



Structure and evolution of planets and their host stars

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**On the structure and evolution of planets and their host stars – effects
of various heating mechanisms on the size of giant gas planets**

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Outlines

New methods for determination of metallicity (Z) and age (t) of the host stars.

- $[Fe/H]$? $[O/H]$?

Heating processes in inflated planets (gas giants).

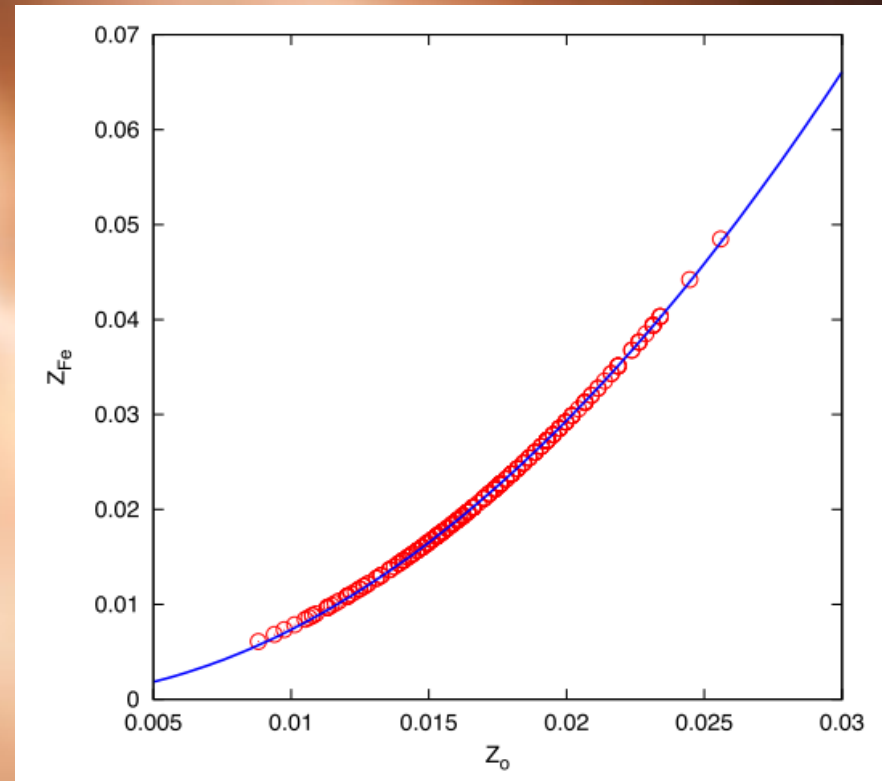
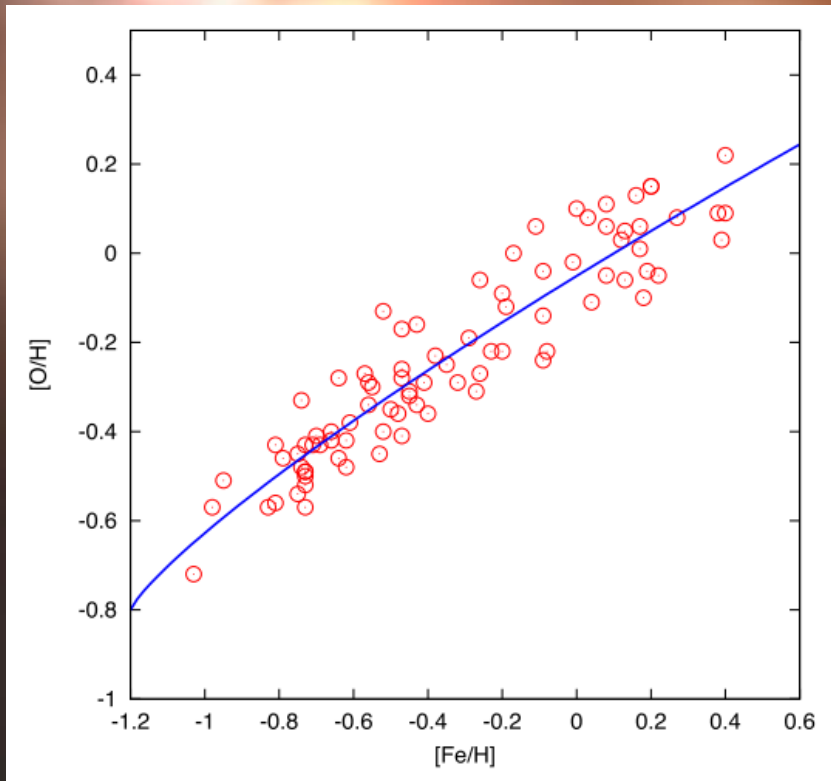
Data from TEPCat (Southworth 2011)

- Irradiation
- Tidal interaction
- Molecular dissociation
- Evaporation
- Effects of metallicity and cooling

Conclusions

Metallicity from [Fe/H] or [O/H]?

Oxygen is the most abundant heavy element.



Edvardsson et al. (1993).

