suppresses star formation in small halos must start acting early, at redshift $z > 3$.**

- unless the **circular velocity profiles of Galactic satellites** peak at values significantly higher than expected from the **stellar line-of-sight velocity dispersion**, **only 1 out of 5 subhalos with $V_{\max} > 20$ km/s** today must be housing a luminous Milky Way dwarf.
- **nearly 600 halos with masses greater than $10^7 M_{\odot}$ are found today in the “field” between 400 and 600 kpc** i.e. small dark matter clumps appear to be relatively inefficient at forming stars even well beyond the virial radius.

Coming next: “Super Via Lactea”, a 10^9 DM particle simulation (DOE INCITE, 1.5 M cpu h)

THE END