Non-gaussian imprints of primordial magnetic fields from inflation

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Outline of the talk

- Cosmic magnetic fields: Brief introduction and generation from inflation
- Deflationary magnetogenesis
- Non-gaussian imprints: Cross-correlation with primordial curvature perturbations
 - ✤ A new magnetic consistency relation
 - The squeezed limit and flattened shape

Conclusions

Our universe is magnetized!

- Large scale magnetic fields are present everywhere in the universe e.g. in our solar system, in stars, in galaxies, in clusters, in galaxies at high redshifts and also in the intergalactic medium.
- Solution Galaxies: B ~ 1 10 μ G with coherence length as large as 10 kpc.

Clusters: B ~ $0.1 - 1 \mu$ G, coherent on scales up to 100 kpc.

Filaments: B ~ 10^{-7} – 10^{-8} G, coherent on scales up to 1 Mpc (Kronberg 2010).

Intergalactic medium: B > 10^{-16} G, coherent on Mpc scales, the lower bound arises due to the absence of extended secondary GeV emission around TeV blazars (Neronov & Vovk, 2010), or even more robust limits of B > 10^{-19} G (Takahashi et al. 2011).

Primordial magnetic fields from inflation

Primordial magnetic fields from inflation

- Standard EM action is conformally invariant the EM fluctuations do not grow in any conformally flat background like FRW - need to break it to generate magnetic fields. (Turner & Widrow, 1988)
- ✤ Various possible couplings:
 - Kinetic coupling: $\lambda(\phi, \mathcal{R})F_{\mu\nu}F^{\mu\nu}$
 - Axial coupling: $f(\phi, \mathcal{R})F_{\mu\nu}\tilde{F}^{\mu\nu}$
 - Mass term: $M^2(\phi, \mathcal{R})A_{\mu}A^{\mu}$

Primordial magnetic fields from inflation...

• Axial coupling: $f(\phi, \mathcal{R})F_{\mu\nu}\tilde{F}^{\mu\nu}$

strong constraints from backreaction, final field strength not enough (Durrer, Hollenstein, RKJ, 2011; Byrnes, Hollenstein, RKJ, Urban, 2012)

• Mass term: $M^2(\phi, \mathcal{R})A_{\mu}A^{\mu}$

 negative mass-squared needed for generating relevant magnetic fields, breaks gauge invariance

Primordial magnetic fields from inflation...

Sauge-invariant coupling: $\lambda(\eta)F_{\mu\nu}F^{\mu\nu}$

• For $\lambda(\eta) \propto a^{2\alpha} \propto \eta^{2\gamma}$, the magnetic field spectrum is

$$\frac{d\rho_B}{d\ln k}(\eta,k) \propto \left(\frac{k}{aH}\right)^{4+2\delta}$$

where $\delta = \gamma$ if $\gamma \leq 1/2$ and $\delta = 1 - \gamma$ if $\gamma \geq 1/2$.

The tilt of the spectrum is $n_B = 4 + 2\delta$ and $n_B = 0$ for $\alpha = 2$ or $\gamma = -2$. However, $n_B = 0$ also for $\gamma = 3$ but then the electric field vary strongly and so not interesting.

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Various constraints

- ✤ Background
 - Strong coupling
 - ✤ Backreaction
- Perturbations
 - ✤ Power spectrum
 - Induced bispectrum

Energy scale of inflation (from B-modes)

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Constraint from strong coupling

➤ Adding the EM coupling to the SM fermions

$$\mathcal{L} = \sqrt{-g} \left[-\frac{1}{4} \lambda(\phi) F_{\mu\nu} F^{\mu\nu} - \bar{\psi} \gamma^{\mu} (\partial_{\mu} + ieA_{\mu}) \psi \right]$$