Stellar Mass-radius relation – Energy transfer in outer regions

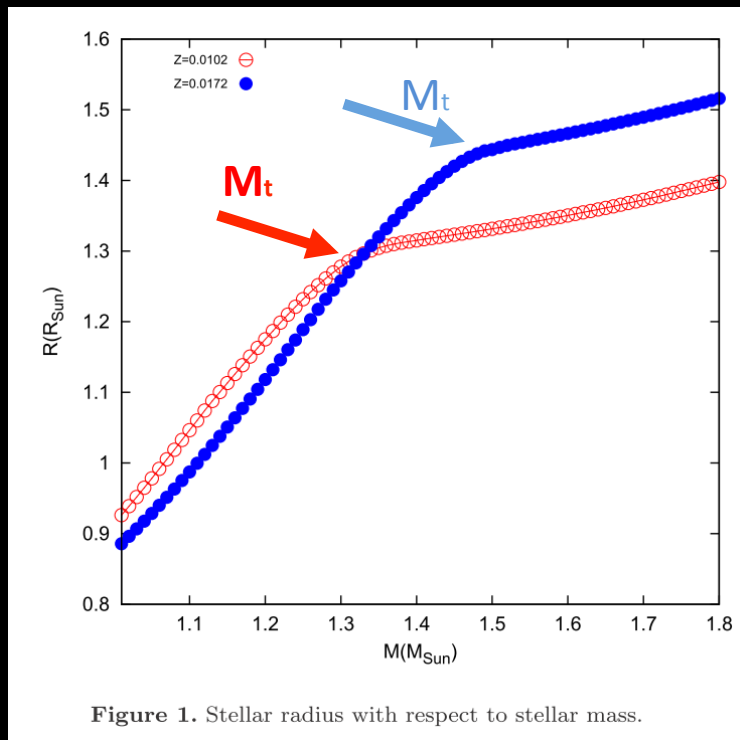
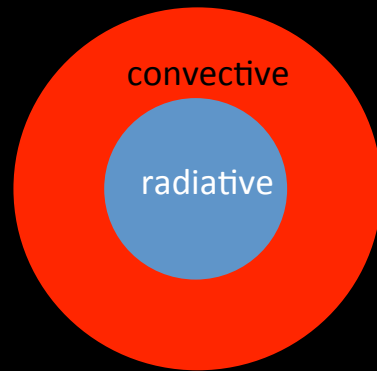
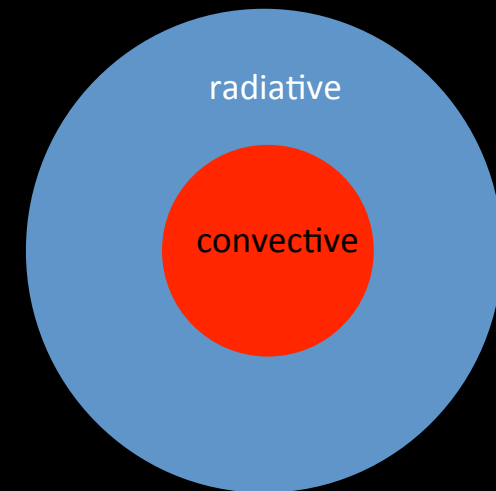


Figure 1. Stellar radius with respect to stellar mass.



Notes

- 1) Two different slopes for $M < M_t$ and $M > M_t$.
- 2) M_t depends on metallicity.
- 3) Slopes do not depend on Z .

Computation of Stellar Age: ANKI models

$$\frac{R(t)}{R_{\odot}} = \frac{R_{\text{ZAMS}}}{R_{\odot}} + a(M, Z)t_{\text{rel}}^{3/2},$$

$$t_{\text{rel}} = \frac{t}{t_{\text{TAMS}}}$$

$$a(M, Z) = 0.114b \left(\left(\frac{M}{8.8 M_{\odot}} \right)^5 + 1 \right) + (0.222 - b) \left(\frac{M}{M_{\odot}} \right)$$

