

# *Primordial Black Holes*

## *and their effect on the cosmic ionization history*

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## Collaborators:

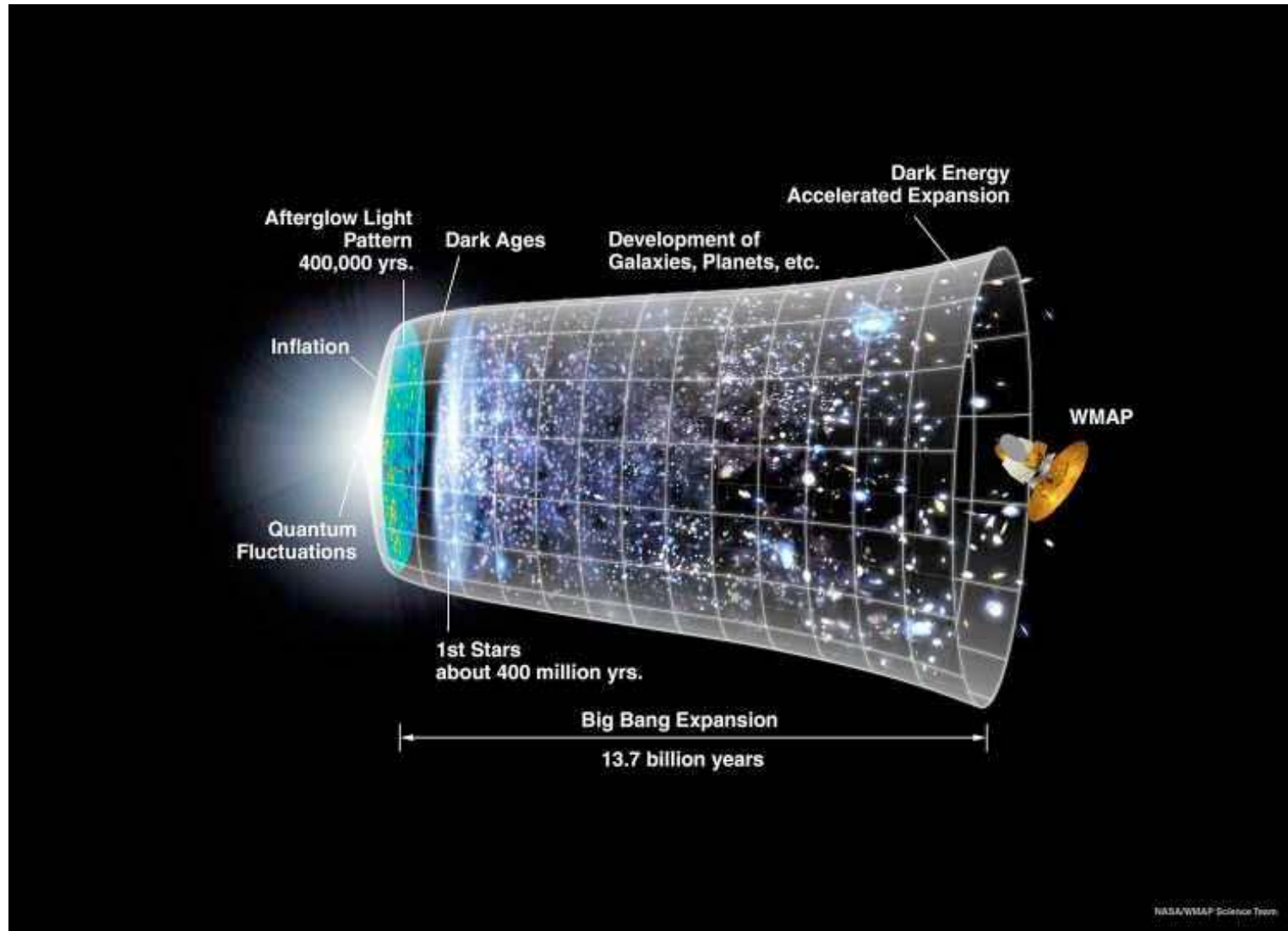


Jerry Ostriker (Princeton), Katie Mack (Princeton)

# Outline

- What are PBHs and why we do we care?
- Modelling accretion onto PBHs:
  - Growth of DM halos, modified Bondi solutions
  - PBHs motions and feedback processes
- Effect on the ionization history
- Effect on the CMB, new obs. constraints and Implications

# Hot Big Bang theory



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1. Collapsed radiation (relativistic matter)
2. Mass comparable to the Horizon mass at formation
3. Form in quasi-linear regime: 50%
4. Tiny collapsed fraction during rad. era may produce all the dark matter!

Newtonian limit easy to understand: During radiation era

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Collapsed fraction depends on the power spectrum of  
 initial density fluctuations and the cosmic equation of state:

- $\delta_{cr} = \delta_{cr}(w)$  where  $P = w$  is the cosmic EOS
- $\delta(M, z) \sim \exp[-(\delta_{cr}/2 \delta(M, z))^2]$  (assuming Gaussian fluctuations)

Radiation is redshifted away, PBHs are not:

$$\rho_{\text{pbh}} = \frac{(1 + z_f)}{(1 + z_{\text{eq}})}$$

$$f_{\text{pbh}} = \frac{\rho_{\text{pbh}}}{\rho_{\text{m}}} = \frac{M_{\text{pbh}}^{1/2}}{1 \text{ M}} \frac{1}{10^9}$$

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$$\rho_{\text{pbh}} = \frac{\rho_{\text{rad}}}{(1 + z_f)/(1 + z_{\text{eq}})}$$

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● Example:

- During QCD phase transition at  $t = 10^{-5}$  sec
- $M_{\text{pbh}} = M_h = 1 M$
- if  $f_{\text{pbh}} = 10^{-9}$ : all the dark matter is made of PBHs

# *Some models for PBH formation*

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2. Collapse of rare density peaks: depend on the shape of inflaton potential (*e.g.*, potential as in Kawasaki et al 06 produces  $100 \text{ M}$  PBHs)

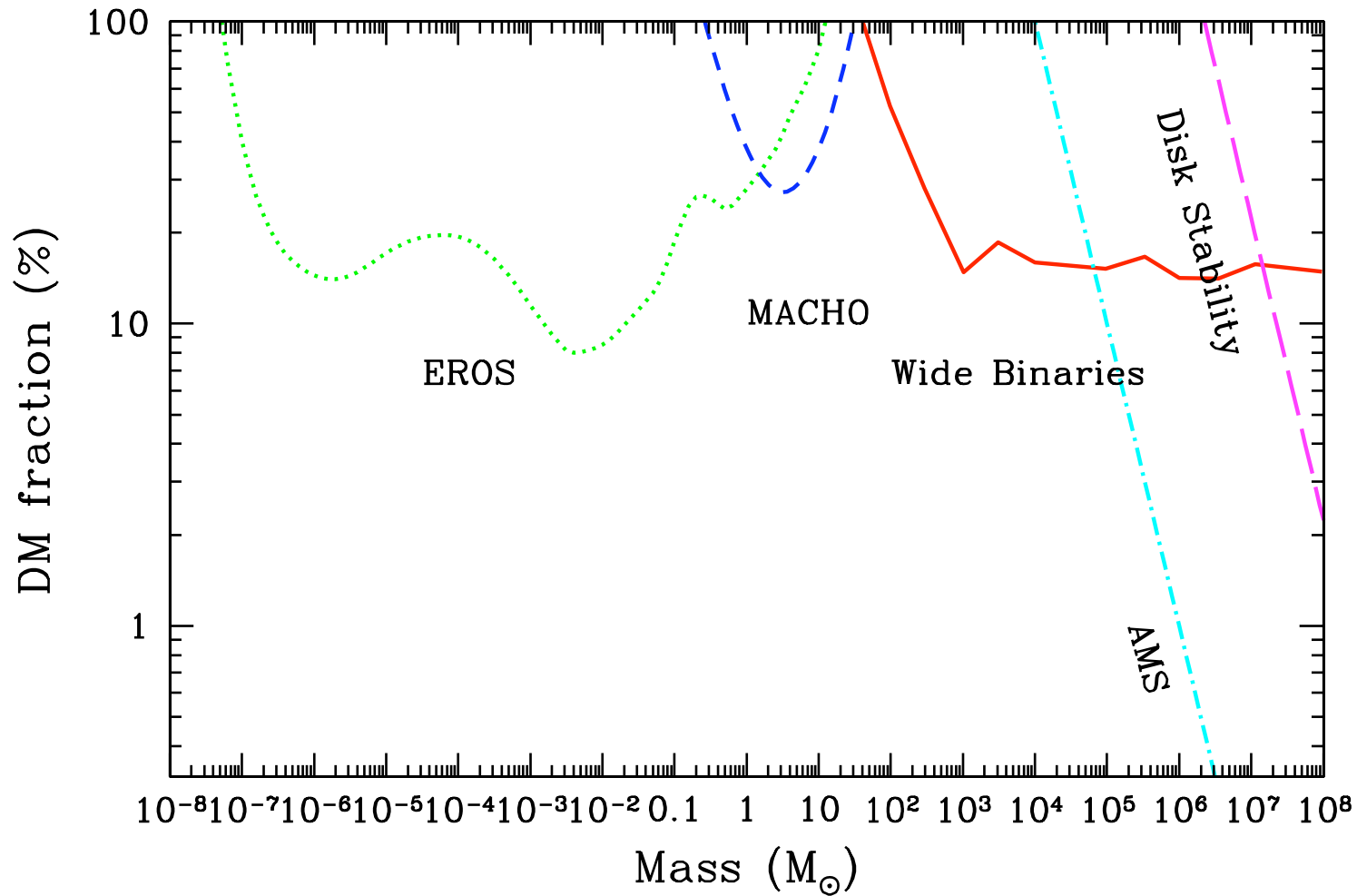


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3. Collapse of cosmic string loops (*e.g.*, Polnarev & Zemboricz 88; Hawking 89; Brandenberger & Wichoski 98)
4. Bubble collisions (*e.g.*, Crawford & Schramm 82; La & Steinhardt 89)
5. Collapse of domain walls (Berezin et al 83; Ipser & Sikivie 84; Rubin et al. 00)