✤ The physical EM coupling now is

$$e_{phys} = e/\sqrt{\lambda(\phi)}$$

- Since $\sqrt{\lambda} \propto a^{\alpha}$ then for $\alpha > 0$, the physical coupling decreases by a large factor during inflation, and must have been very large at the beginning of inflation.
- ∞ QFT out of control initially. (Demozzi et.al, 2009)
- Solutions ?? Speculations...(Caldwell & Motta, 2012, Ferreira, RKJ & Sloth, 2013)

Constraint from backreaction

- → The magnetic fields should not backreact on the background dynamics of the universe i.e. $\rho_{\rm em} < \rho_{\rm inf}$
- → In the non-strongly coupled regime (α <0)

$$p_{\rm em} \simeq d_{\alpha} H^4 e^{-(2\alpha+4)(N_{\rm tot}-N_{\rm b})}, \quad d_{\alpha} \equiv -\frac{\Gamma^2(1/2-\alpha)}{2^{2\alpha+2} \pi^3(2\alpha+4)}$$

 $N_{\text{tot}} = N_{\min} + \Delta N$ - total amount of inflation

 $N_{\min} = \ln(R) + \frac{1}{2} \ln\left(\frac{H}{H_0}\right) + \frac{1}{4} \ln(\Omega_r), \text{ - minimum no. of e-folds}$ $N_b \text{ - e-fold of conformal breaking}$

Constraints from backreaction

The backreaction constraint translates into the inequality:

$$\left(\frac{H}{H_0}\right)^{-\alpha} < \frac{3\,\Omega_r^{(\alpha/2+1)}}{d_\alpha} \left(\frac{M_p}{H_0}\right)^2 e^{(2\alpha+4)(\Delta N - N_{\rm b})}$$

which implies

$$\alpha \gtrsim -2 + \frac{\ln\left(\frac{H}{M_p}\right)}{\frac{1}{2}\ln\left(\frac{H}{H_0}\Omega_r^{1/2}\right) + \Delta N - N_b}.$$

Backreaction + Strong coupling constraints at most lead to B ~10⁻³² G today. (Demozzi et.al, 2009)

Deflationary magnetogenesis

- Flux conservation leads to adiabatic decay of magnetic fields after inflation.
- Problem with modifying the inflationary part to generate even larger field strength during inflation.
- Rather, modify the post-inflationary evolution of magnetic fields until today.
- Consider prolonged reheating rather than instantaneous reheating.
- ▶ Deflation after inflation.

Ferreira, RKJ & Sloth, 2013

Deflationary magnetogenesis

- Sor radiation dominated universe immediately after inflation: $\rho_I / \rho_r = (a_0 / a_f)^4$
- \sim If the universe is instead dominated by a fluid with equation of state ω until the end of reheating:

$$\rho_I / \rho_r = (a_{reh} / a_f)^{3(1+\omega)} (a_0 / a_{reh})^4$$

or
$$\frac{a_0}{a_f} = \frac{1}{R} \left(\frac{\rho_I}{\rho_r}\right)^{\frac{1}{4}}$$

Define the reheating parameter R as

$$\log(R) = \frac{-1 + 3\omega}{4} \log\left(\frac{a_{reh}}{a_f}\right)$$

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Deflationary magnetogenesis

The magnetic field spectrum today is

$$\left. \frac{d\rho_B}{d\log k} \right|_{a_0} = \left. \frac{d\rho_B}{d\log k} \right|_{a_f} \left(\frac{a_f}{a_0} \right)^4$$

 \sim In terms of R, we get

$$B_k(\alpha, H) = \frac{\Gamma(-\alpha - 1/2)}{2^{3/2 + \alpha} \pi^{3/2}} H^2 \left(R \,\Omega_r^{1/4} \right)^{-(1+\alpha)} \left(\frac{H_0}{H} \right)^{\frac{1}{2}(5+\alpha)} \left(\frac{k}{a_0 H_0} \right)^{3+\alpha}$$

→ To get optimal values of the magnetic fields today, maximize in α and R.