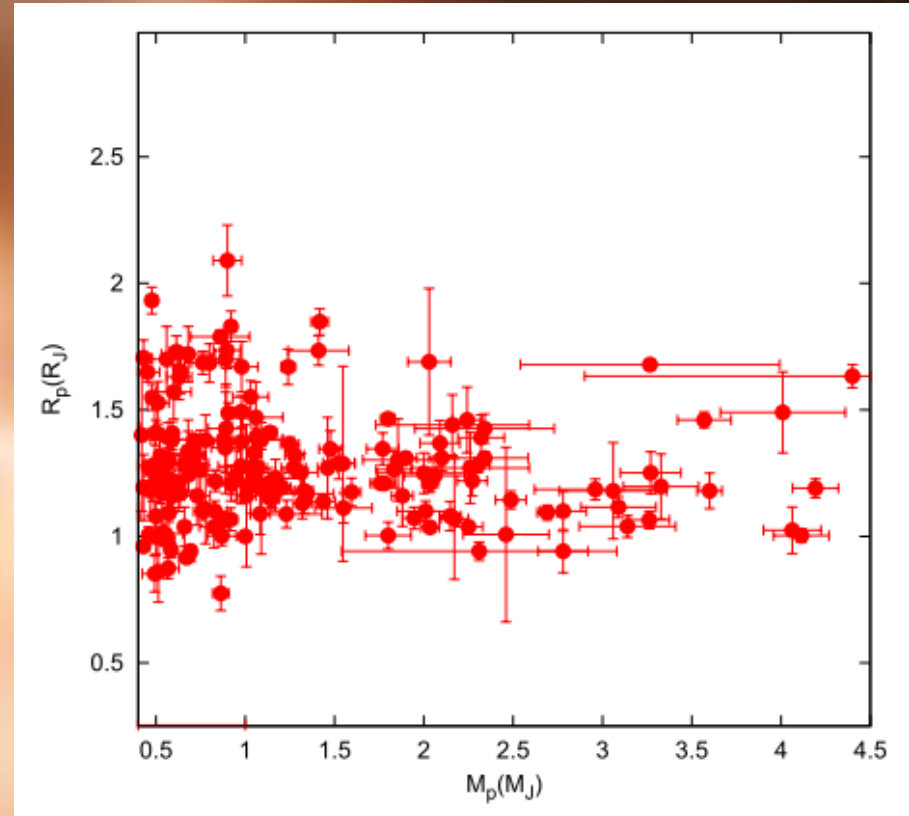
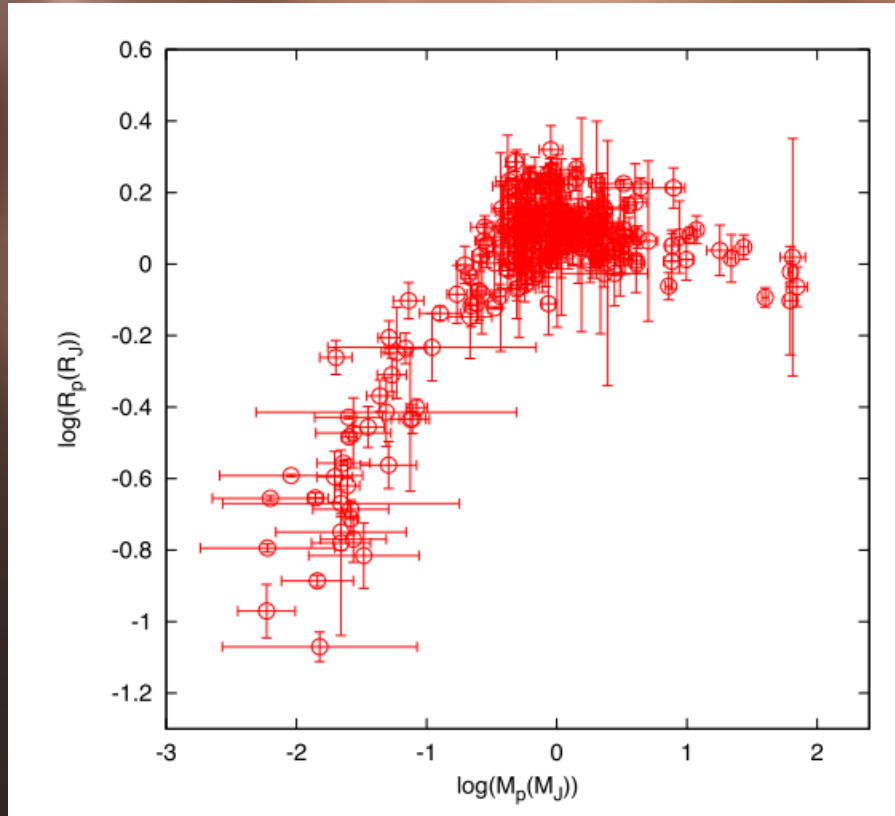
$$b(Z) = \frac{5.297}{3.139 + (Z/Z_{\odot})^{4.6}}.$$

Maximum age from Z_{Fe} is about 17-18 Giga years

Maximum age from Z_{o} is 11 Giga years

**Age of the Galaxy is 13.4 ± 0.8 Giga years
(Pasquini et al. 2004).**

Mass-radius relation for Planets : TEPCat (Southworth 2011)