# *Do PBHs exist?*

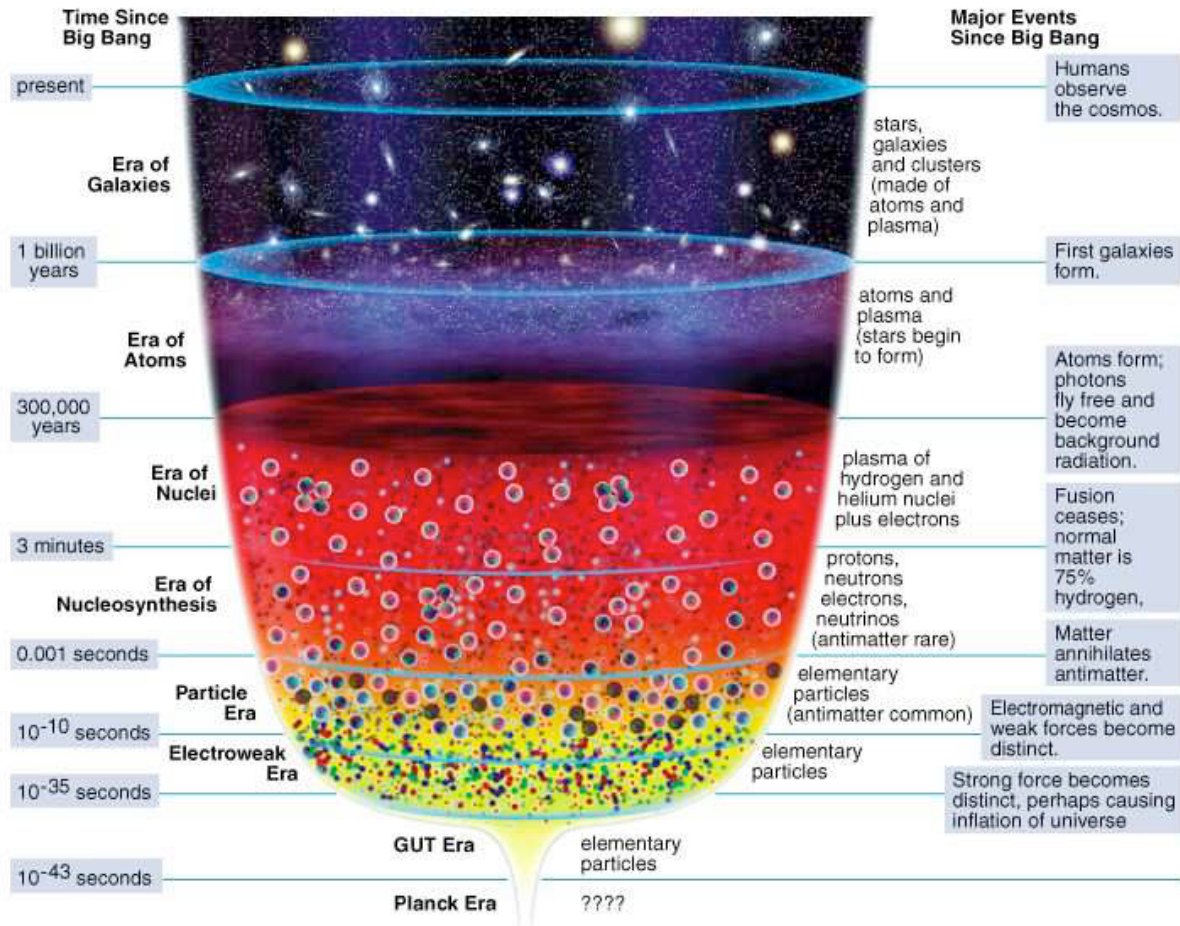
- PBHs with mass  $< 10^{15}$  g evaporate in  $t < t_H$  (Hawking 1975)
  - Abundance of PBHs with mass  $1 \text{ g} < M < 10^{15} \text{ g}$  is  $< 10^{-20} - 10^{-22}$  (e.g., Carr 2003)
- More massive PBHs are poorly constrained:
  - They may constitute the bulk of the dark matter
  - MACHO collaboration: 20% of Milky-Way halo is in compact objects with  $M = 0.1 - 1 M_\odot$  (but 2000 result, non confirmed by later data)



Refs: MACHO collaboration [e.g., Alcock et al. (1998, 2000, 2001); Hamadache et al. 2006]; EROS collaboration; Lacey &

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3. Produce MACHOS, IMBH and ULXs ?
4. Seeds for supermassive Black Holes?



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Gas accretion onto PBHs produce X-rays and affect the ionization history of the IGM



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4. Angular momentum of accreted gas and dark matter
5. Feedback processes (global and local radiative feedbacks)

# *1. Clothing Dark Matter Halo*

1. PBHs seed accumulation of dark halo ( $f_{\text{pbh}} < 1$ )
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# 1. Clothing Dark Matter Halo

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- growth of order unity during radiation era
- $M_h = 3M_{\text{pbh}} \frac{1+z}{1000}^1$
- Self-similar secondary infall solution (*e.g.*, Bertschinger 1985)
- Truncated power-law density profile with  $\gamma = 2.25$
- Truncation at  $r_h = r_{\text{ta}}/3$

## 2. Bondi type accretion

- Spherical accretion ( )
- Steady-state ( $M < 2 \cdot 10^4 M_\odot$ , )
- Viscosity (Compton drag)

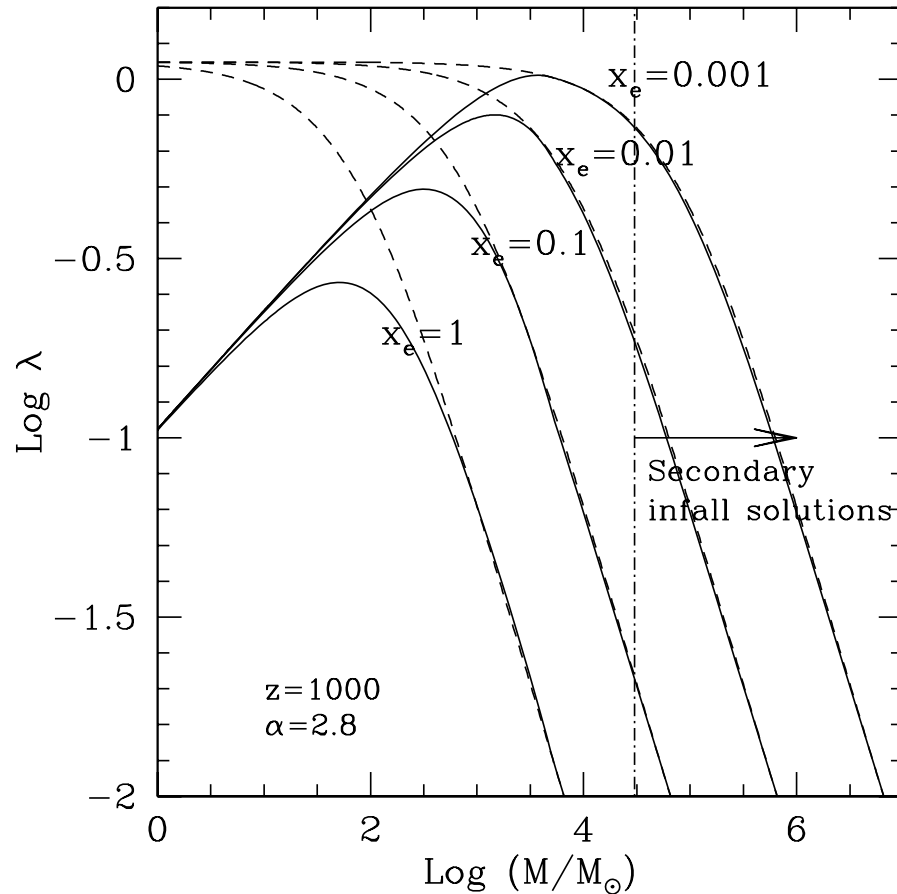
$$\frac{dv}{dt} = \frac{4}{3} \frac{x_e \tau U_{\text{cmb}}}{m_p c} v = -v$$

- Hubble expansion ( $M > 2 \cdot 10^4 M_\odot$ , )
- Clothing dark halo (power-law density profile, )

Ref: Ricotti (2007)



# Spherical accretion rate



- point mass potential (dashed curves)
- dark halo potential (solid curves)

### 3. Relative motion of PBHs and gas

$$\dot{M}_g \propto \frac{M^2}{v_{\text{eff}}^3}$$

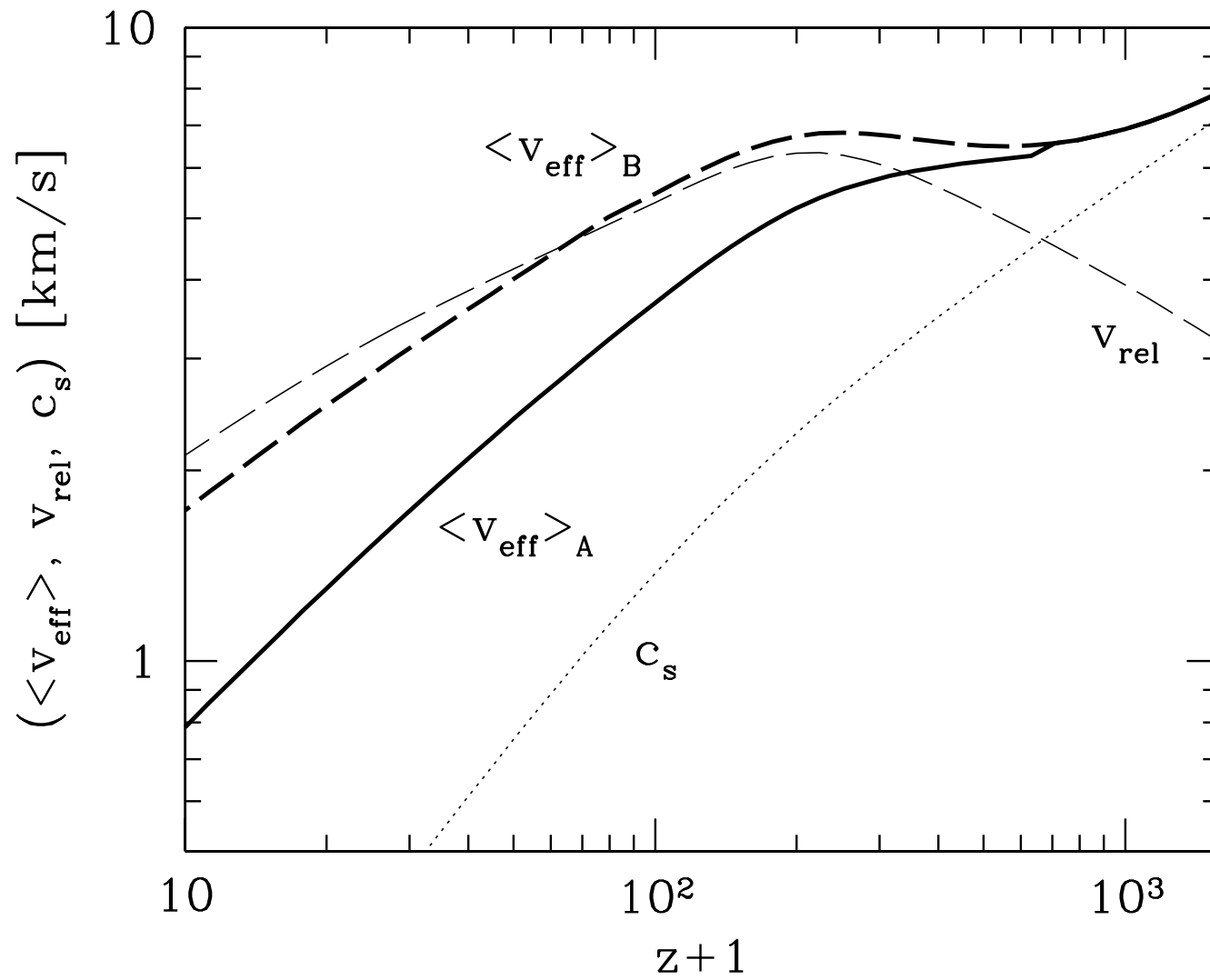
where  $v_{\text{eff}} = (v_{\text{rel}}^2 + c_s^2)^{1/2}$