Ferreira, RKJ & Sloth, 2013

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Final magnetic field strength



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Non-gaussiam imprints of primordial magnetic fields

Magnetic non-Gaussianity

- If magnetic fields are produced during inflation, they are likely to be correlated with the primordial curvature perturbations.
- Such cross-correlations are non-Gaussian in nature and it is very interesting to compute them in different models of inflationary magnetogenesis.
- We consider the following correlation here:

 $\langle \zeta(k_1) \mathbf{B}(k_2) \cdot \mathbf{B}(k_3) \rangle$

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(Ordinary) non-Gaussianity

The primordial perturbations are encoded in the two-point function or the power spectrum

$$\langle \zeta_k \zeta_{k'} \rangle = (2\pi)^3 \delta(\vec{k} + \vec{k'}) P_{\zeta}(k)$$

→ A non-vanishing three-point function $\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle$ is a signal of NG.

• Introduce f_{NL} as a measure of NG.

$$f_{NL} \sim \left\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \right\rangle / P_{\zeta}(k_1) P_{\zeta}(k_2) + perm.$$

(semi)Classical estimate (for squeezed limit)

• Consider $\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle$ in the squeezed limit i.e.

The long wavelength mode rescales the background for short wavelength modes

$$ds^2 = -dt^2 + a^2(t) e^{2\zeta(t,\mathbf{x})} d\mathbf{x}^2$$

Taylor expand in the rescaled background $\langle \zeta_{k_2} \zeta_{k_3} \rangle_{\zeta_1} = \langle \zeta_{k_2} \zeta_{k_3} \rangle + \zeta_1 \frac{\partial}{\partial \zeta_1} \langle \zeta_{k_2} \zeta_{k_3} \rangle + \dots$ $\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle_{\zeta_1} \approx \left\langle \zeta_{k_1} \langle \zeta_{k_2} \zeta_{k_3} \rangle_{\zeta_1} \right\rangle \sim \langle \zeta_{k_1} \zeta_{k_1} \rangle k \frac{d}{dk} \langle \zeta_{k_2} \zeta_{k_3} \rangle$ $\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle \sim -(n_s - 1) \left\langle \zeta_{k_1} \zeta_{k_1} \right\rangle \left\langle \zeta_{k_2} \zeta_{k_3} \right\rangle$ (Maldacena, 2002)

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Non-gaussian cross-correlation

Define the cross-correlation bispectrum of the curvature perturbation with magnetic fields as

 $\langle \zeta(\mathbf{k}_1) \mathbf{B}(\mathbf{k}_2) \cdot \mathbf{B}(\mathbf{k}_3) \rangle \equiv (2\pi)^3 \delta^{(3)}(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) B_{\zeta BB}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3)$

Solution Introduce the magnetic non-linearity parameter $B_{\zeta BB}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) \equiv b_{NL}P_{\zeta}(k_1)P_B(k_2)$

 \sim *Local* resemblance between f_{NL} and b_{NL}

$$\begin{aligned} \zeta &= \zeta^{(G)} + \frac{3}{5} f_{NL}^{local} \left(\zeta^{(G)} \right)^2 \\ \mathbf{B} &= \mathbf{B}^{(G)} + \frac{1}{2} b_{NL}^{local} \zeta^{(G)} \mathbf{B}^{(G)} \end{aligned}$$

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A new magnetic consistency relation

- Use the same semi-classical argument to derive the consistency relation.
- Solution Solution Solution Solution Solution Consider $\langle \zeta(\tau_I, \mathbf{k}_1) A_i(\tau_I, \mathbf{k}_2) A_j(\tau_I, \mathbf{k}_3) \rangle$ in the squeezed limit.
- The effect of the long wavelength mode is to shift the background of the short wavelength mode.

