

Relativistic Shocks in Magnetized pair plasmas

Formation and short-term evolution

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- 1 General considerations
 - Relativistic collisionless shocks
 - Fermi acceleration at shocks
- 2 2D PIC simulations of $e^- - e^+$ Magnetized shocks
 - Simulation setup
 - Global structure
 - Jump conditions
 - Shock formation
- 3 Particle transport and acceleration
 - Distribution functions
 - Particle transport downstream
 - Summary

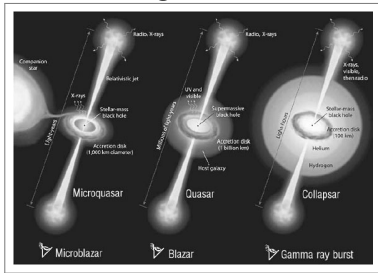
Relativistic Shocks in Astrophysics (I)

	Ex. astro	Size scale	Flow Lorentz Γ
AGN	Cyg A	Mpc	2-20
Micro-Quasar	SS433	pc	≥ 1 (?)
Pulsar wind	Crab (M1)	pc	$10^3 - 10^7$
GRB	GRB 110731A	10^{-2} pc	~ 100

$$\Gamma = 1/\sqrt{1 - V^2/c^2}$$

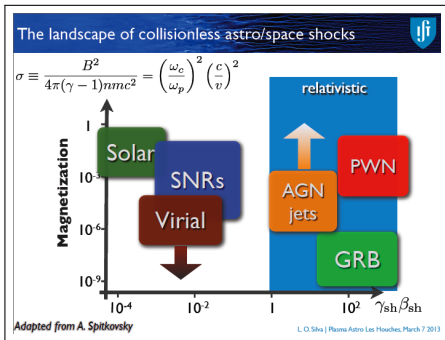
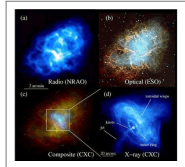
- Universal presence of accretion disks and powerful jets.
- Radiate high energy photons (up to TeV energy)
- Accelerate particles above TeV/nucleon
- Amplify magnetic fields (or generate from scratch)

Jets : similar mechanism on different scales as origin of such shocks.



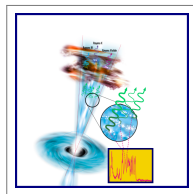
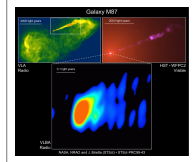
Relativistic Shocks in Astrophysics (II)

Crab Nebula (M1)

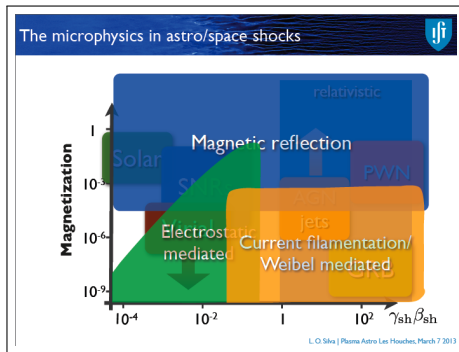


From L. Silva, Ecole des Houches, march 2013

M 87 : Virgo Galaxy



To the microphysics of shocks



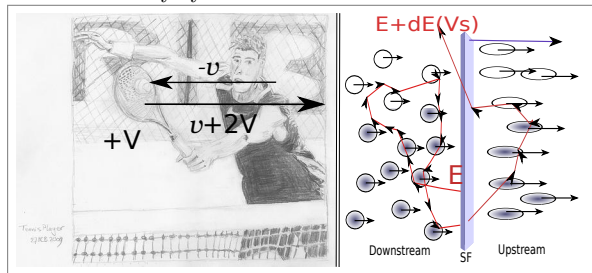
From L. Silva, Ecole des Houches, march 2013

→ Magnetization parameter (σ) : controls the shock structure and particle acceleration efficiency.

→ No complete theory of Magnetized relativistic collisionless shocks. While $\sigma = 0$ is well understood, and theoretical efforts in $0 < \sigma < 0.01$ limit (Lemoine & Pelletier 08,10; Plotnikov et al. 11,13; Lemoine et al. 13a,b), significant advances using PIC simulations (Sironi & Spitkovsky 09,11, Stockem et al 11, Sironi et al 13)...