1. Linear regime: Silk damping (i = baryons, dark matter)

$$V_i^2 = \frac{1.2}{2} \frac{m H^2}{2} \int_0^\infty P_i(k) w_s^2(k, a) w_l^2(k, r_0) dk,$$

$$V_i^2 = \frac{1.2}{2} \frac{m H^2}{2} \int_0^\infty P_i(k) w_s^2(k, a) [1 - w_l^2(k, r_0)] dk.$$

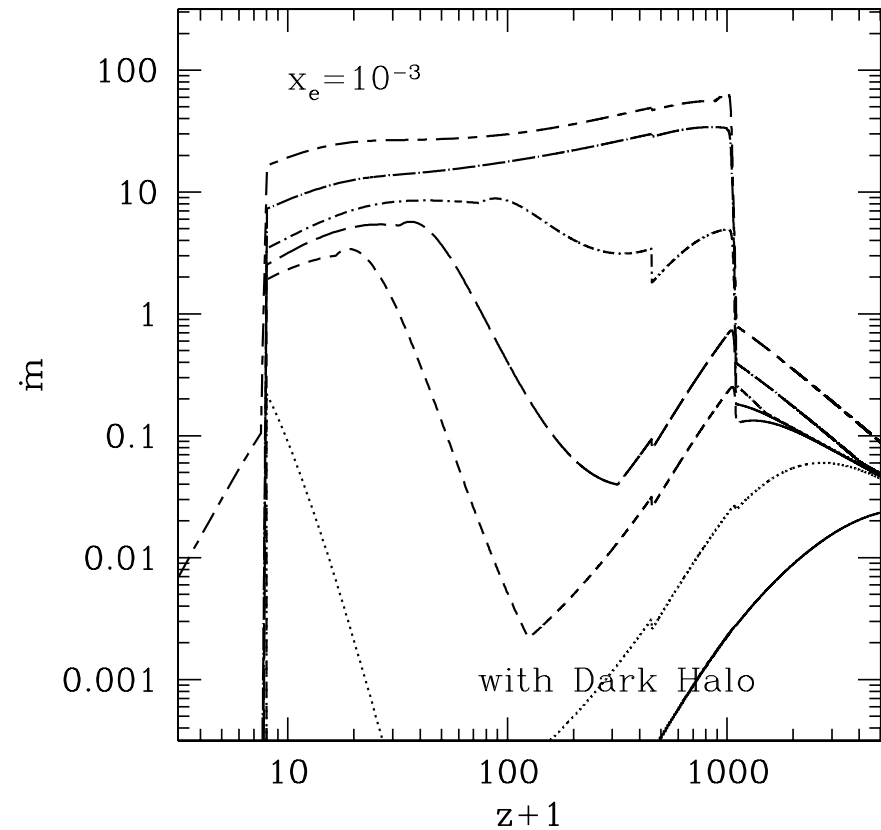
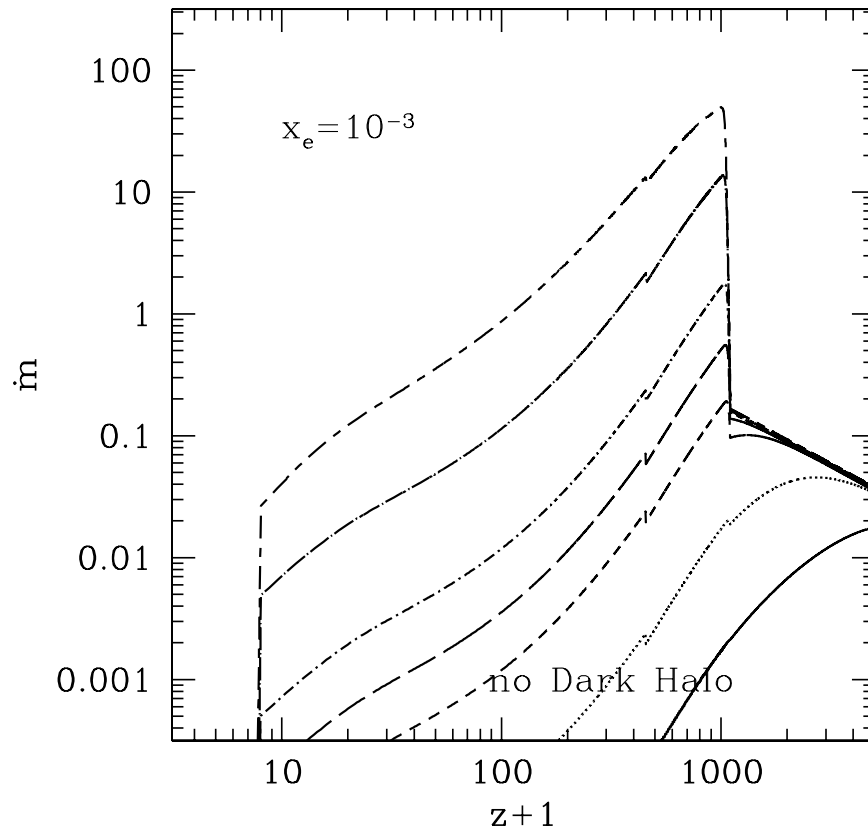
2. Non-linear regime: capture by mini-halos



# *Angular momentum of accreted material*

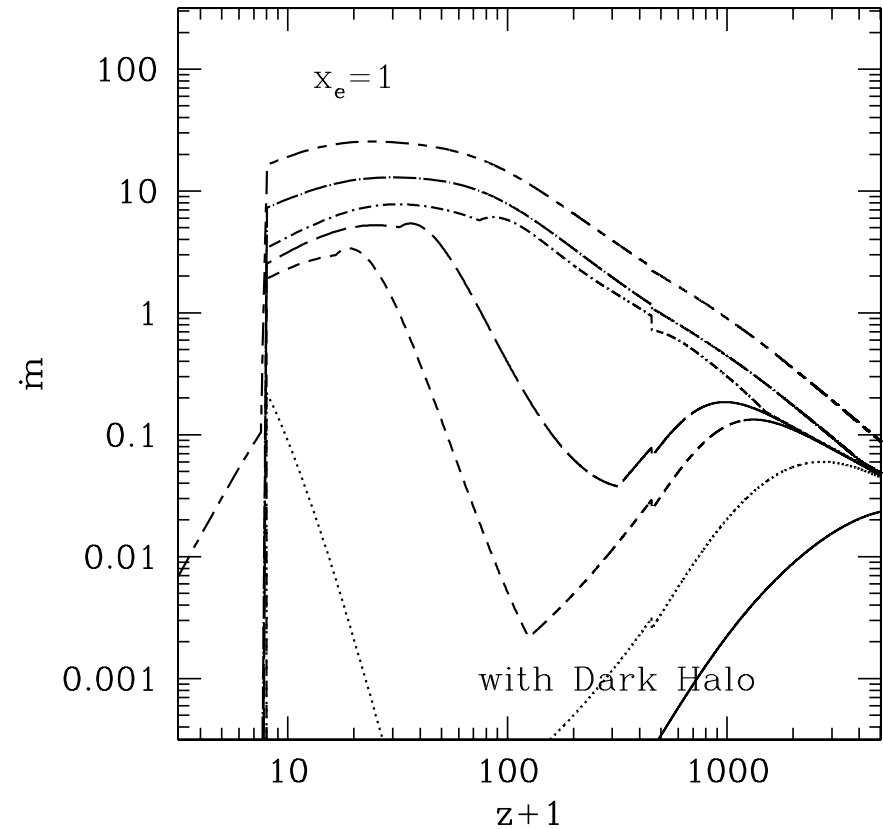
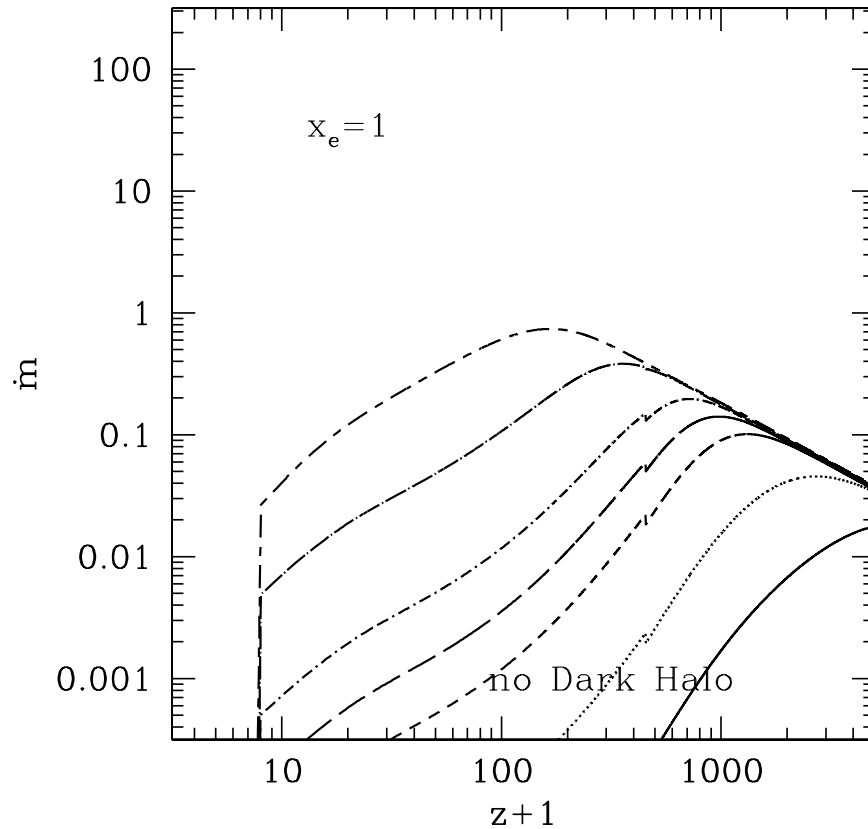
- Dark matter:
  - Quasi-spherical accretion
  - Ang. momentum sufficiently large to avoid direct accretion of DM into PBH
- Gas:
  - Spherical accretion for  $M < 500 M_{\odot}$
  - Compton drag reduces further ang. momentum (Loeb 93; Umemura et al 93)

# 4. Accretion rate neglecting feedback



curves from bottom to top refer to masses of PBHs from  $0.1 M$  to  $10^5 M$  (factor of 10 spacing).