 $\lim_{k_1 \to 0} \left\langle \zeta(\tau_I, \mathbf{k}_1) A_i(\tau_I, \mathbf{k}_2) A_j(\tau_I, \mathbf{k}_3) \right\rangle = \left\langle \zeta(\tau_I, \mathbf{k}_1) \left\langle A_i(\tau_I, \mathbf{k}_2) A_j(\tau_I, \mathbf{k}_3) \right\rangle_B \right\rangle$

Since the gauge field only feels the background through the coupling, all the effects of the long wavelength mode is indeed captured by

$$\lambda_B = \lambda_0 + \frac{d\lambda_0}{d\ln a}\delta\ln a + \dots = \lambda_0 + \frac{d\lambda_0}{d\ln a}\zeta_B + \dots$$

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A new magnetic consistency relation

 Compute the two point function of the vector field in the modified background

$$\langle A_i(\tau, \mathbf{x}_2) A_j(\tau, \mathbf{x}_3) \rangle_B = \left\langle \frac{1}{\lambda_B} v_i(\tau, \mathbf{x}_2) v_j(\tau, \mathbf{x}_3) \right\rangle$$

$$\simeq \frac{1}{\lambda_0} \left\langle v_i(\tau, \mathbf{x}_2) v_j(\tau, \mathbf{x}_3) \right\rangle - \frac{1}{\lambda_0^2} \frac{d\lambda}{d \ln a} \zeta_B \left\langle v_i(\tau, \mathbf{x}_2) v_j(\tau, \mathbf{x}_3) \right\rangle$$

where $v_i = \sqrt{\lambda} A_i$ is the linear canonical vector field.

One finally finds

$$\lim_{k_1 \to 0} \left\langle \zeta(\tau_I, \mathbf{k}_1) A_i(\tau_I, \mathbf{k}_2) A_j(\tau_I, \mathbf{k}_3) \right\rangle$$

$$\simeq -\frac{1}{H} \frac{\dot{\lambda}}{\lambda} \left\langle \zeta(\tau_I, \mathbf{k}_1) \zeta(\tau_I, -\mathbf{k}_1) \right\rangle_0 \left\langle A_i(\tau_I, \mathbf{k}_2) A_j(\tau_I, \mathbf{k}_3) \right\rangle_0$$

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A new magnetic consistency relation • In terms of magnetic fields, the correlation becomes $\langle \zeta(\tau_I, \mathbf{k}_1) \mathbf{B}(\tau_I, \mathbf{k}_2) \cdot \mathbf{B}(\tau_I, \mathbf{k}_3) \rangle$ $= -\frac{1}{H} \frac{\dot{\lambda}}{\lambda} (2\pi)^3 \delta^{(3)}(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) P_{\zeta}(k_1) P_B(k_2)$

• With the coupling $\lambda(\phi(\tau)) = \lambda_I(\tau/\tau_I)^{-2n}$, we obtain

$$b_{NL} = n_B - 4$$

Solution → For scale-invariant magnetic field spectrum, $n_B = 0$ and therefore, $b_{NL} = -4$

→ Not so small.....compared to $b_{NL} \sim O(\epsilon, \eta)$

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A new magnetic consistency relation

▶ In the squeezed limit $k_1 \ll k_2, k_3 = k$, we obtain a new *magnetic consistency relation*

$$\langle \zeta(k_1) \mathbf{B}(k_2) \cdot \mathbf{B}(\mathbf{k_3}) \rangle = (n_B - 4)(2\pi)^3 \delta^{(3)}(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) P_{\zeta}(k_1) P_B(k)$$

with
$$b_{NL}^{\text{local}} = (n_B - 4)$$

Compare with Maldacena's consistency relation

$$\begin{aligned} \langle \zeta(k_1)\zeta(k_2)\zeta(k_3) \rangle &= -(n_s - 1)(2\pi)^3 \delta^{(3)}(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) P_{\zeta}(k_1) P_{\zeta}(k) \\ \text{with } f_{NL}^{\text{local}} &= -(n_s - 1) \end{aligned}$$

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The full in-in calculation

✤ One has to cross-check the consistency relation by doing the full in-in calculation