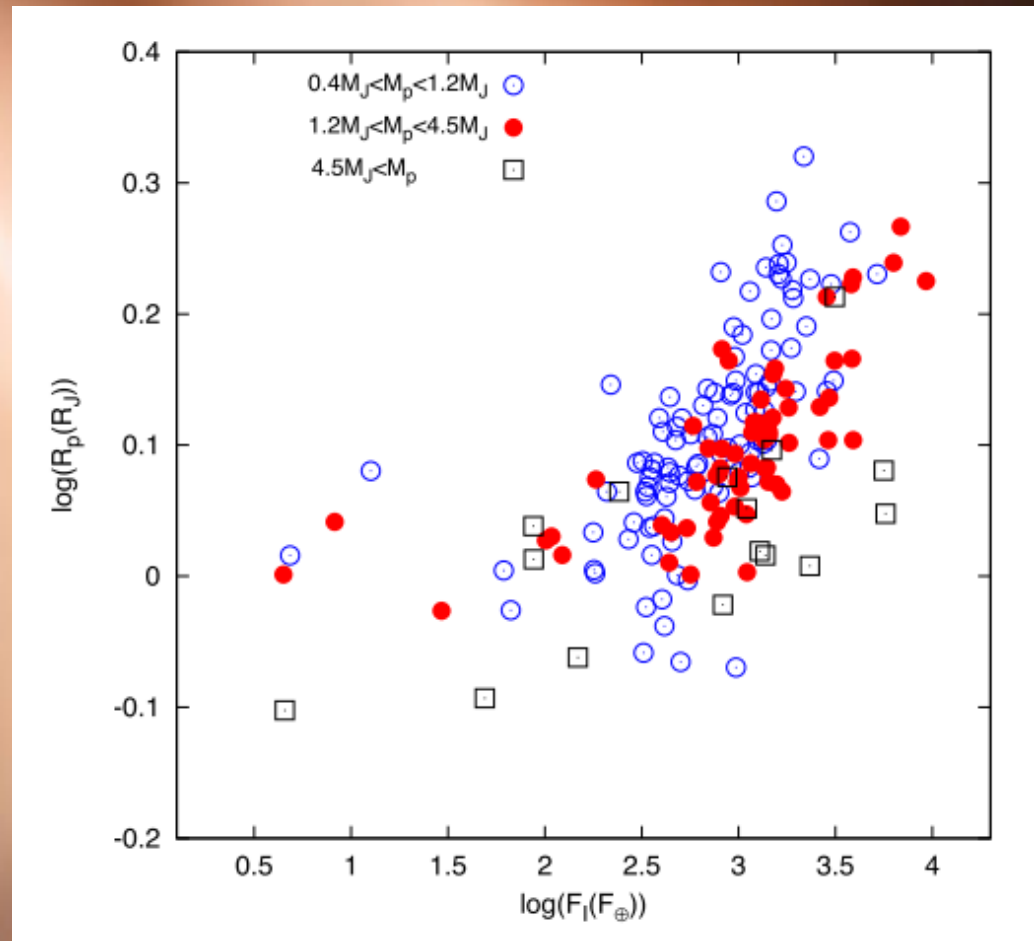
For $M_p=0.4-4.5 M_j$, radius is almost constant.

$0.7 < R < 2.1 R_j$

Why planetary radii are so different?

Inflated Planets: Effect of incident flux

Mass dependent



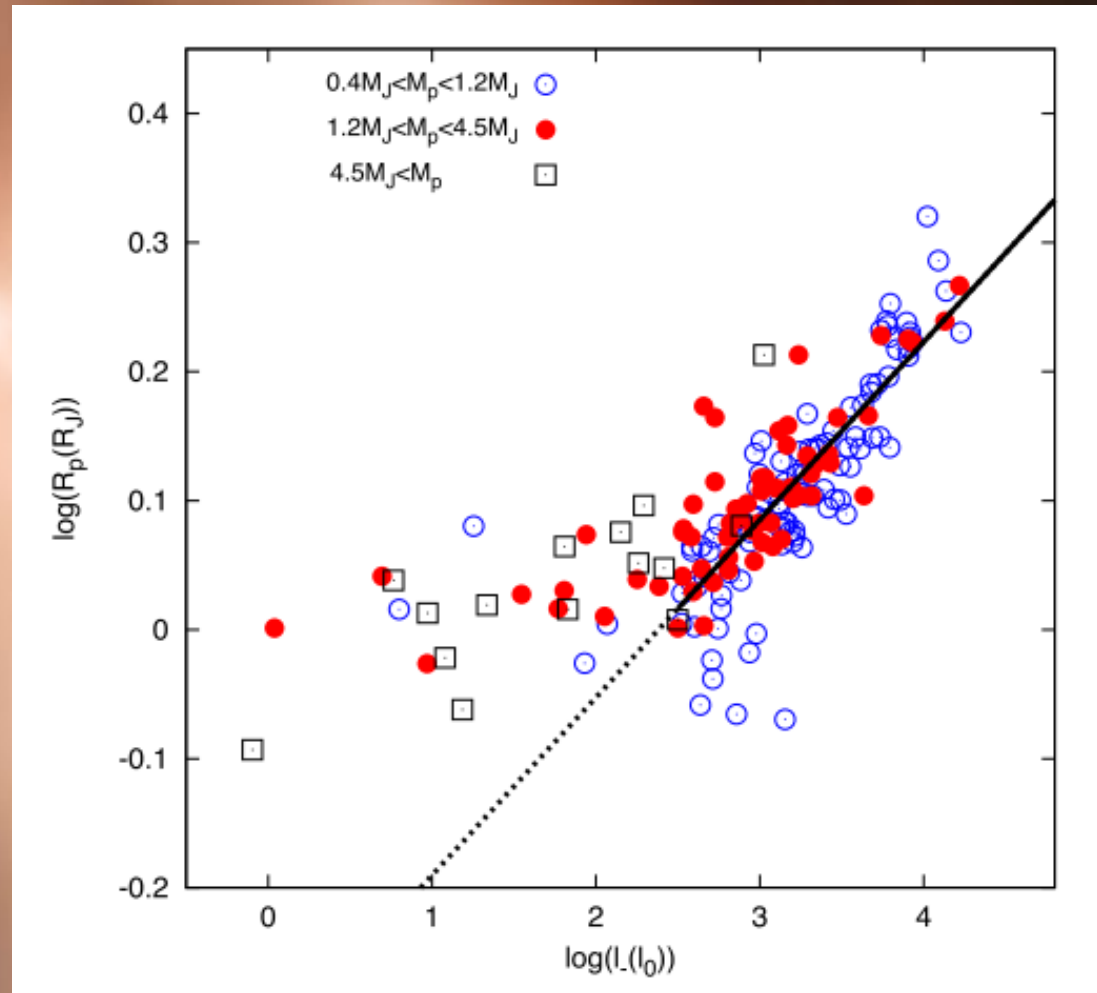
Inflated Planets: Effect of irradiation energy per gram per second