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# Accretion Luminosity

Define dimensionless luminosity  $l = L/L_{\text{Ed}}$  and accretion rate  $\dot{m} = \dot{M}/\dot{M}_{\text{Ed}}$ , then:

$l = \eta \dot{m}$ , where  $\eta$  is the radiative efficiency

We assume:

- $l = 0.01\dot{m}^2$  if  $\dot{m} < 1$  (spherical accretion)
- $l = f_{\text{duty}}(0.1\dot{m}) < f_{\text{duty}}$  if  $\dot{m} > 1$  (thin disk)

# 5. Feedback processes

- Local feedbacks (typically negligible)
  - Size of H II region with respect to Bondi radius:
  - In most cases  $r_{\text{H II}}/r_{\text{B}} < 1$
  - If  $r_{\text{H II}}/r_{\text{B}} > 1$

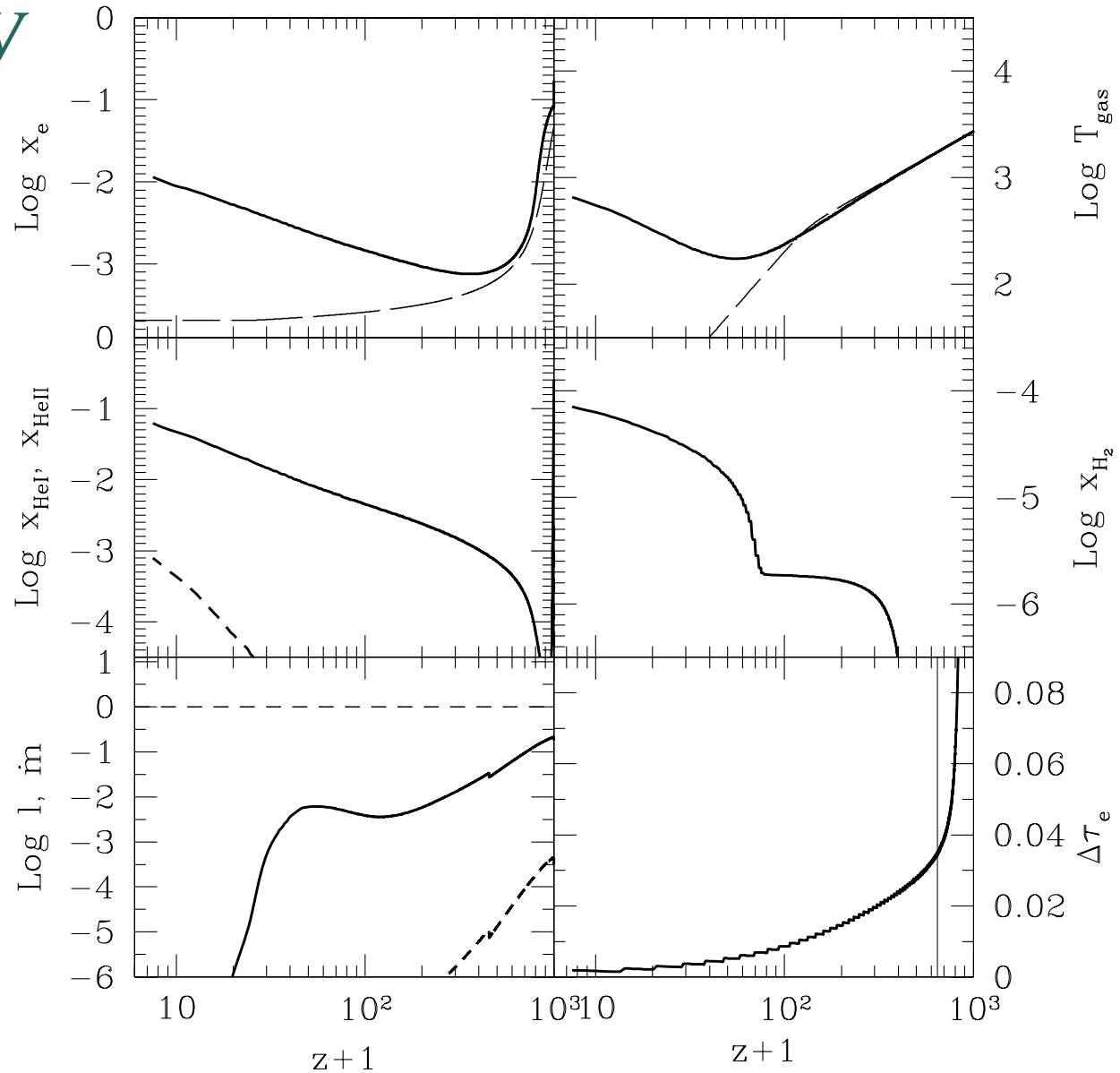
$$I_t = \frac{I}{1 + t_{\text{off}}/t_{\text{on}}} = \frac{I}{1 + (r_{\text{H II}}/r_{\text{B}})^{1/3}} = f_{\text{duty}} I$$

- Temperature of H II region:  $T_{\text{H II}} \gg T_{\text{cmb}}$
- Global feedback (X-ray heating):  
Iterative semi-analytic code (Ricotti & Ostriker 04)



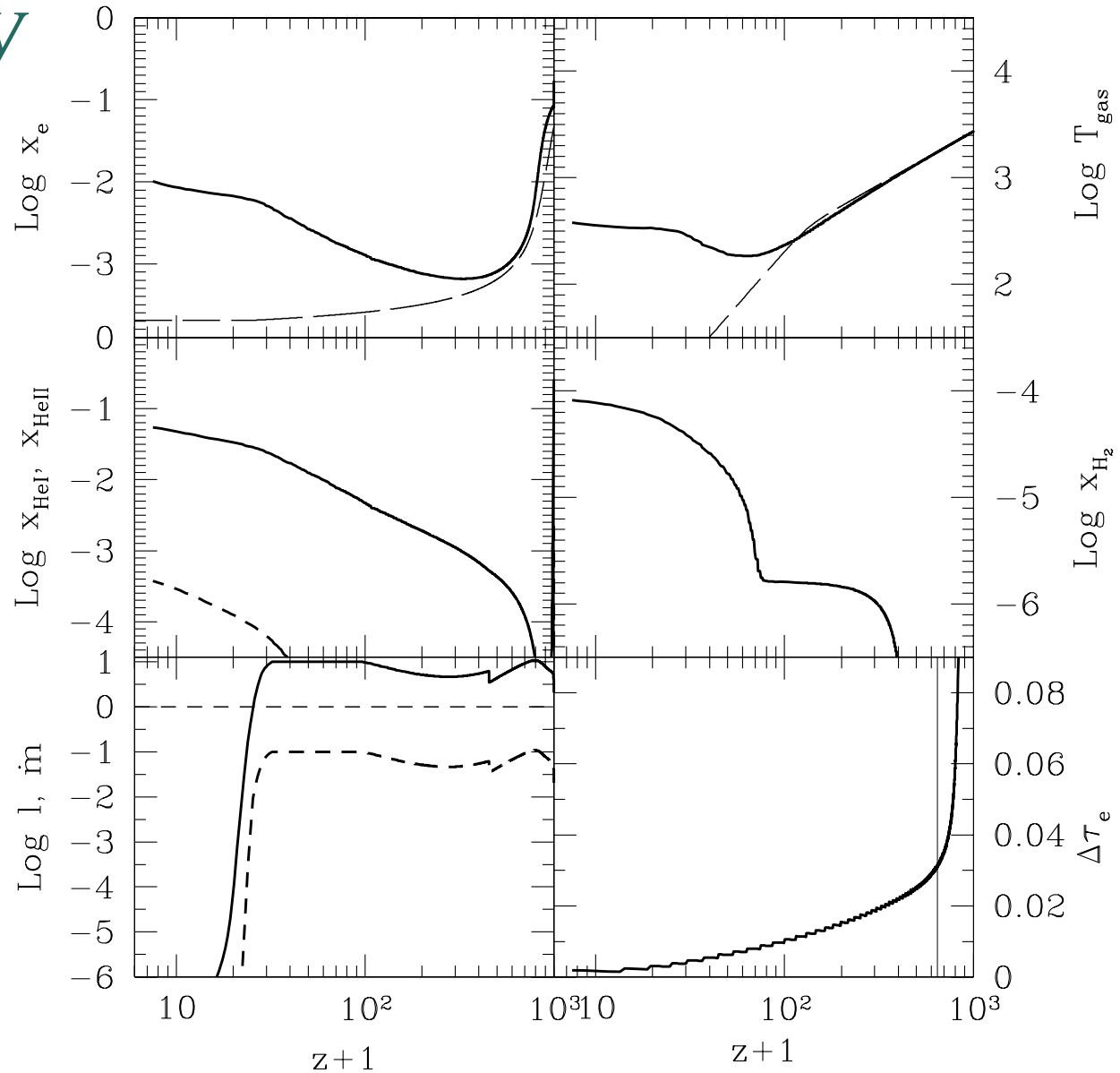
# Cosmic ionization, thermal, and chemical history

**Simulations:**  
 $M_{\text{pbh}} = 100,$   
 $f_{\text{pbh}} = 10^{-4}$



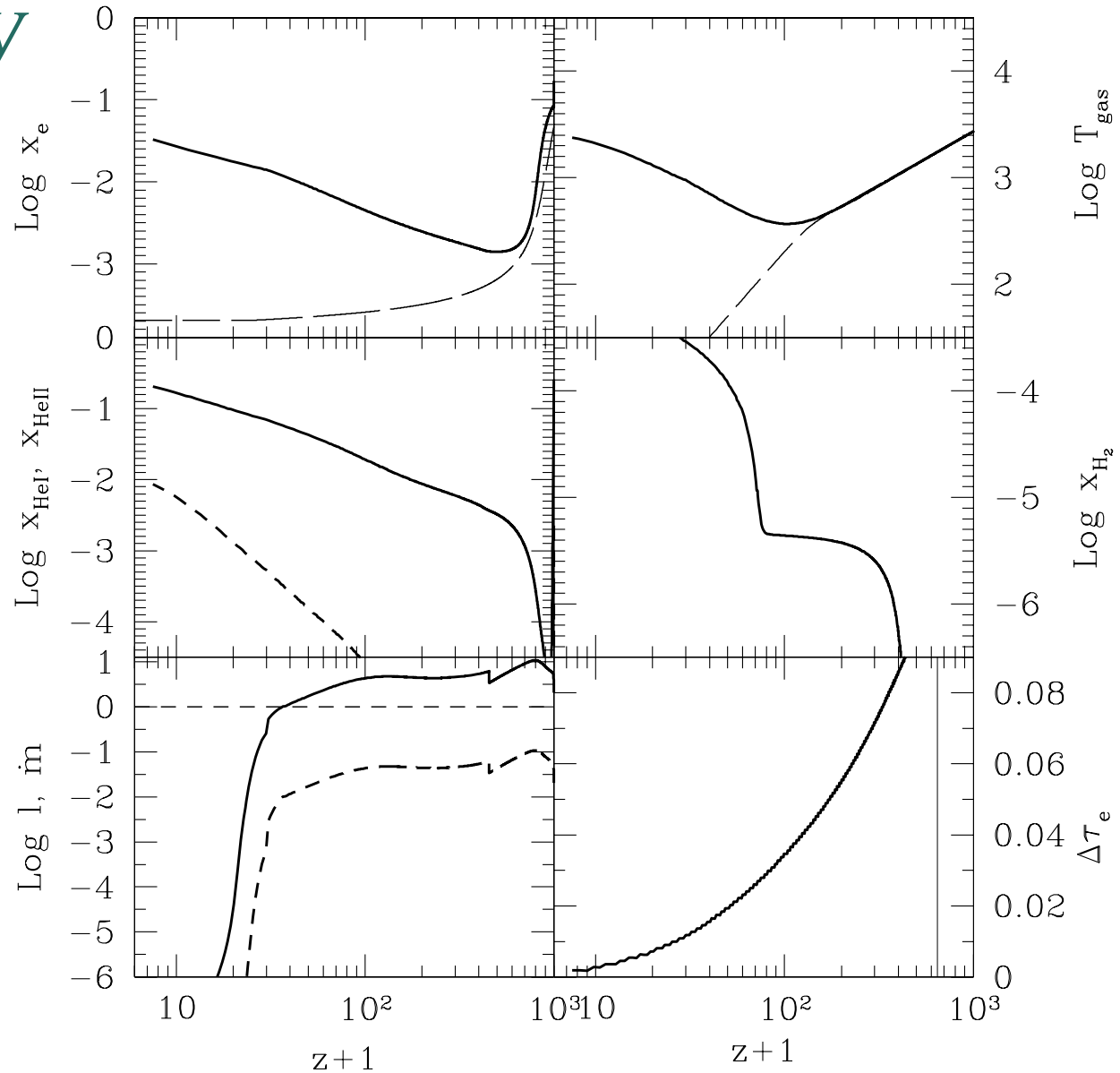
# Cosmic ionization, thermal, and chemical history