 $\langle \Omega | \mathcal{O}(\tau_I) | \Omega \rangle = \langle 0 | \bar{\mathrm{T}} \left(e^{i \int_{-\infty}^{\tau_I} d\tau H_{\mathrm{int}}} \right) \mathcal{O}(\tau_I) \mathrm{T} \left(e^{-i \int_{-\infty}^{\tau_I} d\tau H_{\mathrm{int}}} \right) | 0 \rangle$

 \sim The result is

 $\langle \zeta(\tau_I, \mathbf{k}_1) A_i(\tau_I, \mathbf{k}_2) A_j(\tau_I, \mathbf{k}_3) \rangle = \frac{1}{H} \frac{\lambda_I}{\lambda_I} (2\pi)^3 \delta^{(3)}(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) |\zeta_{k_1}^{(0)}(\tau_I)|^2 |A_{k_2}^{(0)}(\tau_I)| |A_{k_3}^{(0)}(\tau_I)|$ $\times \left[\left(\delta_{il} - \frac{k_{2,i}k_{2,l}}{k_2^2} \right) \left(\delta_{lj} - \frac{k_{3,l}k_{3,j}}{k_2^2} \right) \left(k_2 k_3 \tilde{\mathcal{I}}_n^{(1)} + \mathbf{k}_2 \cdot \mathbf{k}_3 \tilde{\mathcal{I}}_n^{(2)} \right) \right]$ $-\left(\delta_{il}-\frac{k_{2,i}k_{2,l}}{k_2^2}\right)k_{3,l}\left(\delta_{jm}-\frac{k_{3,j}k_{3,m}}{k_3^2}\right)k_{2,m}\tilde{\mathcal{I}}_n^{(2)}$ A generic result **RKJ** & Sloth, 2013 The Primordial Universe after Planck Dec.15-19, 2014

Cross-correlation with magnetic fields

Using this relation

 $\left\langle \zeta(\tau_I, \mathbf{k}_1) \mathbf{B}(\tau_I, \mathbf{k}_2) \cdot \mathbf{B}(\tau_I, \mathbf{k}_3) \right\rangle = -\frac{1}{a_0^4} \left(\delta_{ij} \mathbf{k}_2 \cdot \mathbf{k}_3 - \mathbf{k}_{2,i} \mathbf{k}_{3,j} \right) \left\langle \zeta(\tau_I, \mathbf{k}_1) A_i(\tau_I, \mathbf{k}_2) A_j(\tau_I, \mathbf{k}_3) \right\rangle$

✤ The cross-correlation with magnetic fields is

$$\begin{split} \zeta(\tau_I, \mathbf{k}_1) \mathbf{B}(\tau_I, \mathbf{k}_2) \cdot \mathbf{B}(\tau_I, \mathbf{k}_3) \rangle &= -\frac{1}{H} \frac{\dot{\lambda}_I}{\lambda_I} (2\pi)^3 \delta^{(3)}(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) |\zeta_{k_1}^{(0)}(\tau_I)|^2 |A_{k_2}^{(0)}(\tau_I)| |A_{k_3}^{(0)}(\tau_I)| \\ & \times \left[\left(\mathbf{k}_2 \cdot \mathbf{k}_3 + \frac{(\mathbf{k}_2 \cdot \mathbf{k}_3)^3}{k_2^2 k_3^2} \right) k_2 k_3 \tilde{\mathcal{I}}_n^{(1)} + 2(\mathbf{k}_2 \cdot \mathbf{k}_3)^2 \tilde{\mathcal{I}}_n^{(2)} \right] \,. \end{split}$$

The two integrals can be solved exactly for different values of n.

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The integrals...