Acceleration at shocks : Fermi I mechanism

Shocks : convergent flows with frozen-in magnetic turbulence.
Gain by cycles on both sides of the shock.

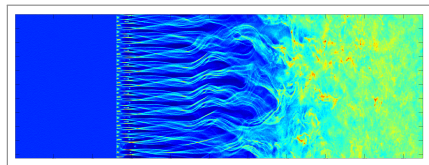


Krimsky 77, Axford et al. 77, Blandford & Ostriker 78, Bell 78 :

Diffusive Shock Acceleration by Fermi I mechanism : power-law particle distribution
 $f(E) \propto E^{-s}$, with $s \simeq 2$ (2.2 for UR shocks [Achterberg et al. 01](#))

Evidenced in long-term 2D-3D PIC simulations of rel. shocks (e.g. [Spitkovsky 08](#),
[Martins et al. 09](#), [Haugbolle 2011](#))

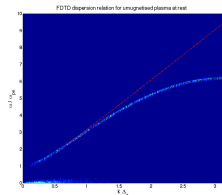
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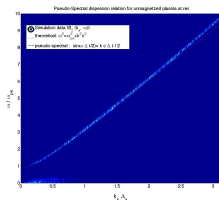
Simulation codes

Two types of codes used : FDTD 2D PIC code “Smilei” and a pseudo-spectral 2D PIC code “Shockpic”.// Dispersion relations of light waves from PIC codes :

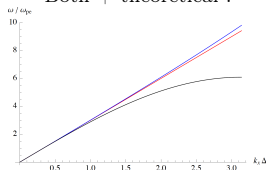
FDTD, “Smilei”



Spectral, “Shockpic”



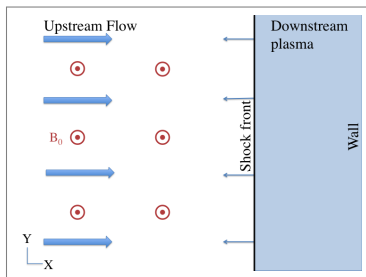
Both + theoretical :



- In theory we should get $\omega^2 = \omega_{pe}^2 + k^2 c^2$ for a light wave in an unmagnetized plasma. Significant deviation for FDTD solvers, more subtle for Spectral solvers
- The difference is less obvious on the other proper plasma wavemodes (Whistler, Langmuir, Bernstein modes)
- Different techniques to mitigate the spurious grid-Cerenkov instability

Simulations setup

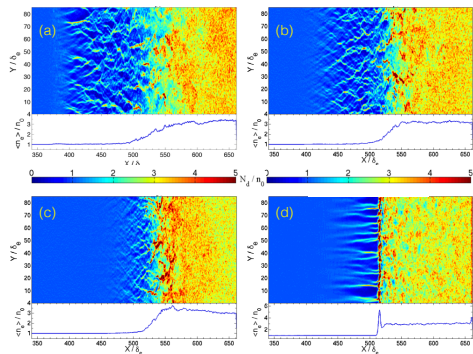
Shock is initiated by reflection of a cold $e^- - e^+$ beam on a reflecting wall at the right boundary (piston method) \rightarrow interaction of two beams is unstable and bulds a shock as seen from the shocked plasma restframe.



- Time : Simulations done up to $2000\omega_{pe}^{-1}$ and $< 500\omega_{pe}^{-1}$ with the *Smilei* and *Shockapic* codes, respectively (Sironi et al 13. : $> 10^4\omega_{pe}^{-1}$)
- Resolution : grid size is $\simeq \delta_e/4$ and the box transverse size $\simeq 256\delta_e$
- Noise : 20 part./cell (2 for *Shockapic*)
- Grid : 20 simulations exploring $\sigma \in [10^{-6}, 0.1]$ with each code. Complementary $\sigma = 0$ and > 0.1 runs.

Global structure for different σ (I)

Density maps of $\gamma_0 = 10$ shocks at
 $t\omega_{pe} = 300$



$\sigma = 10^{-5}$ (a), 10^{-4} (b), 10^{-3} (c) and $3 \cdot 10^{-2}$ (d).