Simulations:  
 $M_{\text{pbh}} = 1000,$   
 $f_{\text{pbh}} = 10^{-7}$

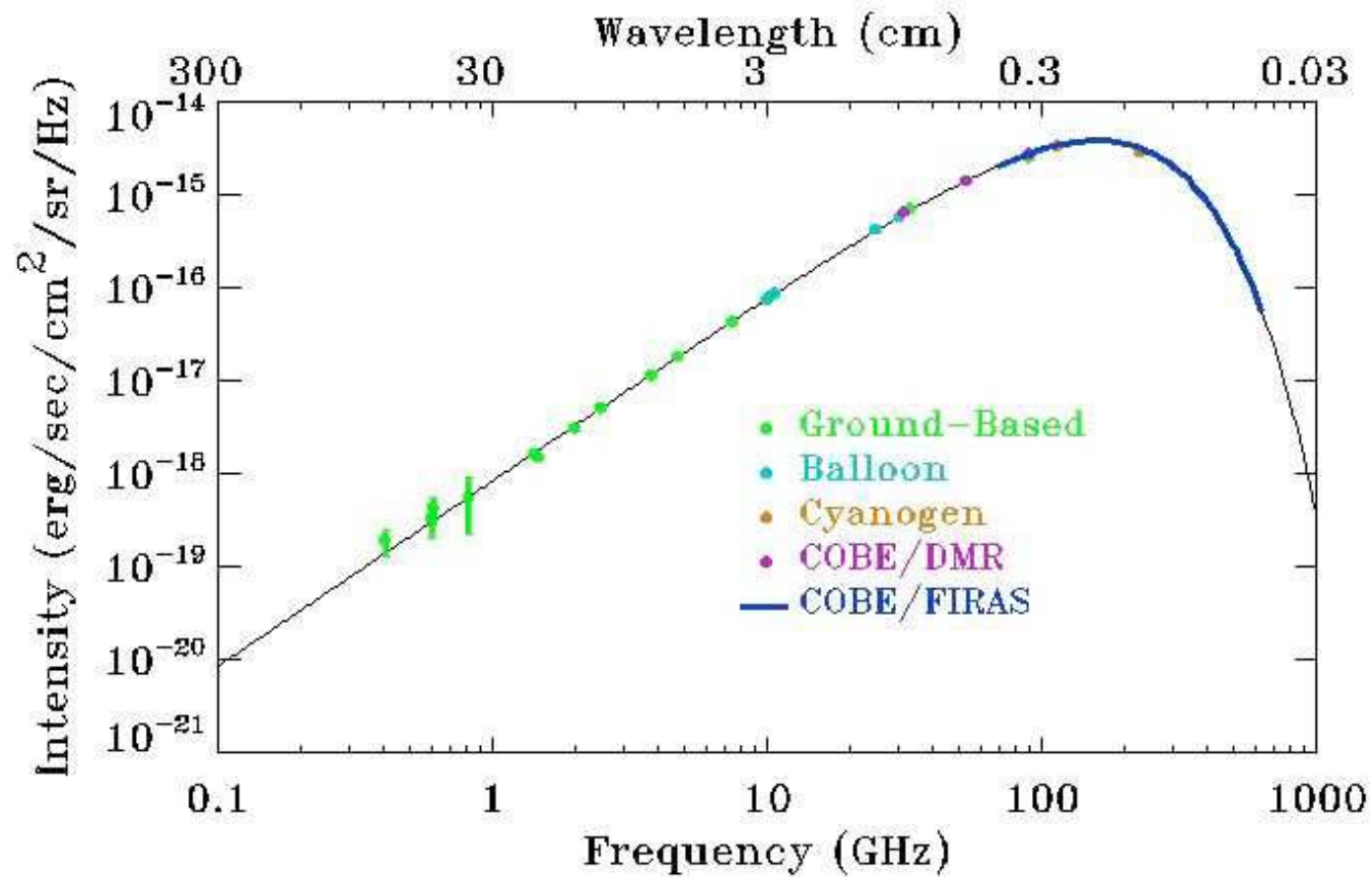


# Cosmic ionization, thermal, and chemical history

Simulations:  
 $M_{\text{pbh}} = 1000,$   
 $f_{\text{pbh}} = 10^{-6}$



# Spectrum of the CMB



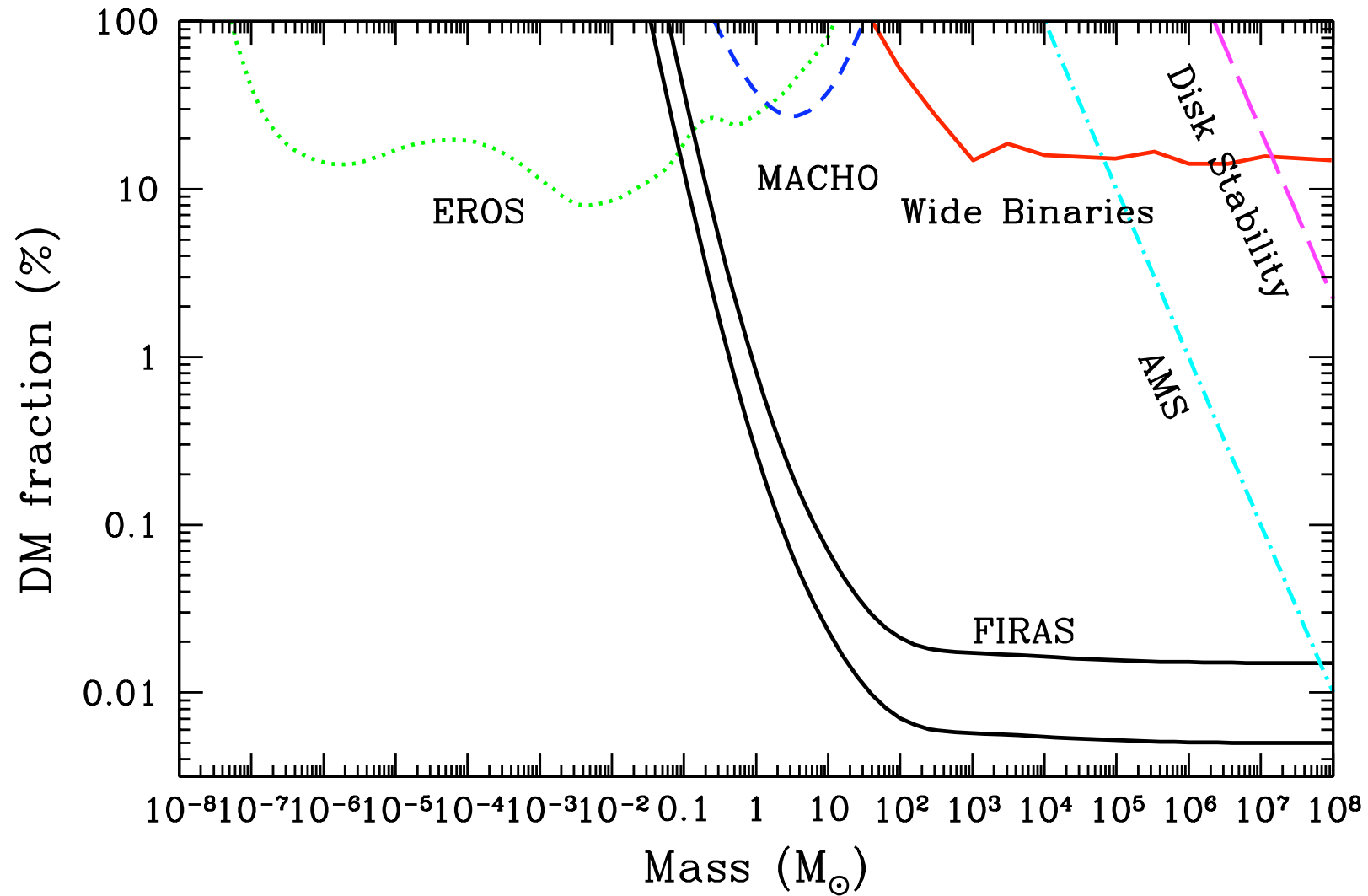
# CMB spectral distortions

- $M_{\text{pbh}} < 10 M_{\odot}$  weakly affected by Compton drag even before recombination
- FIRAS  $y = 1.5 \times 10^{-5}$  at 95% confidence
- 3 phases:  $y = y_1 + y_2 + y_3$ 
  1.  $z_{\text{rec}} < z < z_{\text{eq}}$ : all energy injected absorbed by gas
  2.  $z_{\text{dec}} < z < z_{\text{rec}}$ : fraction of energy absorbed by gas
  3.  $z < z_{\text{dec}}$ : Compton heating becomes negligible

Constrain on maximum energy injection imposed by:

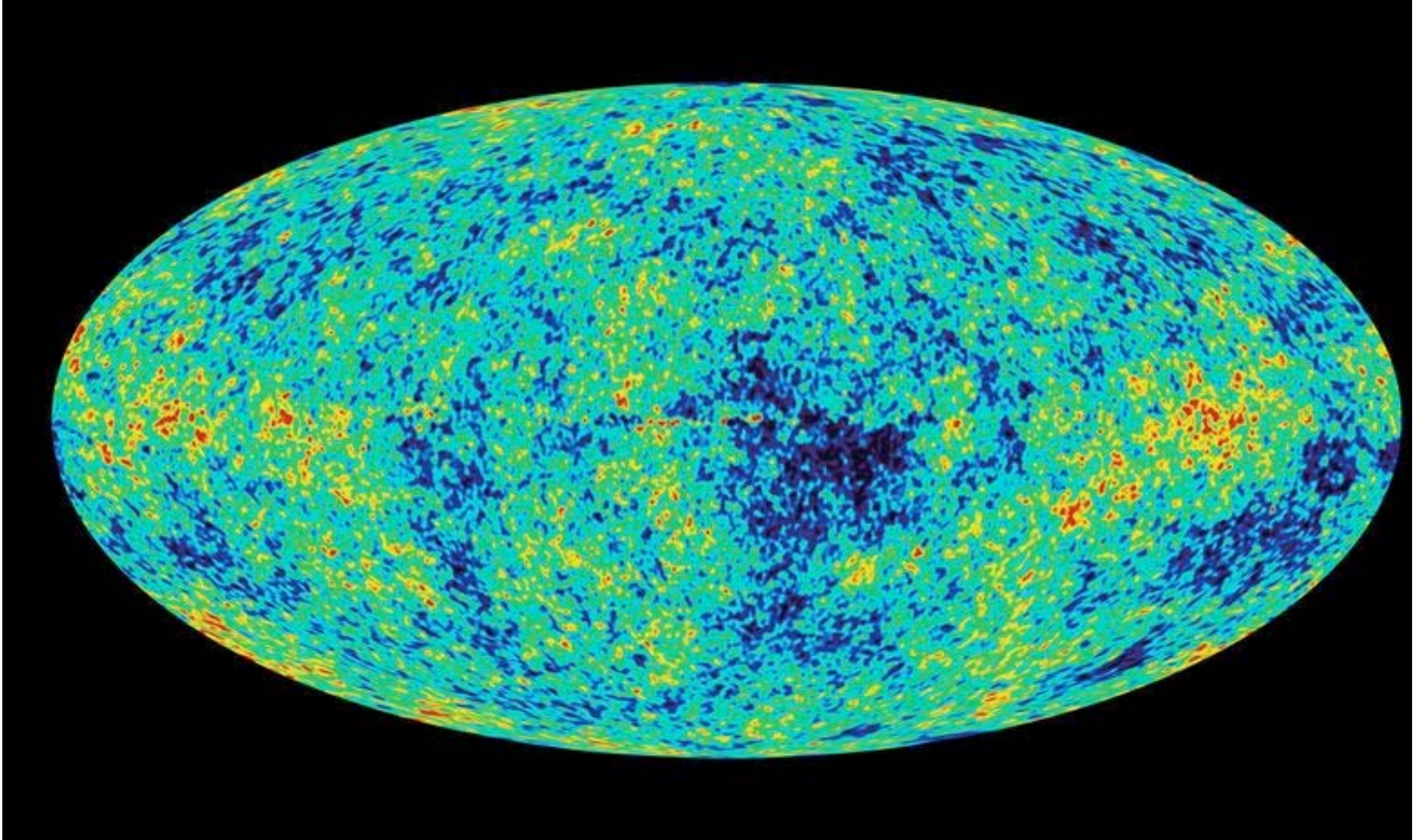
$$y = \frac{1}{4U(z_{\text{eq}})} \int_{z_{\text{eq}}}^{z_{\text{rec}}} \frac{dz}{aH(z)} \frac{dU(z)}{dt} \approx 1.5 \times 10^{-5}$$

# Constraints on $f_{PBH}$



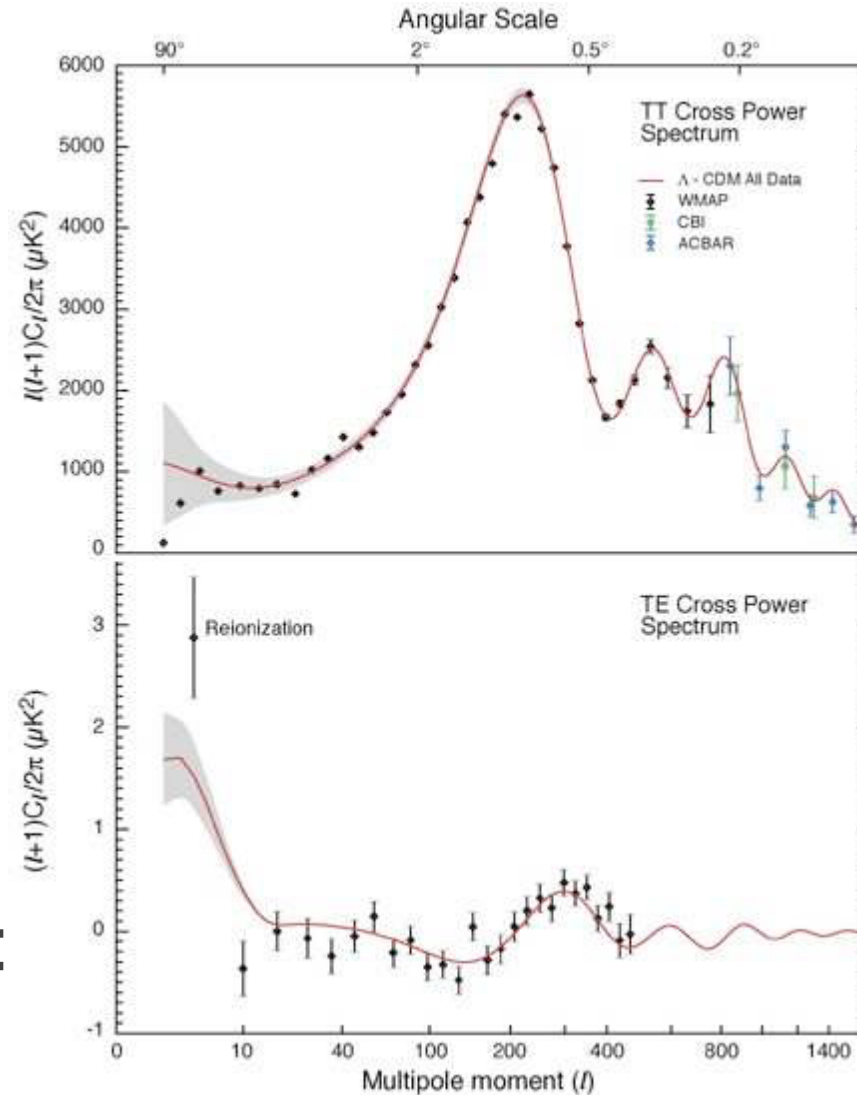


# *CMB anisotropies: WMAP*



# CMB anisotropies: spectrum

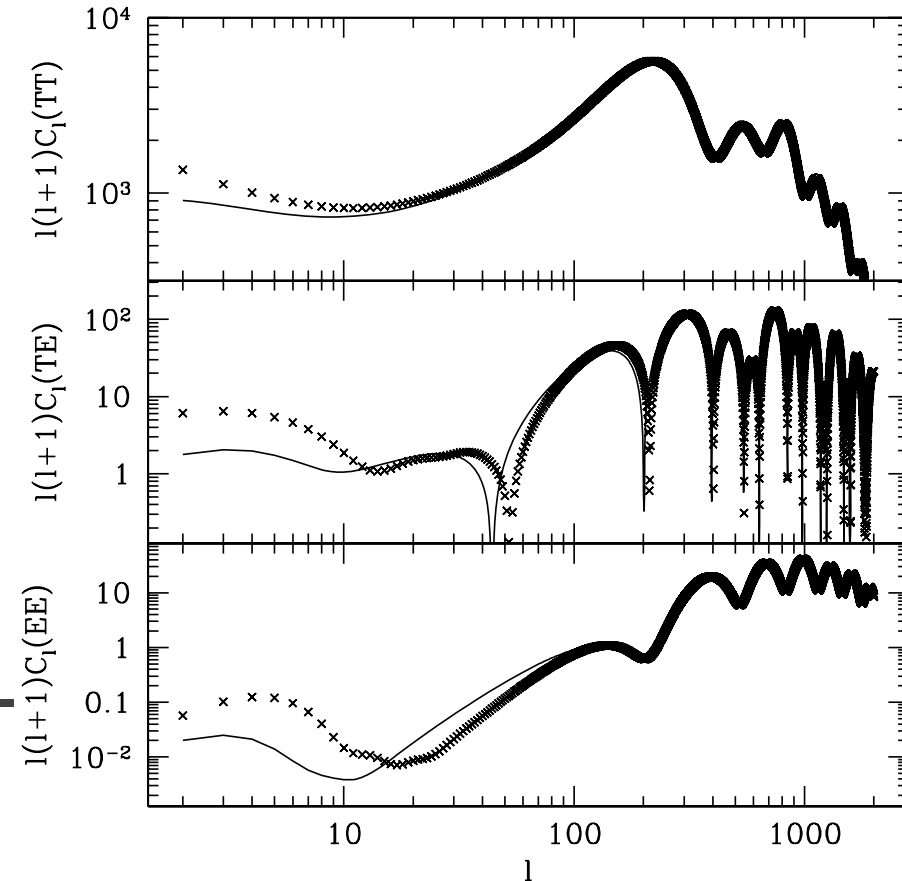
- Cosmological parameters:  
 $\Omega_m = 0.24, \Omega_b = 0.046, h = 0.73$
- Initial density perturbations:  
 $\sigma_8 = 0.74, n_s = 0.95$  (little power at small scales!)
- Ionization history:  
 $z_{\text{rei}} = 12, \tau = 0.1$





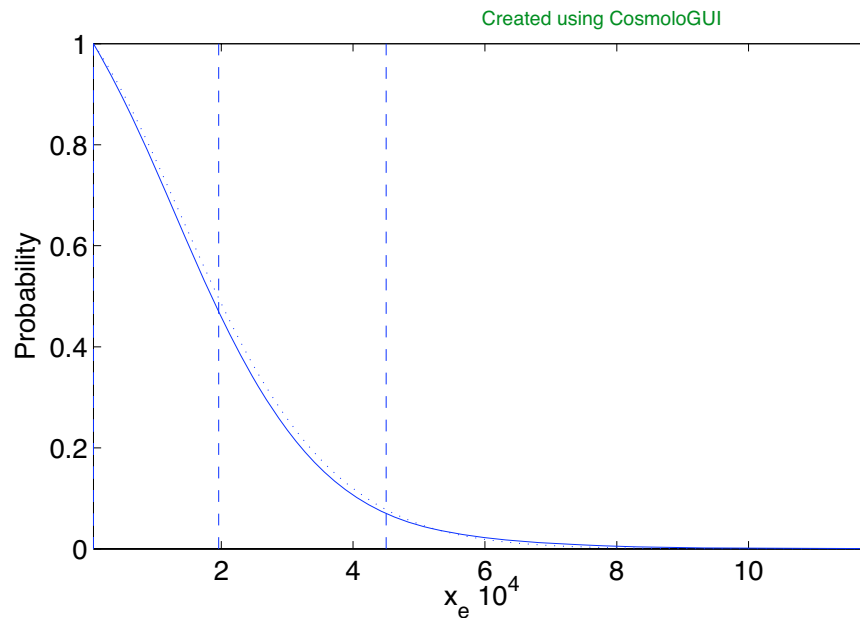
# Effects of PBHs on CMB anisotropies

- Affects recombination
- Complementary and uncorrelated to reionization effects
- Affect small angular scales:  $l > 10$