$$L_{-} = \pi R_p^2 F_I.$$

$$l_{-} = L_{-} / M_p$$

Mass independent
relation between
R and l_{-} ?

$$l_{-} = \frac{\pi F_I}{M_p / R_p^2} \propto \frac{F_I}{g_p}.$$



$$\Delta \log(R_l) = 0.138(\Delta \log(l_{-}/l_0) - 2.5).$$

Inflated Planets: Molecular dissociation?

For a sphere:

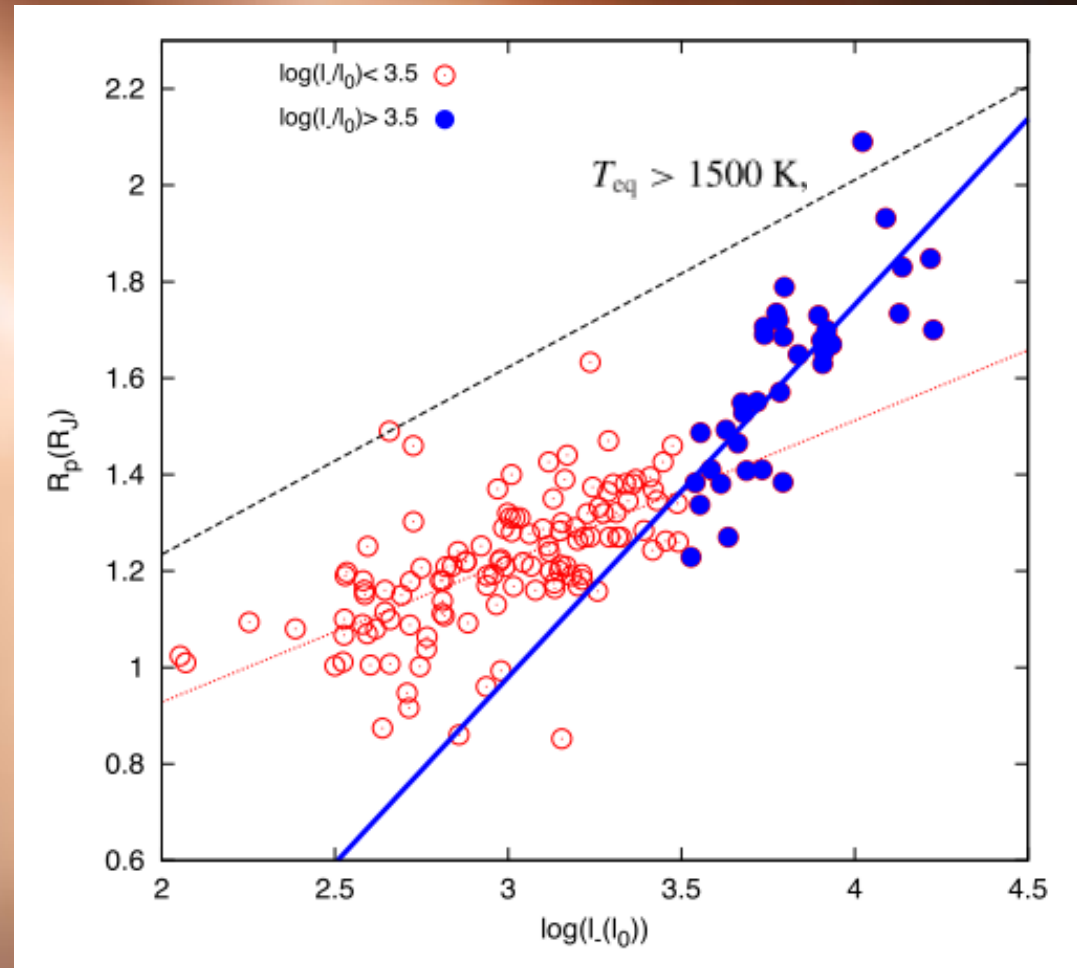
$$\frac{\Delta R}{R_i} = \frac{1}{3} \frac{\Delta V}{V_i}$$