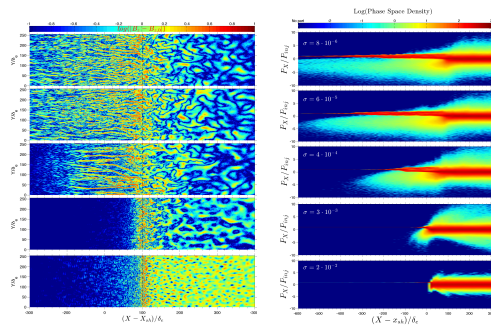
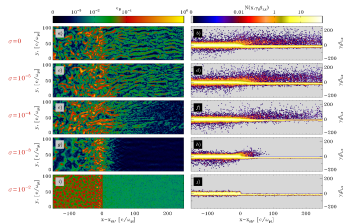
- Shock front thickness $\simeq 10 - 50\delta_e$
- $\sigma = 0$ (a) : Weibel-filamentation governed shock structure.
- At intermediate $10^{-5} < \sigma < 10^{-2}$ (b,c) : the filaments in the precursor are slightly oblique. The precursor lengthscale is governed by the upstream magnetic field amplitude. About a Larmor radius of returning particles with energy $\gamma_0 m_e c^2$: $\ell_p \sim R_L = \gamma_0 m_e c^2 / (eB_0)$ (e.g. Lemoine & Pelletier 2010).
- For $\sigma > 10^{-2}$ (d) : no particle precursor, strong EM emission from the front (see, e.g. Gallant et al. 92). Overshoot structure at the front. Apparent filamentary structure disappears in later simulation times.

Global structure for different σ (II)

Magnetic turbulence and phase-space structure as function of σ .

- Recover very similar structure to the one presented by [Sironi et al 13](#)

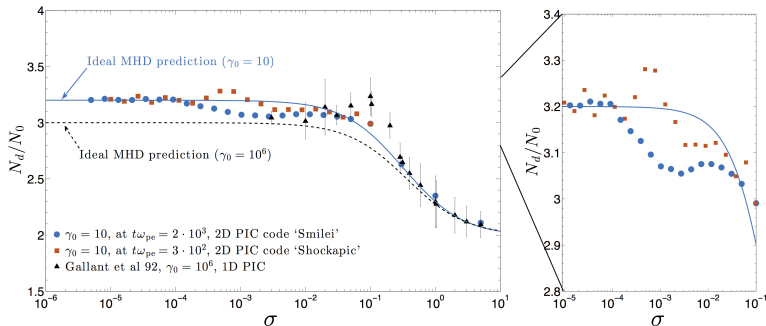
$\gamma_0 = 10$ shocks at $t\omega_{pe} = 2000$
 Left $|B_z - B_{z,0}|$, Right : $x - p_x$.



Shock Jump conditions : density

Compression ratio N_d/N_0 from simulations as function of σ .

Solid lines : ideal MHD prediction from conservation laws expressed in the downstream frame.



At low $\sigma < 10^{-4}$ consistent with the unmagnetized jump $[\Gamma_{\text{ad}} - 1](\gamma_0 - 1)/(\gamma_0\beta_0)$ (Blandford & McKee 76, Kirk & Duffy 99, Spitkovsky 08). At high σ , $N_d/N_0 \rightarrow 2$.

Notable deviation when $10^{-4} < \sigma < 0.1$.

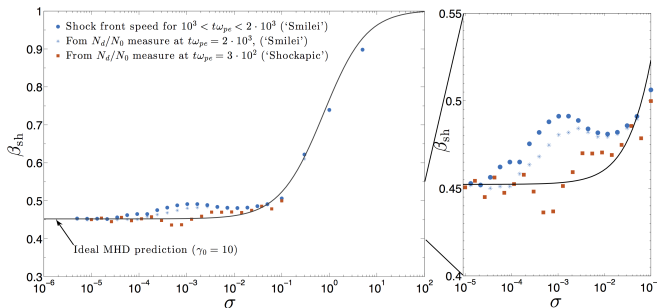
Front speed

Derivation of the MHD front speed as seen from the downstream (strong shock limit) gives