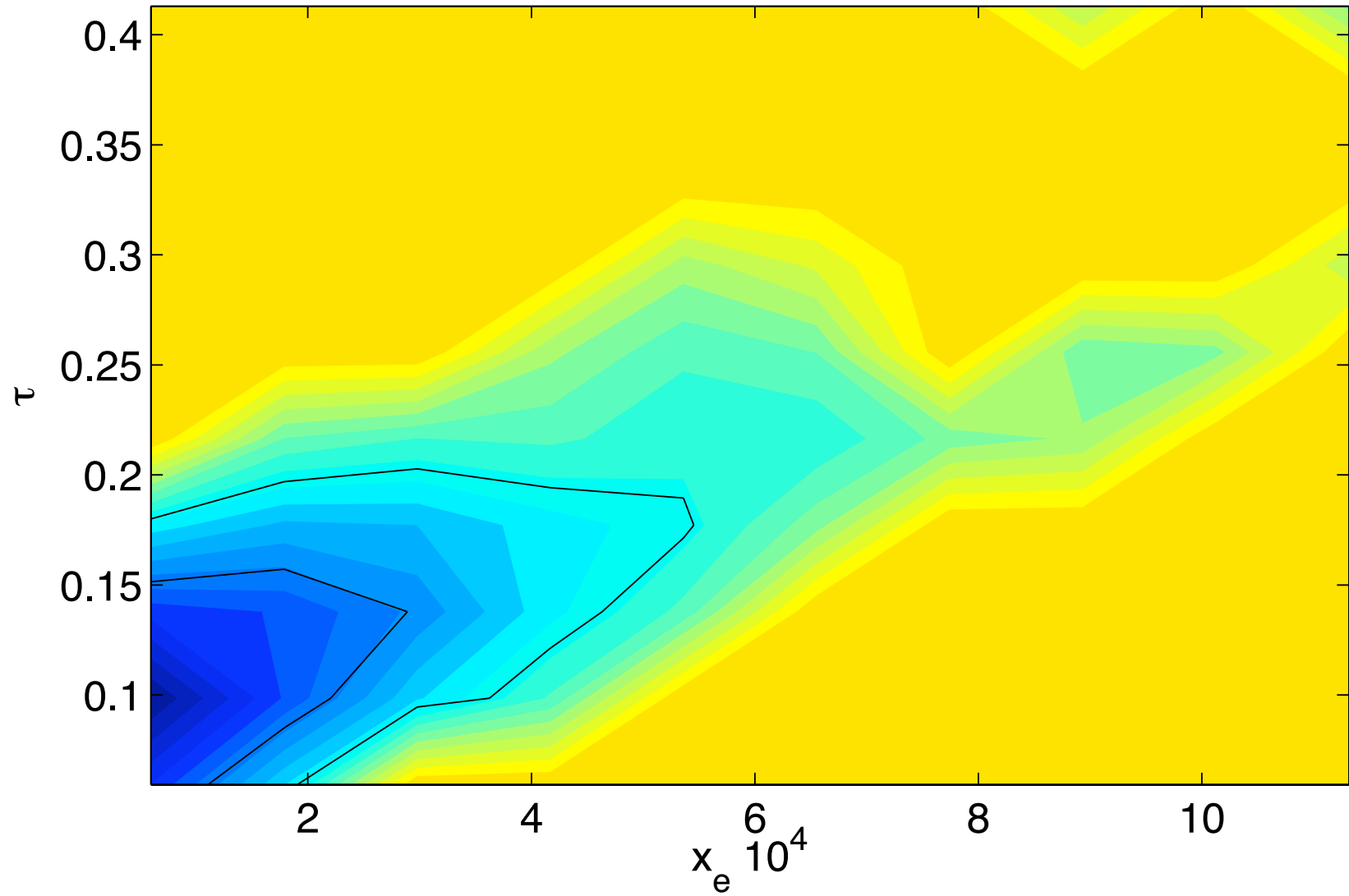
# Modified recombination history

$$x_e(z) = x_{e,\text{rec}}(z) + \min \left( x_{e0} \frac{1+z}{1000}, 0.1 \right)$$