If complete dissociation

$$n_f \approx 2n_i,$$

$$V_f \approx 2V_i,$$

$$R_f = R_i + \Delta R = 1.33R_i.$$



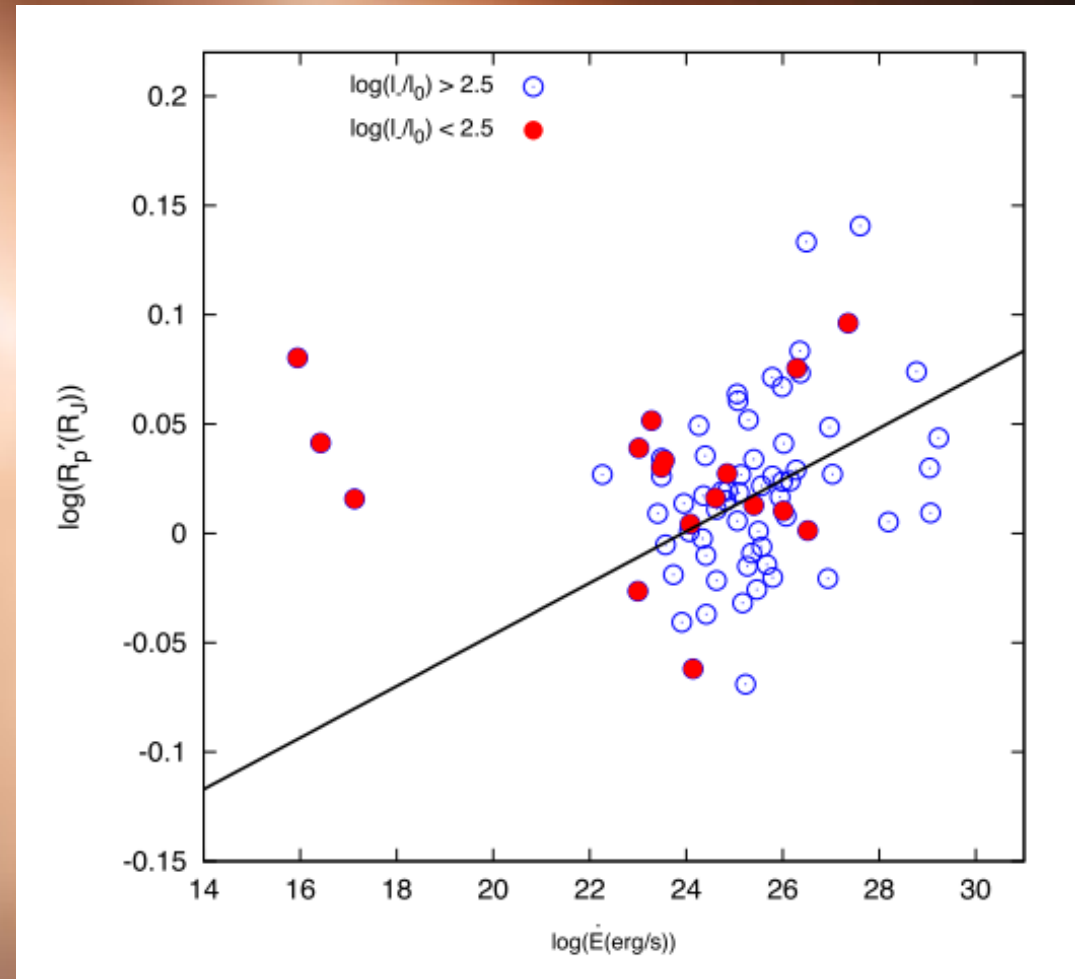
Inflated Planets: Tidal effect

Rate of energy converted
from orbital energy to
heat (Storch & Lai 2014)

Eccentricity (Knutson et al. 2014)