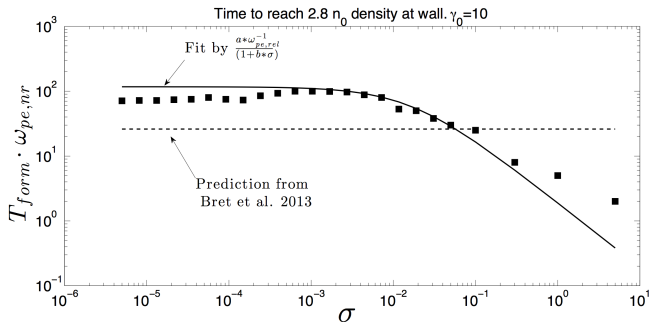
$$\beta_f = \frac{2(\gamma_0 - 1)(\Gamma_{\text{ad}} - 1) + \Gamma_{\text{ad}}\gamma_0\sigma + \sqrt{8(\gamma_0^2 - 1)\sigma(1 + \sigma)(2 - \Gamma_{\text{ad}}) + [2(\gamma_0 - 1)(\Gamma_{\text{ad}} - 1) + \Gamma_{\text{ad}}\gamma_0\sigma]^2}}{4(1 + \sigma)\sqrt{\gamma_0^2 - 1}}$$

→ Consistent with [Spitkovsky 08](#) in $\sigma = 0$ limit and with [Kennel & Coroniti 84](#), [Lemoine et al 16](#) for $\Gamma_{\text{ad}} = 4/3$ ($3/2$ here because 2D plasma). For $\sigma > 1$, $\beta_f \rightarrow 1$.

Comparison with simulations :



Shock formation timescales



$$\rightarrow T_{\text{form}} \propto \omega_{pe,rel}^{-1} \propto \sqrt{\gamma_0} \omega_{pe}^{-1} \text{ for all } \sigma$$

$$\rightarrow T_{\text{form}} \propto \omega_{pe,rel}^{-1} / \sigma \text{ when } \sigma \text{ close to unity}$$

Case of a $\sigma = 10^{-5}$ shock

- Well-studied case (Silva et al. 03, Spitkovsky 08, Sironi et al 13, Bret et al 13)
- Initial flows overlap is Weibel-filamentation unstable at a $\sim \delta_e \sqrt{\gamma_0}$ scale.
- Currents reach the Alfvén limit and build up the shock (magn. energy grows up to the level when the oncoming flow is stopped)
- Precursor beam of reflected/accelerated electrons \rightarrow Weibel structured precursor by interaction of hot beam with cold upstream flow

Case of a $\sigma = 10^{-3}$ shock

- Mixed case. Filamentation still dominant but accumulation is observable at the tip of the reflected flow.
- Slightly oblique filaments
- Measurable rms perp current in the precursor.

Case of $\sigma \geq 0.01$ shocks

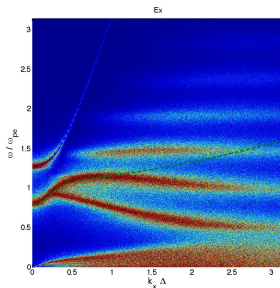
Evolution of J_{\perp} for a $\sigma = 0.01$,
 $\gamma_0 = 30$ shock.

Density accumulation at the tip of interpenetrating beams \rightarrow Shell kicked towards downstream if pressure is not sufficient to support the shock front. Oblique filamentation (if possible) in the downstream forming region during shock formation.

Theoretical challenges

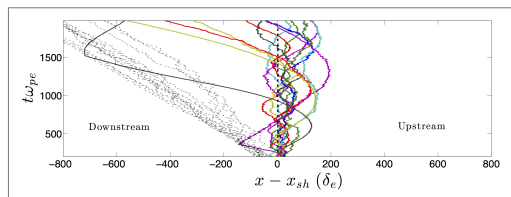
While the shock formation for a $\sigma = 0$ shock was conveniently described by [Bret et al 13](#) and a model of a $\sigma \gg 1$ shocks is described by [Alsop & Arons 88](#), [Gallant et al. 92](#), the case of $0 \ll \sigma < 1$ is more involved