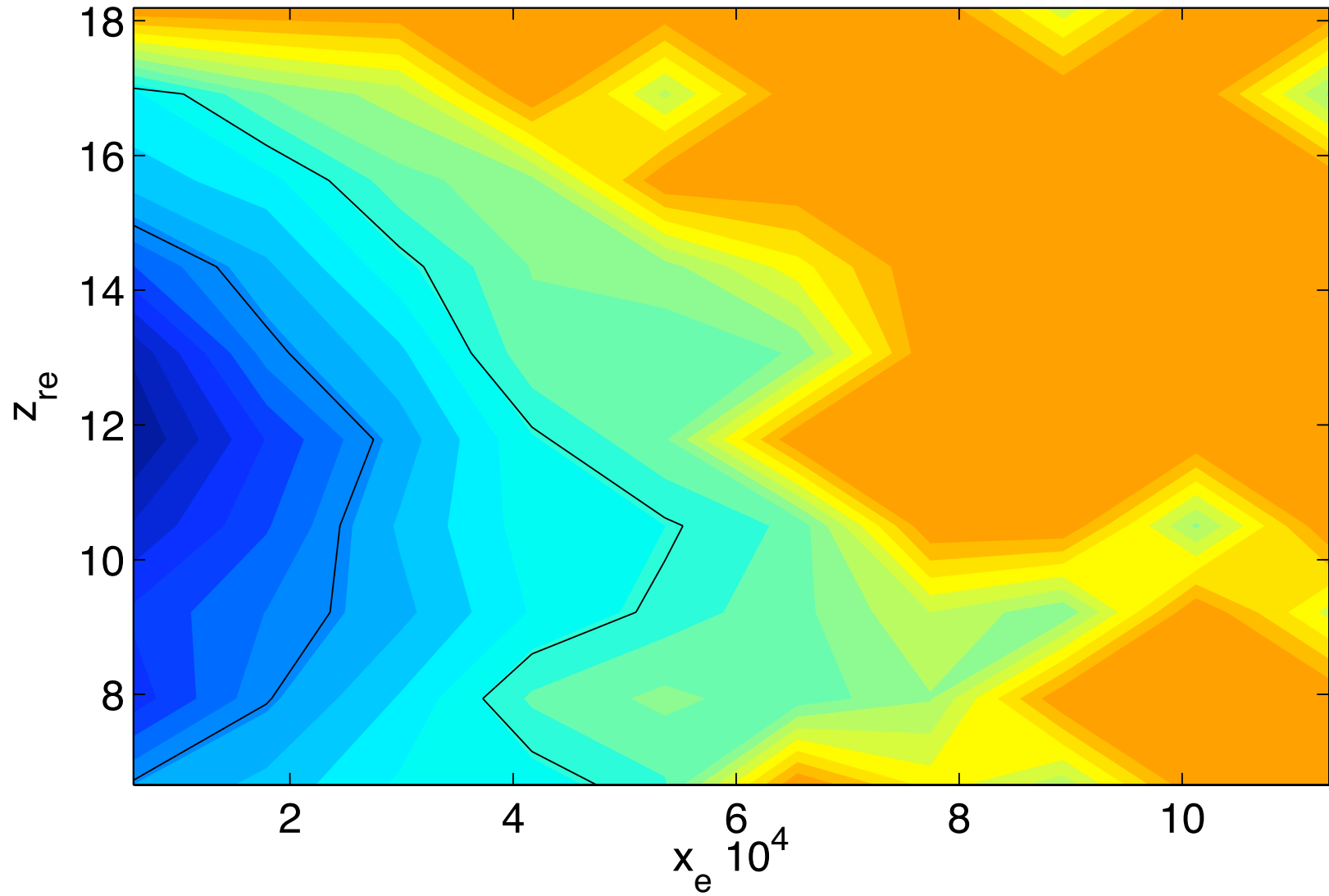


RECFAST: Seager, Sasselov & Scott 99;  
COSMOMC: Lewis & Bridle 02

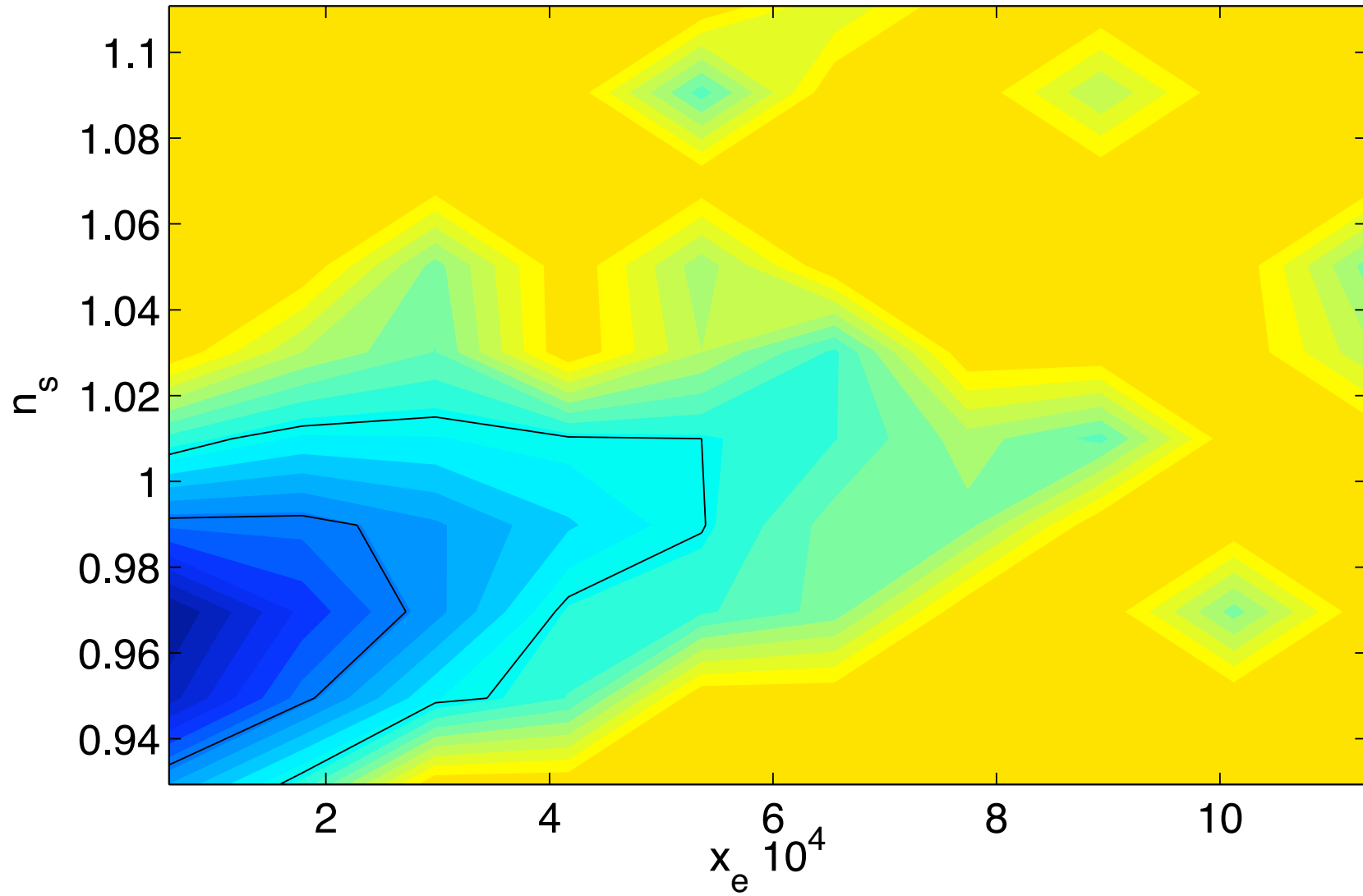
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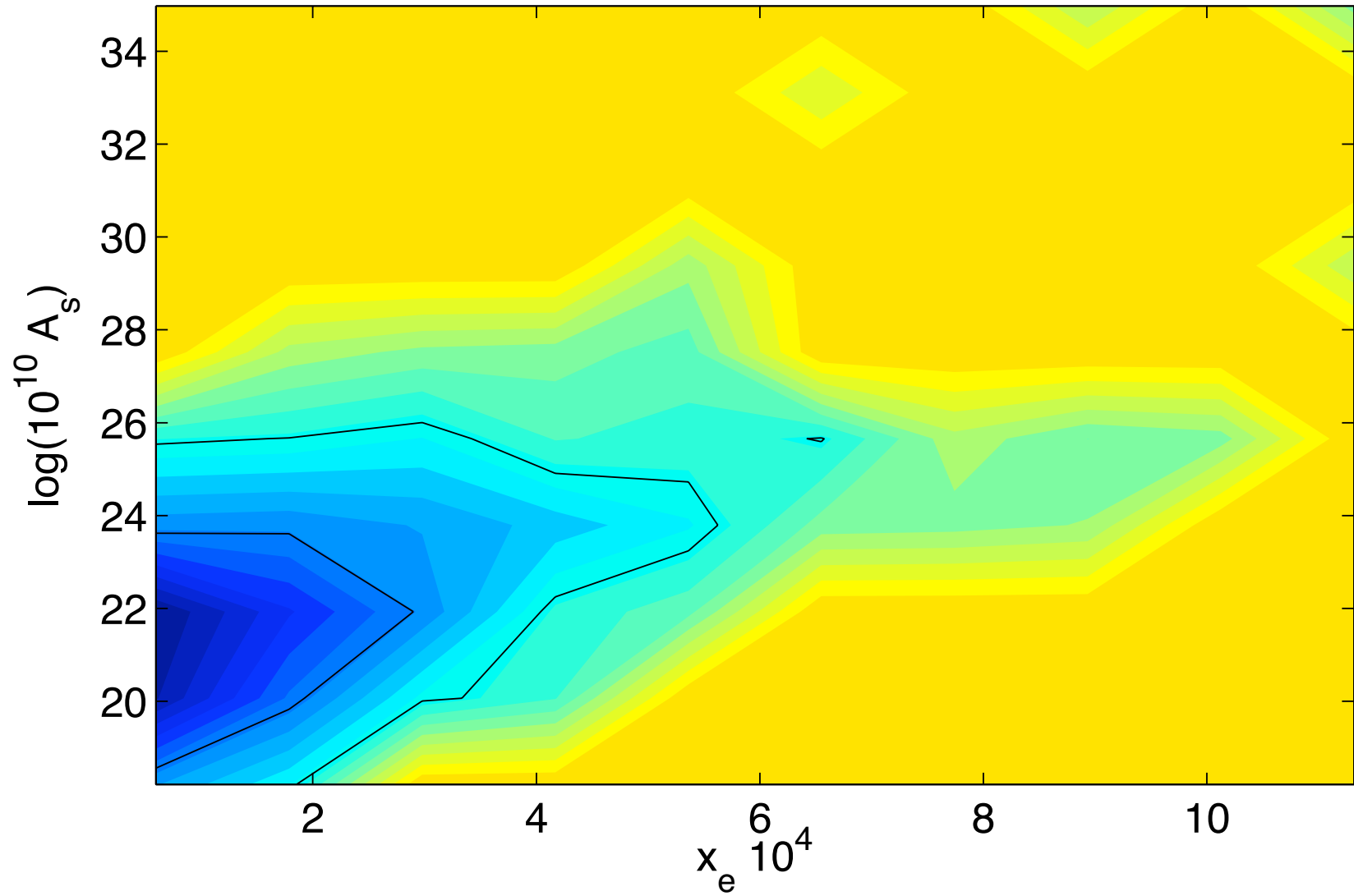
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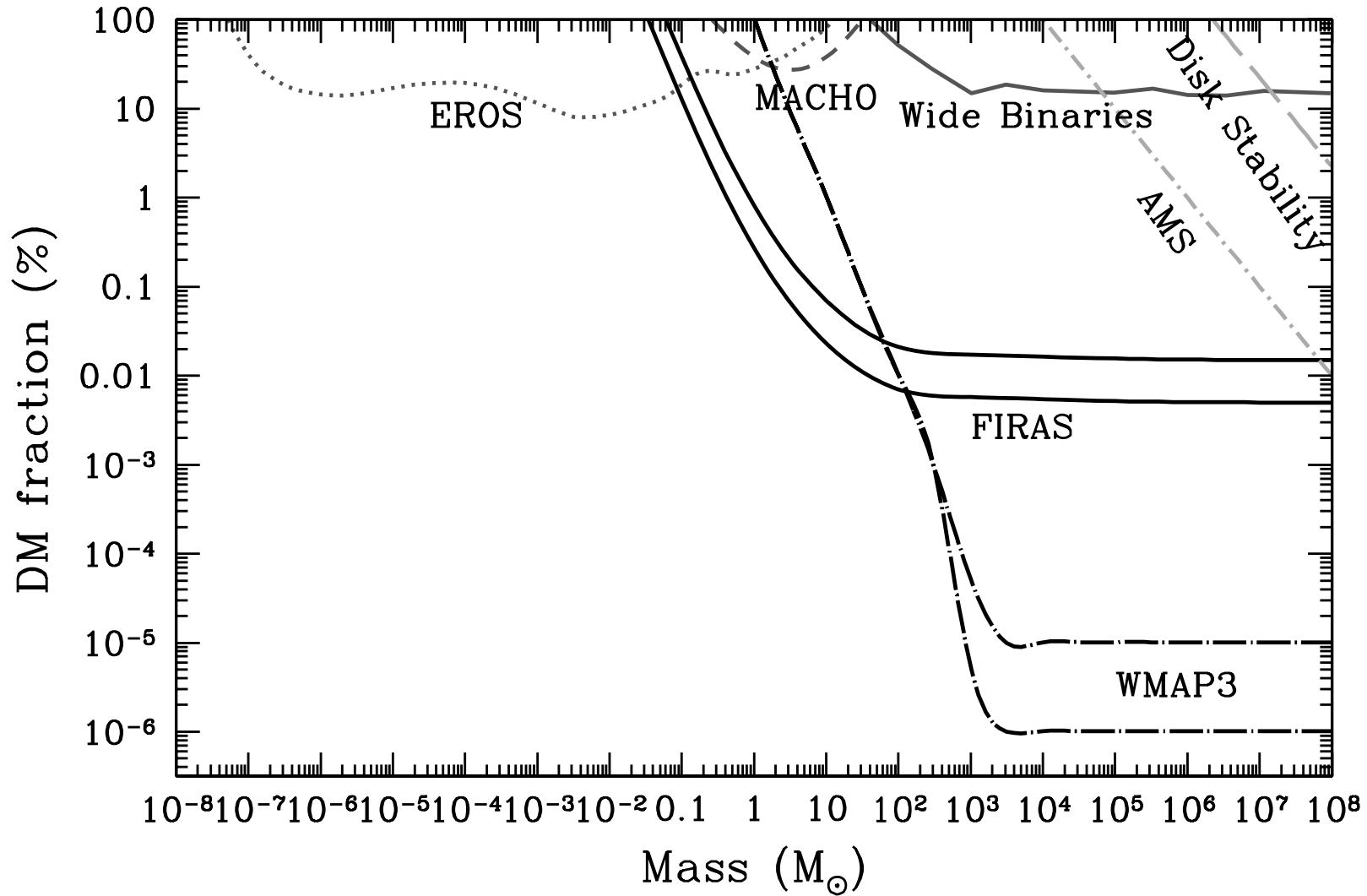
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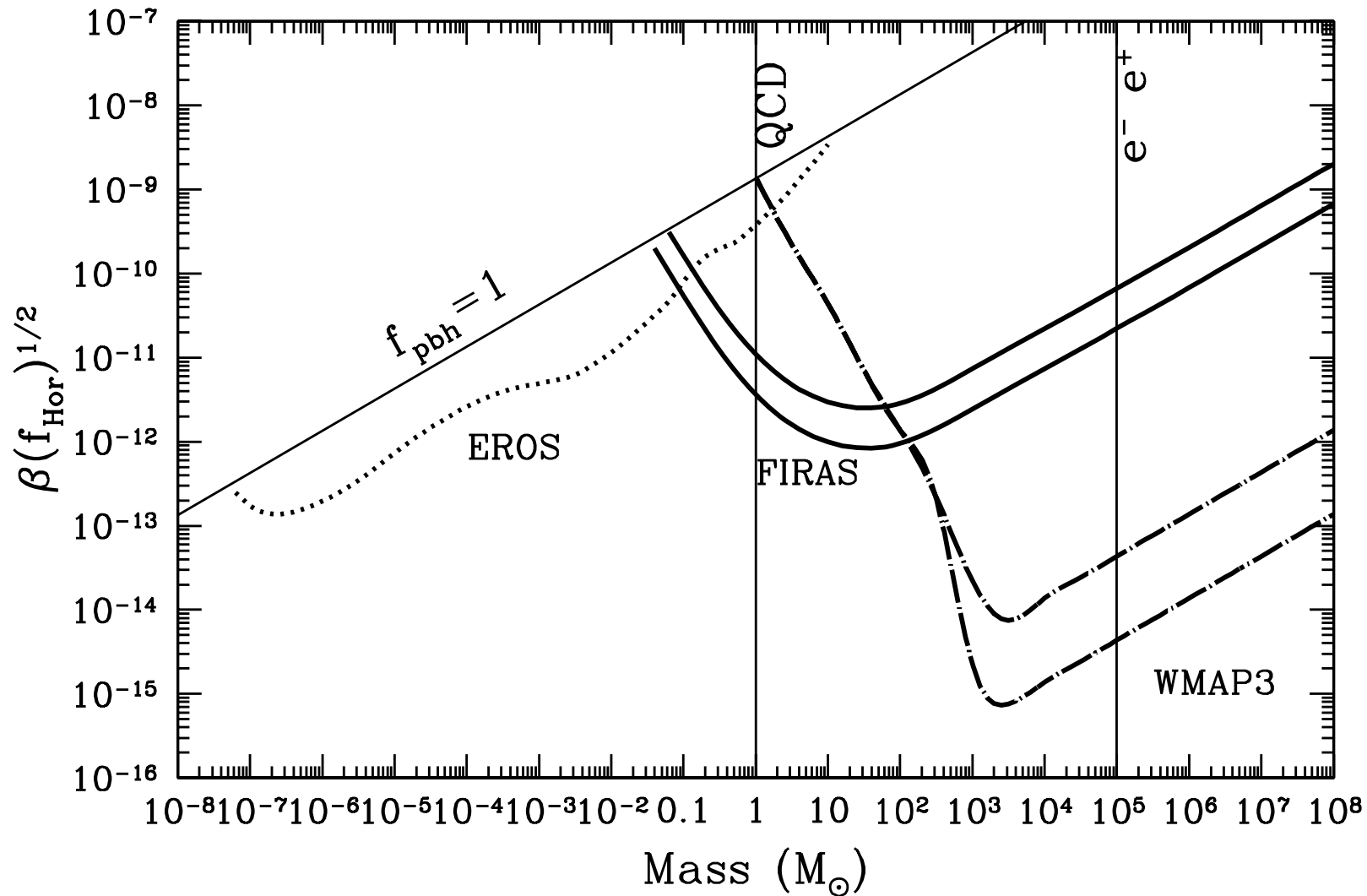
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- Upper limits on  $f_{\text{pbh}}$  improved by a lot:
  - PBHs more massive than the moon ( $\sim 10^{26}$  grams) cannot be the dark matter
  - PBHs may explain origin of ULXs and SMBHs

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