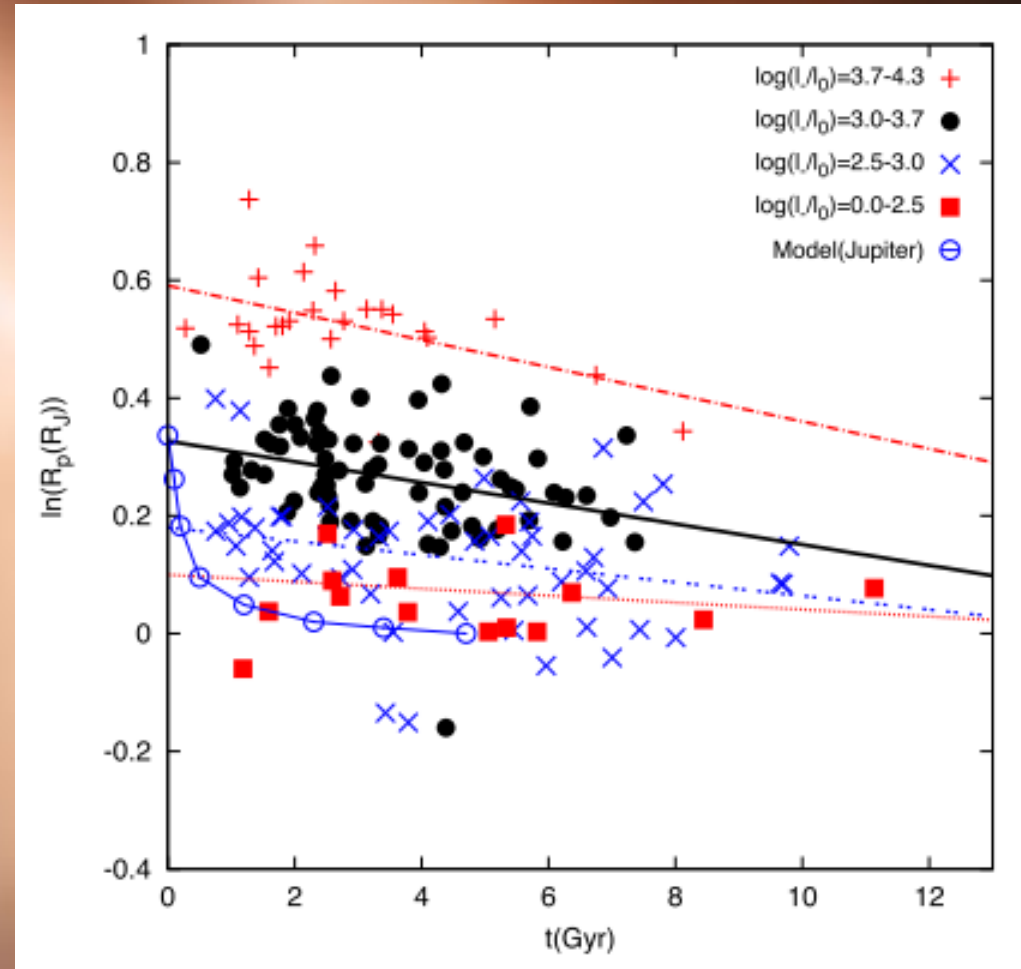
Effect of irradiation
energy on R is
subtracted.

$$R'_p \text{ is } R_p - \Delta R_l$$



Inflated Planets: Cooling

Cooling of Jupiter from
Nettelmann et al. (2012)



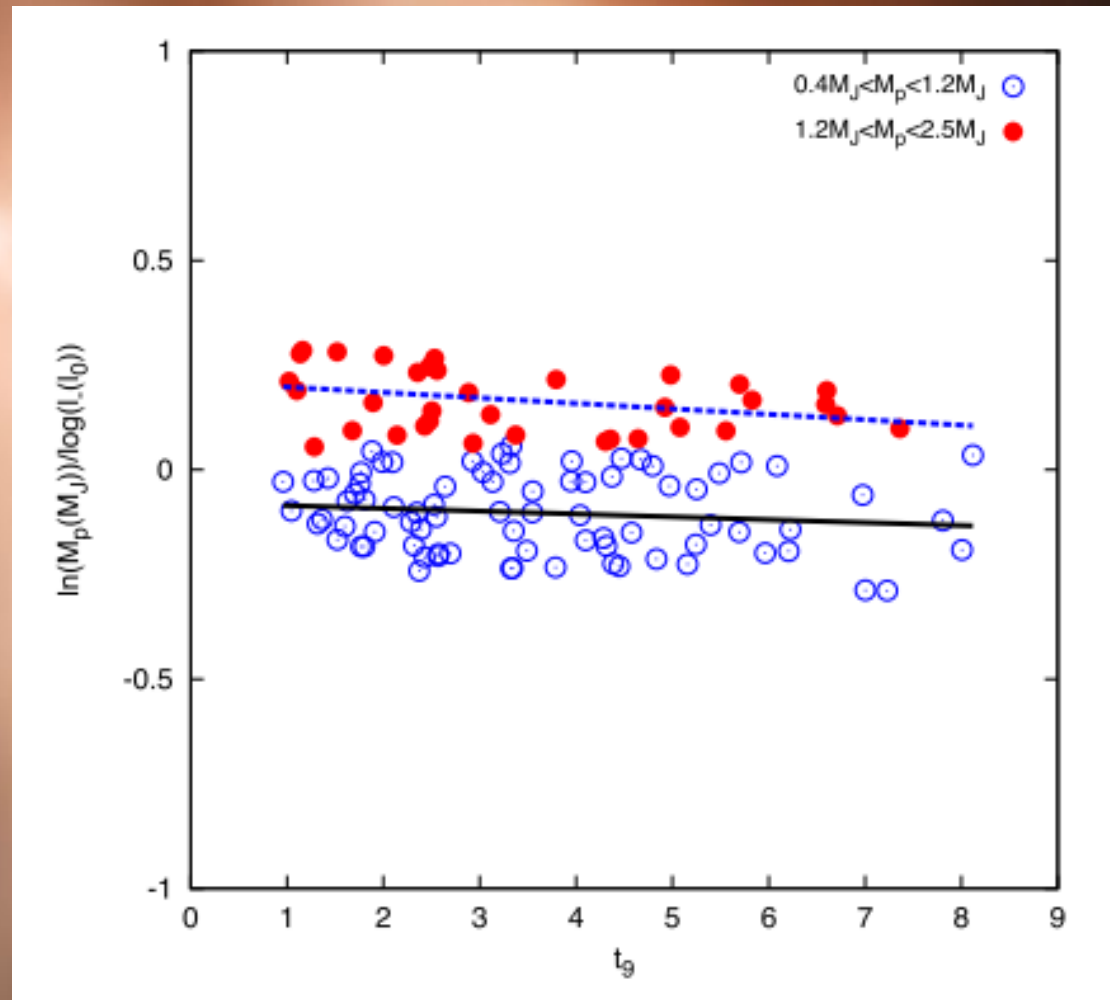
Inflated Planets: Evaporation

Mass-loss rates:

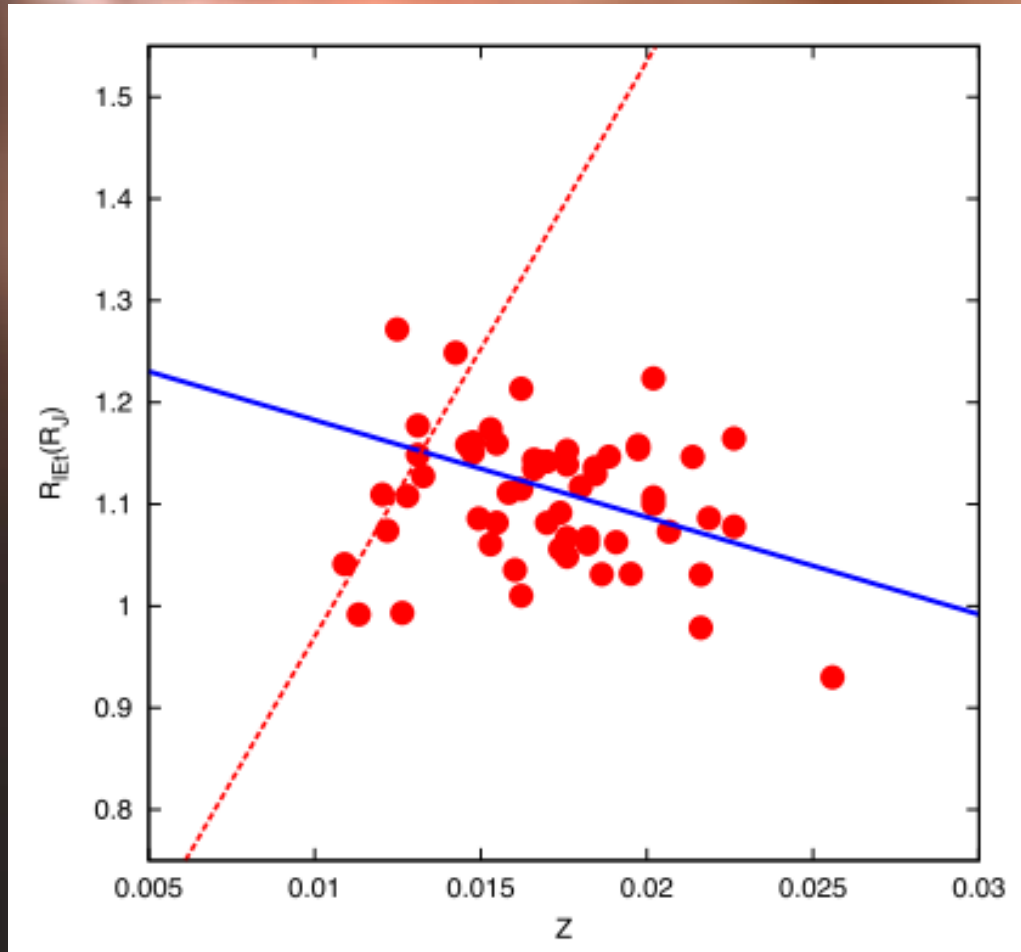
$$10^{11} - 10^{13} \text{ g s}^{-1}$$

$$10^{10} - 10^{12} \text{ g s}^{-1}$$

The mass loss for the
most irradiated planets
is about 5% in 1 Gyr.



Inflated Planets: Effect of Metallicity



$$R_l = R_p - \frac{\Delta R_p}{\Delta \log(l_-)} \delta \log(l_-).$$

$$R_{\text{IE}} = R_l - \frac{\Delta R_l}{\Delta \log(\dot{E})} \delta \log(\dot{E}).$$

$$R_{\text{IEt}} = R_{\text{IE}} + \frac{\Delta R_{\text{IE}}}{\Delta t_9} \delta t_9.$$

**Good agreement with
the findings of
Guillot et al.(2006) and
Miller & Fortney (2011)**



Conclusions

- * New methods are developed for age and metallicity (Z) of the host stars.
- * The most effective mechanism on planetary radius is irradiation energy ($\sim 30\%$).

The relation between R and irradiation is mass independent, if we consider received energy per gram per second (I_{r}).

- * Tidal effect $\sim 10-15\%$
- * Cooling and metallicity influence R.
- * Evaporation seems to cause significant mass loss.

Further analysis is required.