Transverse to \vec{B} plasma
 fluctuations for $\omega_{ce}/\omega_{pe} = 0.5$



- → Importance of the fluctuations study and beam-type instabilities
- X-mode (coupled to Bernstein modes) → Maser-synchrotron → Parallel to shock normal but involves transverse to \vec{B}_0 modes.
- Filamentation, aperiodic instability → Perp to the shock normal and to \vec{B}_0 .
- Convenient description needs to account for both with growing σ
- Role of third dimension in the shock structure?(e.g. Simulations of [Sironi et al 13](#))

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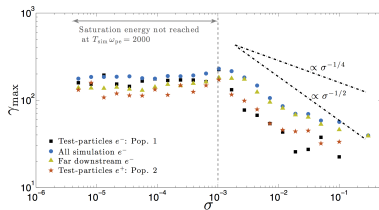
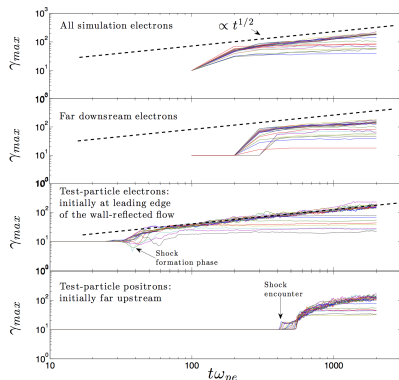


Downstream distribution for diff. magnetizations

Downstream distribution functions $f(\gamma)$

- For $\sigma \leq 10^{-4}$, acceleration similar to the unmagnetised shocks.
- For $\sigma \leq 10^{-3}$ slightly more rapid acceleration, but saturation energy reached at $t\omega_{pe} = 2000$.
- For $\sigma \geq 10^{-2}$ no supra-thermal component.
- Power-law tail index $s \simeq 2$. ?

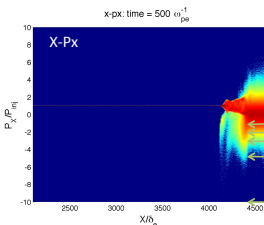
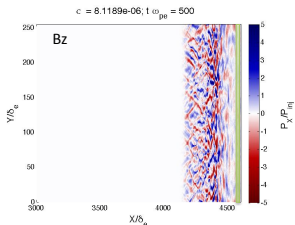
Maximal energy in time



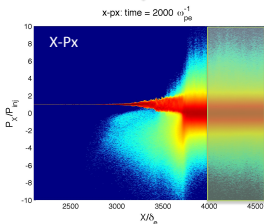
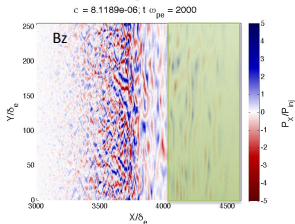
- $\gamma_{max} \propto t^{1/2}$ recovered, as found in [Stockem et al. 11](#), [Sironi et al. 13](#)
- ... γ_{max} is not saturated for $\sigma < 10^{-3}$ at the simulations end
 $= 2000\omega_{pe}^{-1} \simeq 600\omega_{pe,rel}^{-1}$. Probably not sufficient to fill the acceleration box and arrive to the saturation energy (as demonstrated by [Sironi et al. 13](#)).

Test-particles kinematics downstream (I)

Downstream turbulence \rightarrow Static decaying microturbulence.
 Particles injected from the wall at $t\omega_{pe} = 500$ with $\vec{p} = p_x \vec{n}$
 \rightarrow Experience downstream decaying turbulence.



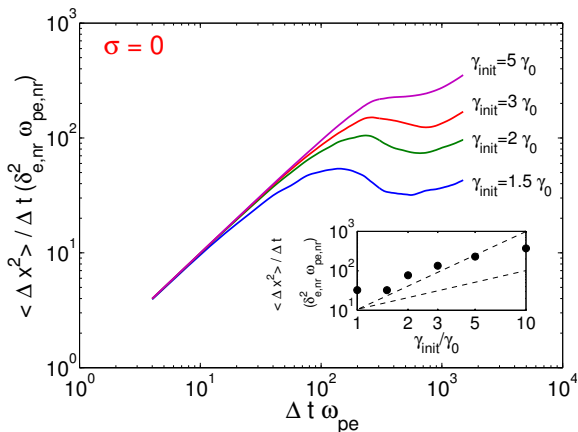
Injected
 8192 test-
 particles /
 energy.
 from wall,
 at $t = 500$