✤ The two integrals are

$$\tilde{\mathcal{I}}_{n}^{(1)} = \frac{\pi^{3}}{2} \frac{2^{-2n-1}}{\Gamma^{2}(n+1/2)} (-k_{2}\tau_{I})^{n+1/2} (-k_{3}\tau_{I})^{n+1/2} \\
\times \operatorname{Im} \left[(1+ik_{1}\tau_{I})e^{-ik_{1}\tau_{I}}H_{n+1/2}^{(1)}(-k_{2}\tau_{I})H_{n+1/2}^{(1)}(-k_{3}\tau_{I}) \\
\times \int^{\tau_{I}} d\tau \tau (1-ik_{1}\tau)e^{ik_{1}\tau}H_{n-1/2}^{(2)}(-k_{2}\tau)H_{n-1/2}^{(2)}(-k_{3}\tau) \right] \\
\tilde{\mathcal{I}}_{n}^{(2)} = \frac{\pi^{3}}{2} \frac{2^{-2n-1}}{\Gamma^{2}(n+1/2)} (-k_{2}\tau_{I})^{n+1/2} (-k_{3}\tau_{I})^{n+1/2}$$

$$\Sigma_{n}^{(2)} = \frac{1}{2} \frac{\Gamma^{2}(n+1/2)}{\Gamma^{2}(n+1/2)} (-k_{2}\tau_{I})^{n+1/2} (-k_{3}\tau_{I})^{n+1/2} \times \operatorname{Im} \left[(1+ik_{1}\tau_{I})e^{-ik_{1}\tau_{I}}H_{n+1/2}^{(1)}(-k_{2}\tau_{I})H_{n+1/2}^{(1)}(-k_{3}\tau_{I}) \right] \times \int^{\tau_{I}} d\tau \tau (1-ik_{1}\tau)e^{ik_{1}\tau}H_{n+1/2}^{(2)}(-k_{2}\tau)H_{n+1/2}^{(2)}(-k_{3}\tau) \right]$$

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The flattened shape

▶ In this limit, $k_1 = 2k_2 = 2k_3$, the second integral dominates

$$\tilde{\mathcal{I}}_{2}^{(2)} \simeq -\frac{3k_{1}^{3}}{(k_{2}k_{3})^{5/2}}\ln(-k_{t}\tau_{I})$$

- Solution The cross-correlation thus becomes $\langle \zeta(\tau_I, \mathbf{k}_1) \mathbf{B}(\tau_I, \mathbf{k}_2) \cdot \mathbf{B}(\tau_I, \mathbf{k}_3) \rangle \simeq 96 \ln(-k_t \tau_I) P_{\zeta}(k_1) P_B(k_2)$
- → For the largest observable scale today, $\ln(-k_t \tau_I) \sim -60$,

$$\left| b_{NL}^{flat} \right| \sim 5760$$

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The squeezed limit

In this limit, the integrals are

$$\tilde{\mathcal{I}}_{n}^{(1)} = \pi \int^{\tau_{I}} d\tau \tau J_{n-1/2}(-k\tau) Y_{n-1/2}(-k\tau)$$

 $\tilde{\mathcal{I}}_n^{(2)} = \tilde{\mathcal{I}}_{n+1}^{(1)} \; .$

The cross-correlation now becomes

$$\langle \zeta(\tau_I, \mathbf{k}_1) \mathbf{B}(\tau_I, \mathbf{k}_2) \cdot \mathbf{B}(\tau_I, \mathbf{k}_3) \rangle = -\frac{1}{H} \frac{\dot{\lambda}_I}{\lambda_I} (2\pi)^3 \delta^{(3)}(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) P_{\zeta}(k_1) P_B(k_2)$$

with $b_{NL} = -\frac{1}{H}\frac{\dot{\lambda}_I}{\lambda_I} = n_B - 4$ in agreement with the magnetic consistency relation.

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Conclusions

- Inflationary + deflationary magnetogenesis can produce strong enough fields on large scales without the backreaction and strong coupling problem.
- Low scale inflationary magnetogenesis is still a viable possibility (given the status of BICEP2).
- The consistency relation is an important theoretical tool to cross-check the full in-in calculations, it's violation will rule out an interesting class of inflationary magnetogenesis models.
- The magnetic non-Gaussianity parameter is large in the flattened limit and can have non-trivial phenomenological consequences.