Follow
 kinematics
 between
 500 and
 2000
 plasma
 times

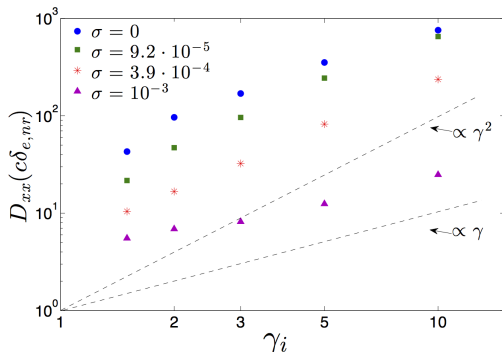
Test-particles kinematics downstream (II)

Diffusion coefficient in the shock propagation direction (Perp. to \vec{B}_0)



Diffusion effectively reached but $D_{\perp} \propto \gamma_i^2$ is not obvious.
 Also the diffusion 'plateau' is not asymptotic...

Test-particles diffusion for increasing σ



D_{\perp} saturation for increasing σ . Result of lower turbulence $\delta B^2/B_0$ level or tighter turbulence region ?

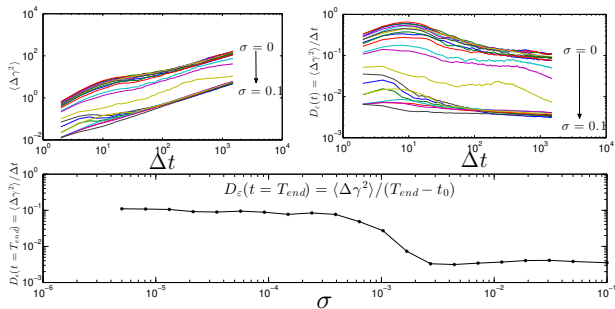
Energy diffusion

In a simple form the Fokker-Planck equation for the shock swept particles writes

$$\frac{\partial f}{\partial t} = \frac{\partial}{\partial \gamma} \left[\mathbf{D} \cdot \frac{\partial f}{\partial \gamma} - \mathbf{A} f \right] \quad (1)$$

$D = \langle \Delta \gamma^2 \rangle / \Delta t$ is the momentum diffusion term responsible for the isotropic part of f (e.g. [Moiseev & Sagdeev 63](#)). Second order in energy.

\mathbf{A} is the drag term \rightarrow First order term.



\rightarrow Clear transition between $\sigma = 10^{-3}$ and $\sigma = 10^{-2}$

Summary and further ideas

- ① Shock structure follows the description by Sironi et al 13, but the precursor structure need a careful attention (importance of perp. current with growing σ , e.g., Lemoine et al. 14 and supplementary analysis here).
- ② Shock jump conditions and speed satisfactorily explained by the ideal MHD for $\sigma < 10^{-4}$ and ideal MHD-EM precursor for $\sigma > 0.1$. Deviation at intermediate σ .
- ③ Shock formation ... at $\sigma < 10^{-4}$ unmagnetized approx. is ok (framework described by Bret et al. 13).
- ④ Requirement for a general formalism at arbitrary magnetization. Theoretically involved because of transverse filamentation is competing with beam cyclotron instability. Also the problem is not periodic. Note that a current-based approach is presented in Lemoine et al. 14
- ⑤ Maximum particle energy $\propto \sqrt{t}$, in consistency with Sironi et al. 13. But $\gamma_{max} \propto \sigma^{-1/2}$ here, at shorter simulation times. While $\propto \sigma^{-1/4}$ in long simulations ($> 10^4 \omega_{pe,rel}^{-1}$).
- ⑥ Downstream particle diffusion scales as E^2 in weakly magnetized shocks but does not hold at intermediate σ . Eventually no diffusion for $\sigma > 10^{-2}$.
- ⑦ Clear transition seen between $\sigma = 10^{-3}$ and $\sigma = 10^{-2}$ shocks.